

# Mutation Testing Meets Approximate Computing

Milos Gligoric<sub>1</sub>, Sarfraz Khurshid<sub>1</sub>, Sasa Misailovic<sub>2</sub>,  
**August Shi<sub>2</sub>**

ICSE NIER 2017

Buenos Aires, Argentina

May 24, 2017

1



CCF-1409423, CCF-1421503,  
CCF-1566363, CCF-1629431,  
CCF-1319688, CNS-1239498

2



# Mutation Testing

- **Goal:** Evaluate quality of test suites
- **How:** Apply transformations (mutation operators) on the code and run tests to see if they can detect the changes
- **Example:**

**x = x + 1**

# Mutation Testing

- **Goal:** Evaluate quality of test suites
- **How:** Apply transformations (mutation operators) on the code and run tests to see if they can detect the changes

- **Example:**

$$x = x + 2$$

- **Problems:**

- Evaluation of quality limited by mutation operators
- Too slow

# Approximate Computing

- **Goal:** Improve performance of code
- **How:** Apply transformations that may lead to (slightly) inaccurate results
- **Example:**

```
for (i = 0; i < n; i = i + 1)
```

# Approximate Computing

- **Goal:** Improve performance of code
- **How:** Apply transformations that may lead to (slightly) inaccurate results

- **Example:**

```
for (i = 0; i < n; i = i + 2)
```

- **Problems:**

- Not sure where in exact code to apply approximations
- Unclear how to check quality of tests on already approximate code

How can  
**Mutation Testing** and  
Approximate Computing  
improve one another?

# Improving One Another

- Approximate computing to provide new mutation operators for **evaluating quality of tests**
- Approximate computing to **improve speed** of mutation testing
- Mutation testing to **point out opportunities** for applying approximations on exact code
- Mutation testing to **evaluate quality of tests** on (already) approximate code

# Example Code: Commons-Math

```
// MathArrays.java
static double[] unique(double[] data) {
```

```
// MathArraysTest.java
void testUnique() {
    double[] x = {0, 9, 3, 0, 11,
        7, 3, 5, -1, -2};
    double[] values = {11, 9, 7,
        5, 3, 0, -1, -2};
    assertEquals(values,
        MathArrays.unique(x), 0);
}
```



**Test Passes**



# Mutant: Constant Replacement

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet<Double> values =
        new TreeSet<>();
    for (int i = 0; i < data.length; i++) {
        values.add(data[i]);
    }
    int count = values.size();
    double[] out = new double[count];
    Iterator<Double> iterator =
        values.descendingIterator();
    int i = 1;
    while (iterator.hasNext()) {
        out[i++] = iterator.next();
    }
    return out;
}
```

```
// MathArraysTest.java
void testUnique() {
    double[] x = {0, 9, 3, 0, 11,
        7, 3, 5, -1, -2};
    double[] values = {11, 9, 7,
        5, 3, 0, -1, -2};
    assertEquals(values,
        MathArrays.unique(x), 0);
}
```



**Test Fails**

**Mutant Killed**

Replace 0 with **1**

# Mutant: Constant Replacement

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet<Double> values =
        new TreeSet<>();
    for (int i = 1; i < data.length; i++) {
        values.add(data[i]);
    }
    int count = values.size();
    double[] out = new double[count];
    Iterator<Double> iterator =
        values.descendingIterator();
    int i = 0;
    while (iterator.hasNext()) {
        out[i++] = iterator.next();
    }
    return out;
}
```

```
// MathArraysTest.java
void testUnique() {
    double[] x = {0, 9, 3, 0, 11,
        7, 3, 5, -1, -2};
    double[] values = {11, 9, 7,
        5, 3, 0, -1, -2};
    assertEquals(values,
        MathArrays.unique(x), 0);
}
```



**Test Passes**

**Mutant Survived**

Replace 0 with **1**

# Approximate: Loop Perforation

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet<Double> values =
        new TreeSet<>();
    for (int i = 0; i < data.length; i+=2)
        values.add(data[i]);
    }
    int count = values.size();
    double[] out = new double[count];
    Iterator<Double> iterator =
        values.descendingIterator();
    int i = 0;
    while (iterator.hasNext()) {
        out[i++] = iterator.next();
    }
    return out;
}
```

```
// MathArraysTest.java
void testUnique() {
    double[] x = {0, 9, 3, 0, 11,
        7, 3, 5, -1, -2};
    double[] values = {11, 9, 7,
        5, 3, 0, -1, -2};
    assertEquals(values,
        MathArrays.unique(x), 0);
}
```



**Test Fails**

Skip every other iteration

68% of runtime is in this loop

Modify assertion

# Approximate: Loop Perforation

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet<Double> values =
        new TreeSet<>();
    for (int i = 0; i < data.length; i+=2)
        values.add(data[i]);
    }
    int count = values.size();
    double[] out = new double[count];
    Iterator<Double> iterator =
        values.descendingIterator();
    int i = 0;
    while (iterator.hasNext()) {
        out[i++] = iterator.next();
    }
    return out;
}
```

