

## Syntax and semantics of rules

Will study classification based on header fields

- IP src/dest addresses, protocol, TCP src/dest ports

Syntactically, rule is *(predicate, action)* pair

- predicate is sequence of prefixes, one per header field
  - in some formulations, use intervals for succinctness
- action is an integer in some range  $[0, A - 1]$

Semantically, packet satisfies predicate iff each header field from packet matches corresponding prefix

- rule-set — collection of rules
- each rule is given a priority, action taken is that of (any) highest priority rule satisfied by packet

## Working example

Rule	F1	F2
R1	00*	00*
R2	0*	01*
R3	1*	0*
R4	00*	0*
R5	0*	1*
R6	*	1*

Rules ordered from top to bottom

## Packet Classification

Adnan Aziz

The University of Texas

References:

- P. Gupta. Algorithms for routing lookups and packet classification. PhD Thesis, Stanford University, 2001.
  - Excellent survey, pages 106–128; recursive flow classification
- F. Baboescu and G. Varghese. Scalable packet classification. ACM SIGCOMM, 2001.
- P. Agrawal and J. Erickson. Geometric range searching and its relatives.
  - Rigorous, mathematical treatment.

## Motivation

IP networks have very limited support for QoS, security, accounting

- customers unwilling to commit to IP-based infrastructure

In principle, packet classification could help solve these problem

- differentiate between customers, type of traffic

In practise, performance drops dramatically

- number of algorithms & architectures for fast packet classification

### Relationship with computational geometry

A 2-D rule represents a rectangle parallel to the axes

- rule in  $d$ -dimensions —  $d$ -dimensional hyper-rectangle
- packet with  $d$  fields in header — point in  $d$ -dimensional space

Classifier is collection of rectangles, each labeled with priority

- classification: find highest priority rectangle containing packet

Point location problem:

- given set of nonoverlapping regions in  $d$ -dimensional space, find region containing point

Claim commonly made that packet classification is as hard as point location problem

- not clear (to me): coming from prefixes

Best bounds for point location:  $N$  regions,  $d$  dimensions (can do better in 2-D and 3-D)

- $\Theta(\log N)$  time with  $\Theta(N^d)$  space
- $\Theta((\log N)^{d-1})$  time with  $\Theta(N)$  space

Conclusion: need heuristics that exploit statistics of rule-sets seen in practise

### Computational complexity

First implementation of firewalls: linear scan, with some tricks

- works fine for 3 Mb Ethernet, 10 rules in rule-set

Innate complexity: performing classification is akin to searching geometrical structures

- recall from IP forwarding: prefix corresponds to interval of  $[0, 2^{32} - 1]$

Given set of  $N$  disjoint ranges  $\{[l_1, u_1], \dots, [l_N, u_N]\}$  partitioning  $[0, 2^{32} - 1]$  range lookup problem is to find range corresponding to point  $P$

- assumption: lots of lookups, can spend time preprocessing set
- various solutions: binary search on endpoints, prefix matching (convert range to set of prefixes)
  - $[4, 7]$  — 01\*\*; Interval  $[3, 8]$  — 0011, 01\*\*, 1000; Interval  $[1, 14]$  — 0001, 001\*, 01\*\*, 10\*\*, 110\*, 1100
  - worst case: range on  $W$ -dimensions becomes  $2^W - 2$  prefixes

How to lookup  $(v_1, v_2, \dots, v_d)$ ?

- proceed recursively in each dimension
- at **each** F1-trie node, follow next-trie pointer recursively
- encounter a rule iff rule matches  $\Rightarrow$  keep record of highest priority rule

Complexity:

- space —  $\Theta(N \cdot d \cdot W)$  “rake”
- time — Gupta says  $O(W^d)$ ??? Looks like DFS,  $\Theta(N \cdot d \cdot W)$ ???

