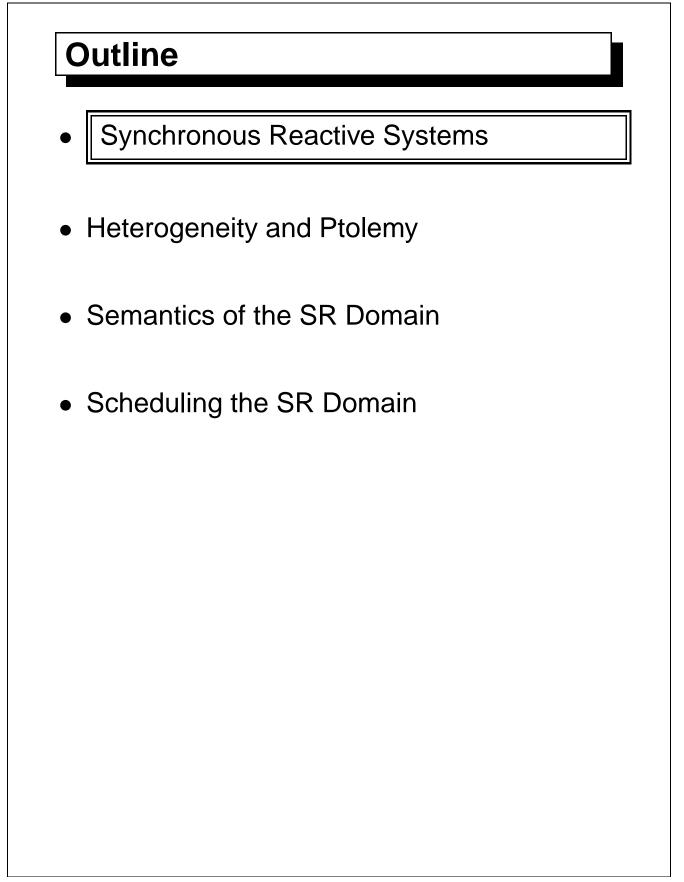
Synchronous Reactive Systems

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Reactive Embedded Systems

- Run at the speed of their environment
- When as important as what
- Concurrency for controlling the real world
- Determinism desired
- Limited resources (e.g., memory)
- Discrete-valued, time-varying
- Examples:
 - Systems with user interfaces
 - * Digital Watches
 - * CD Players
 - Real-time controllers
 - * Anti-lock braking systems
 - * Industrial process controllers

The Digital Approach

Why do we build digital systems?

- Voltage noise is unavoidable
- Discretization plus non-linearity can filter out low-level noise completely
- Complex systems becomes predictable and controllable
- Incredibly successful engineering practice

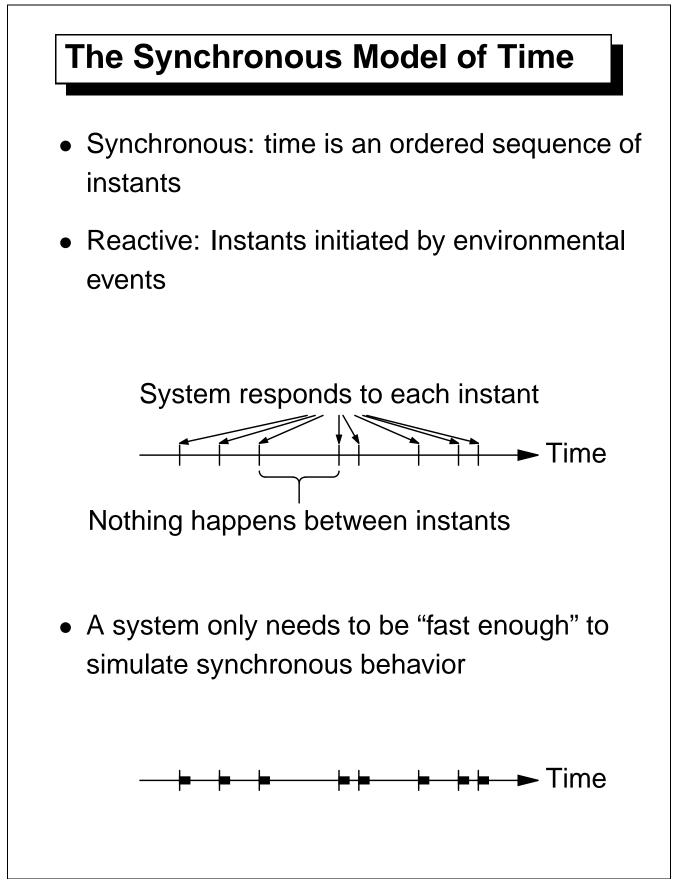
The Synchronous Approach

Idea: Use the same trick to filter out "time noise."