Skip every other iteration

68% of runtime is in this loop

```
// MathArraysTest.java
void testUnique() {
    double[] x = {0, 9, 3, 0, 11,
        7, 3, 5, -1, -2};
    double[] values = {11, 9, 7,
        5, 3, 0, -1, -2};
    assertArraySubset(values,
        MathArrays.unique(x), 0);
}
```



**Test Passes**

**Approximation is Acceptable**

# Comparison of Transformation Results

Mutation  
Testing

Approximate  
Computing

Failing Test



Passing Test



# Comparison of Transformation Results

Mutation  
Testing

Approximate  
Computing

Failing Test



Passing Test



# Approx. Transformation as Operator

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet<Double> values =
        new TreeSet<>();
    for (int i = 0; i < data.length; i++)
        values.add(data[i]);
    }
    int count = values.size();
    double[] out = new double[count];
    Iterator<Double> iterator =
        values.descendingIterator();
    int i = 0;
    while (iterator.hasNext()) {
        out[i++] = iterator.next();
    }
    return out;
}
```

```
// MathArraysTest.java
void testUnique() {
    double[] x = {0, 9, 3, 0, 11,
        7, 3, 5, -1, -2};
    double[] values = {11, 9, 7,
        5, 3, 0, -1, -2};
    assertEquals(values,
        MathArrays.unique(x), 0);
}
```

# Approx. Transformation as Operator

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet<Double> values =
        new TreeSet<>();
    for (int i = 0; i < data.length; i+=2)
        values.add(data[i]);
    }
    int count = values.size();
    double[] out = new double[count];
    Iterator<Double> iterator =
        values.descendingIterator();
    int i = 0;
    while (iterator.hasNext()) {
        out[i++] = iterator.next();
    }
    return out;
}
```

```
// MathArraysTest.java
void testUnique() {
    double[] x = {0, 9, 3, 0, 11,
        7, 3, 5, -1, -2};
    double[] values = {11, 9, 7,
        5, 3, 0, -1, -2};
    assertEquals(values,
        MathArrays.unique(x), 0);
}
```



**Test Fails**

**Mutant Killed**

Replace `i++` with `i+=2`  
Perforates loop



# Questions for Approx. Operators

- Do killed approximate mutants indicate different strengths? Do surviving approximate mutants indicate new weaknesses in the test suite?
- How do mutants generated by approximate computing differ from traditional mutants?
- Are approximate mutants faster than traditional mutants?

# Mutants Find Approx. Opportunities

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet<Double> values =
        new TreeSet<>();
    for (int i = 0; i < data.length; i++)
        values.add(data[i]);
    }
    int count = values.size();
    double[] out = new double[count];
    Iterator<Double> iterator =
        values.descendingIterator();
    int i = 0;
    while (iterator.hasNext()) {
        out[i++] = iterator.next();
    }
    return out;
}
```

```
// MathArraysTest.java
void testUnique() {
    double[] x = {0, 9, 3, 0, 11,
        7, 3, 5, -1, -2};
    double[] values = {11, 9, 7,
        5, 3, 0, -1, -2};
    assertEquals(values,
        MathArrays.unique(x), 0);
}
```

# Mutants Find Approx. Opportunities

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet<Double> values =
        new TreeSet<>();
    for (int i = 1; i < data.length; i++)
        values.add(data[i]);
}
int count = values.size();
double[] out = new double[count];
Iterator<Double> iterator =
    values.descendingIterator();
int i = 0;
while (iterator.hasNext()) {
    out[i++] = iterator.next();
}
return out;
}
```

```
// MathArraysTest.java
void testUnique() {
    double[] x = {0, 9, 3, 0, 11,
        7, 3, 5, -1, -2};
    double[] values = {11, 9, 7,
        5, 3, 0, -1, -2};
    assertEquals(values,
        MathArrays.unique(x), 0);
}
```



**Test Passes**



**Approximable?**

Replace 0 with **1**

# Questions for Approx. Opportunities

- How can we classify surviving mutants?  
Are they good for approximate computing?
- What approximations are applicable for which surviving mutants?
- How can we tailor mutants for the purpose of finding approximate computing opportunities?

# Improving One Another

- Approximate computing to provide new mutation operators for **evaluating quality of tests** 
- Approximate computing to **improve speed** of mutation testing
- Mutation testing to **point out opportunities** for applying approximations on exact code 
- Mutation testing to **evaluate quality of tests** on (already) approximate code

More in paper!