### Set-pruning tries

Improve search time by replication

- construction similar to that of hierarchical trie
  - for **each** prefix  $p$  in  $F1$ , recursively construct  $(d-1)$ -dimensional trie  $T_p$  on those rules which specify  $p$  **or** a prefix of  $p$  in first dimension
  - conceptually “pushing” down prefixes

### Hardware solution — TCAMs

Very much in spirit of IP forwarding. TCAM essential, cannot do with CAMs (great diversity in lengths)

Very much as in IP forwarding

- select highest priority matching rule with priority encoder
- need to pipeline for performance
- various architectures trading off area/time, lookup/update
- same problems (density/cost, power)

### Hierarchical tries

Natural extension of tries; construct recursively

- $d = 1$ , very similar to usual trie (difference???)
- $d > 1$ , construct  $F1$  trie on prefixes from first dimension
  - use next-trie pointer to link  $p$  to  $T_p$

Convince yourself that the hierarchical trie actually captures rule-set

### Crossproducting

Basic idea — first identify which interval in each field incoming packet lies in

- index into multidimensional array to find highest priority rule

Details: use binary search on array of endpoints for interval identification

- $N$  rules implies  $\Theta(\lg N \cdot d)$  complexity: search on each field,  $\Theta(\lg N)$  time since, prefixes partition number line into at most  $2N$  intervals
- if  $G_k$  is set of intervals corresponding to  $k$ -th field, multidimensional array is of size  $\prod_{i=1}^d |G_i|$

### Tuple-state space search

Very similar to binary search on hash tables for IP forwarding

Map each  $d$ -dimensional rule into a  $d$ -tuple of integers, whose  $i$ -th component denote the length of prefix in  $i$ -th dimension

- $M$  distinct tuples  $\Rightarrow$  build  $M$  hashtables, do  $M$  hash lookups
- improve upon  $M$  by using markers, perform binary search

No markers —  $O(N)$  storage, with markers?

Note: Same authors continue to publish very different schemes

Search for  $(v_1, v_2, \dots, v_d)$  by finding longest matching prefix of  $v_1$ , follow its next trie pointer, recurse

- guaranteed every matching rule encountered

Complexity:

- time —  $\Theta(W \cdot d)$  (no backtrack!)
- space —  $\Theta(N^d \cdot d \cdot W)$

### 2-D classification

Can do  $O(N)$  space and  $O(W)$  time in two dimensions (as opposed to  $\Theta(N^2)$  space from set-pruning tries)

- first dimension — prefix, second dimension — arbitrary interval

Intuition: order prefixes on first field by length, use pruning information from search on previous length on second field

## Recursive flow classification

View as logic function mapping  $S$  bits in header to  $T = \lceil \lg N \rceil$  bits

- directly create table  $\Rightarrow$  size  $2^S$

RFC: basic idea is to “re-encode” input space

- suppose rule-set is on 5 header fields, and for each field rule-set engenders at most 16 intervals
  - encode interval with 4 bits  $\Rightarrow$  can solve with lookup table with  $2^{20}$  entries

Unfortunately, nontrivial rule-set won't yield so few intervals on each field

- iterate construction: map 16 bits to 8, combine pairs, repeat

Which pairs to combine: most “correlated” so as to reduce the number of equivalence classes

- no details on this

Results: 2 4Mb SRAM, 2 4-bank 64 Mb SDRAM, 125 Mhz suffices for all rule-sets

Updates: delete easy, insert hard

Relationship to BDDs?

## Bitmap intersecting

Foundation: Set of rules  $S$  matching a packet is  $\cap_{i=1}^d S_i$ , where  $S_i$  is rules matching in  $i$ -th dimension

- compute  $S_i$  using binary search on interval endpoint
- take intersection efficiently by encoding subset of rule-set as  $N$  bit vector
- index rules in decreasing order of priority

Storage:  $\Theta(d \cdot N \cdot N)$ , time is  $\Theta(d \cdot \lg N + d \cdot N/w)$ , where  $w$  is word length

- parallel hardware  $\Rightarrow$  reduce by a factor of  $d$

F. Baboescu and G. Varghese SIGCOMM 01 extend this scheme by performing aggregation on the bit vectors

- individual  $S_i$  sets tend to be small, so corresponding bit vectors are sparse
  - actually, if even one  $S_i$  is small, scheme works well
- rather than AND  $N$ -bit vectors, aggregate (OR)  $A$  consecutive bits, then search only in locations where conjunction of aggregated vectors evaluates to 1
- reorder rule indices to get sparser aggregated vectors
  - heuristic: sort on rules on prefix length
  - nontrivial: given  $k$  sets  $S_1, \dots, S_k$  of  $N$ -bit vectors, it's NP-complete to find if  $\exists x_i \in S_i$  such that  $\cap_{i=1}^d x_i \neq 0$