- Noise: Uncontrollable and unpredictable delays
- Discretization ⇔ global synchronization
- The synchrony hypothesis:

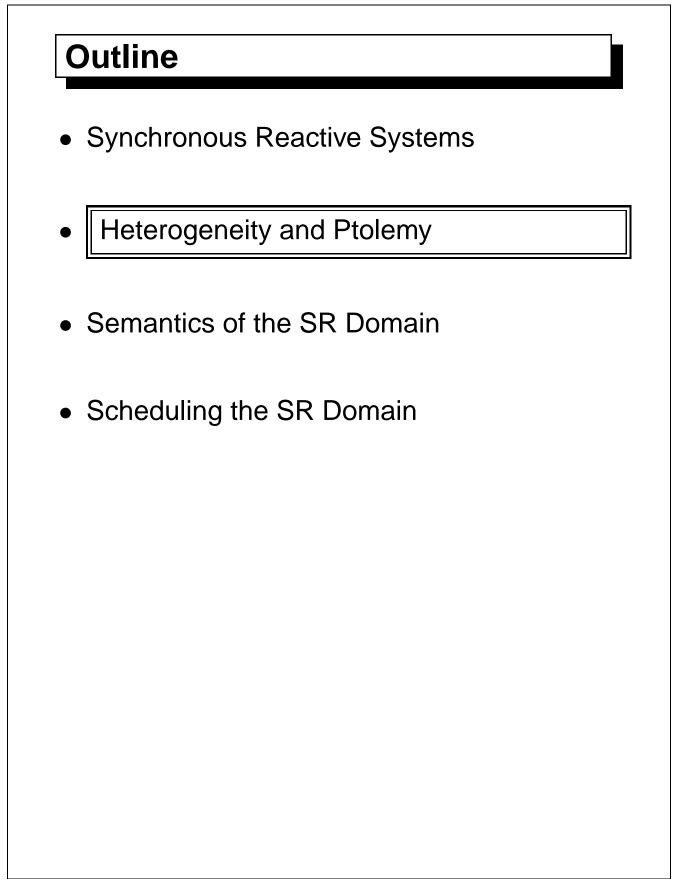
Things compute instantaneously

- Already widespread:
 - Synchronous digital systems
 - Finite-state machines



Who Uses This Stuff?

- Virtually all digital logic designed this way
- In software,
 - Dassult (French aircraft manufacturer)
 builds avionics with synchronous software
 - Polis (Berkeley HW/SW codesign project) uses Esterel for specifying EFSMs
 - Cadence built product (Cierto VCC) based on Polis
 - TI exploring using synchronous software for specifying/simulating DSPs



Heterogeneity

Why are there so many system description languages?

- Want a succinct description for *my* system.
- "Let the language fit the problem"

Bigger systems have more diverse problems; use a fitting language for each subproblem.

Want a heterogeneous coordination scheme that allows many languages to communicate.

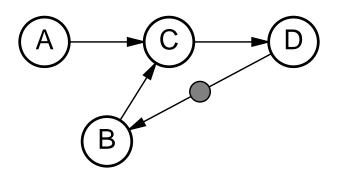
Heterogeneity in Ptolemy

Ptolemy: A system for rapid prototyping of heterogeneous systems

A Ptolemy *domain* (model of computation):

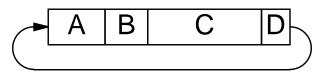
• Set of blocks:

Atomic pieces of computation that can be "fired" (evaluated).