# Conclusions

- Approximate computing can provide new mutation operators
- Mutation testing can show opportunities for approximate computing on exact code
- There is so much more we can do  
(More directions in the paper)

**August Shi: [awshi2@illinois.edu](mailto:awshi2@illinois.edu)**

BACKUP

# Mutating Approximate Code?

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet<Double> values =
        new TreeSet<>();
    for (int i = 1; i < data.length; i++) {
        if (i%2 != 0) continue;
        values.add(data[i]);
    }
    return values.toArray();
}
```

```
// MathArraysTest.java
void testUnique() {
    double[] x = {0, 9, 3, 0, 11,
        7, 3, 5, -1, -2}
    double[] values = {11, 9, 7,
        5, 3, 0, -1, -2};
    assertEquals(values,
        MathArrays.unique(x), 0);
}
```



Test Passes

Replace 0 with **1**



# Mutation testing approximate code?

Approximate Transformation	Instance	% Mutants Killed
Exact Version	N/A	95
Loop Perforation (Line 04)	Skip every 2 <sup>nd</sup> iteration	100
	Skip every 4 <sup>th</sup> iteration	95
	Only execute every 4 <sup>th</sup> iteration	100

What precisely do these changes in percentages mean?

# Directions for Research

- If approximate version is proxy of exact version, is mutation score of approximate version also proxy of mutation score of exact version?
  - Do I get same confidence in quality of tests at cheaper cost?
- If so, what are the exact conditions where they are good proxies?

# Approximate Code to Speed up Testing?

```
// MathArrays.java
```

```
01. static double[] unique(double[] data) {
02.     TreeSet values =
03.         new TreeSet<>();
04.     for (int i = 0;
05.         i < data.length; i++) {
06.         if (i%2 != 0) continue;
07.         values.add(data[i]);
08.     }
09.     int count = values.size();
10.     double[] out = new double[count];
11.     Iterator iterator =
12.         values.descendingIterator();
13.     int i = 0;
14.     while (iterator.hasNext()) {
15.
16.         out[i++] = iterator.next();
17.     }
19.     return out;
20. }
```

```
// MathArraysTest.java
```

```
void testUnique() {
    double[] x = {0, 9, 3, 0, 11,
                 7, 3, 5, -1, -2}
    double[] values = {11, 3,
                      0, -1};
    assertEquals(values,
                 MathArrays.unique(x), 0);
}
```

Loop (line 04) takes  
68% of runtime

Perforation can cut  
time in half

# Approximate Code to Speed up Testing?

// MathArrays.java

```
01. static double[] unique(double[] data) {
02.     TreeSet values =
03.         new TreeSet<>();
04.     for (int i = 0;
05.         i < data.length; i++) {
06.         if (i%2 != 0) continue;
07.         values.add(data[i]);
08.     }
09.     int count = values.size()
10.     double[] out = new double[count];
11.     Iterator iterator =
12.         values.descendingIterator();
13.     int i = 0;
14.     while (iterator.hasNext()) {
15.
16.         out[i++] = iterator.next();
17.     }
19.     return out;
20. }
```

// MathArraysTest.java

```
void testUnique() {
    double[] x = {0, 9, 3, 0, 11,
        7, 3, 5, -1, -2}
    double[] values = {11, 9, 7,
        5, 3, 0, -1, -2};
    assertApproxEquals(values,
        MathArrays.unique(x), 0
        0.8);
}
```

Introduce new assertions?

# Example: Mutation Testing (SURVIVED)

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet values =
        new TreeSet<>();
    for (int i = 0;
        i < data.length; i++) {

        values.add(data[i]);
    }
    int count = values.size()
    double[] out = new double[count];
    ...
    return out;
}
```

Original



Constant  
Replacement

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet values =
        new TreeSet<>();
    for (int i = 1;
        i < data.length; i++) {

        values.add(data[i]);
    }
    int count = values.size()
    double[] out = new double[count];
    ...
    return out;
}
```

Mutant

```
// MathArraysTest.java
void testUnique() {
    double[] x = {0, 9, 3, 0, 11,
        7, 3, 5, -1, -2}
    double[] values = {11, 9, 7, 5, 3,
        0, -1, -2};
    assertEquals(values,
        MathArrays.unique(x), 0);
}
```

Test passes on original

Test passes on mutant => Mutant SURVIVED

# Example: Mutation Testing (KILLED)

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet values =
        new TreeSet<>();
    for (int i = 0;
        i < data.length; i++) {
        values.add(data[i]);
    }
    int count = values.size()
    double[] out = new double[count];
    ...
    return out;
}
```

Original



Boundary  
Mutator

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet values =
        new TreeSet<>();
    for (int i = 0;
        i <= data.length; i++) {
        values.add(data[i]);
    }
    int count = values.size()
    double[] out = new double[count];
    ...
    return out;
}
```

Mutant

```
// MathArraysTest.java
void testUnique() {
    double[] x = {0, 9, 3, 0, 11,
        7, 3, 5, -1, -2}
    double[] values = {11, 9, 7, 5, 3,
        0, -1, -2};
    assertEquals(values,
        MathArrays.unique(x), 0);
}
```

Test passes on original

Test passes on mutant => Mutant KILLED

# Example: Loop Perforation

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet values =
        new TreeSet<>();
    for (int i = 0;
        i < data.length; i++) {

        values.add(data[i]);
    }
    int count = values.size()
    double[] out = new double[count];
    ...
    return out;
}
```

Original



**Skip Every  
Other Iteration**

```
// MathArrays.java
static double[] unique(double[] data) {
    TreeSet values =
        new TreeSet<>();
    for (int i = 0;
        i < data.length; i+=2) {

        values.add(data[i]);
    }
    int count = values.size()
    double[] out = new double[count];
    ...
    return out;
}
```

Mutant