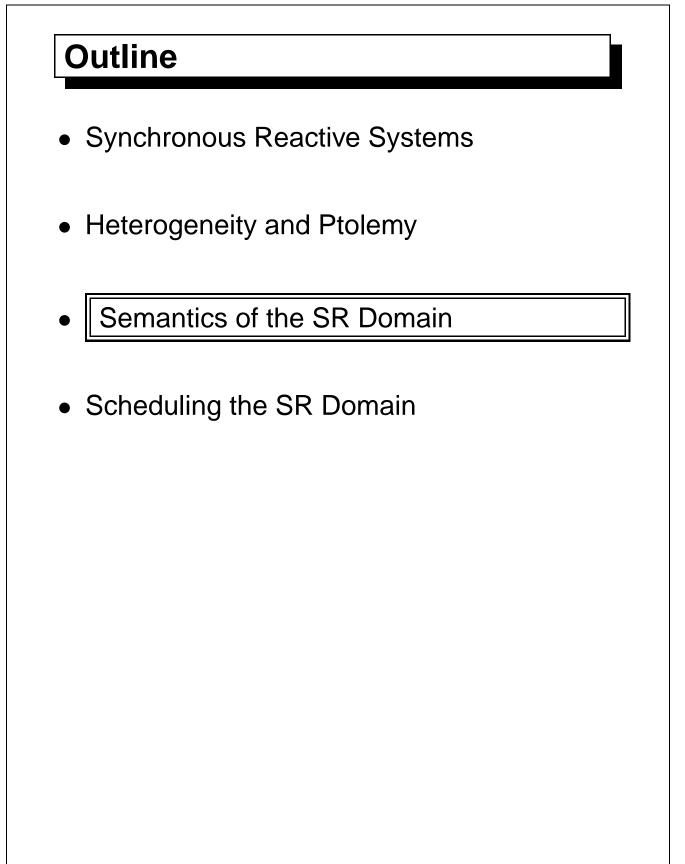
• Scheduler:

Determines block firing order before or during system execution.



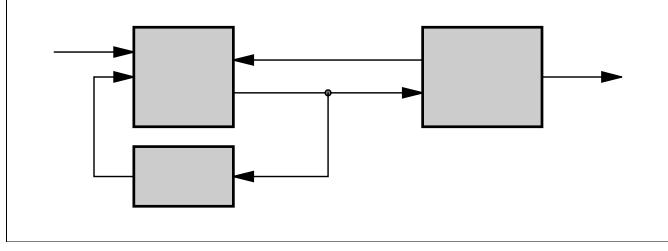
Schedulers Support Heterogeneity

- Scheduler does not know block contents, only how to fire
- Block contents may be anything
- "Wormhole": A block in one domain that behaves as a system in another
- Hierarchical heterogeneity: Any system may contain subsystems described in different domains

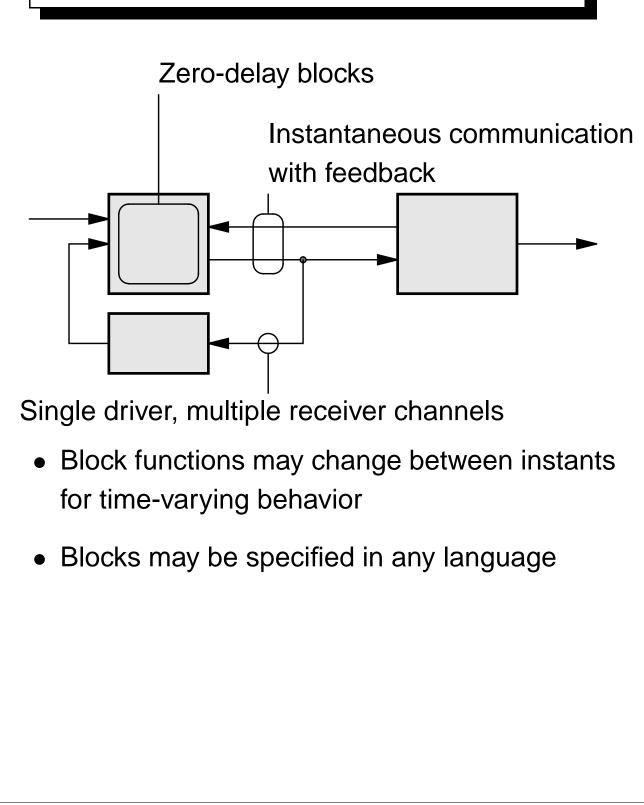


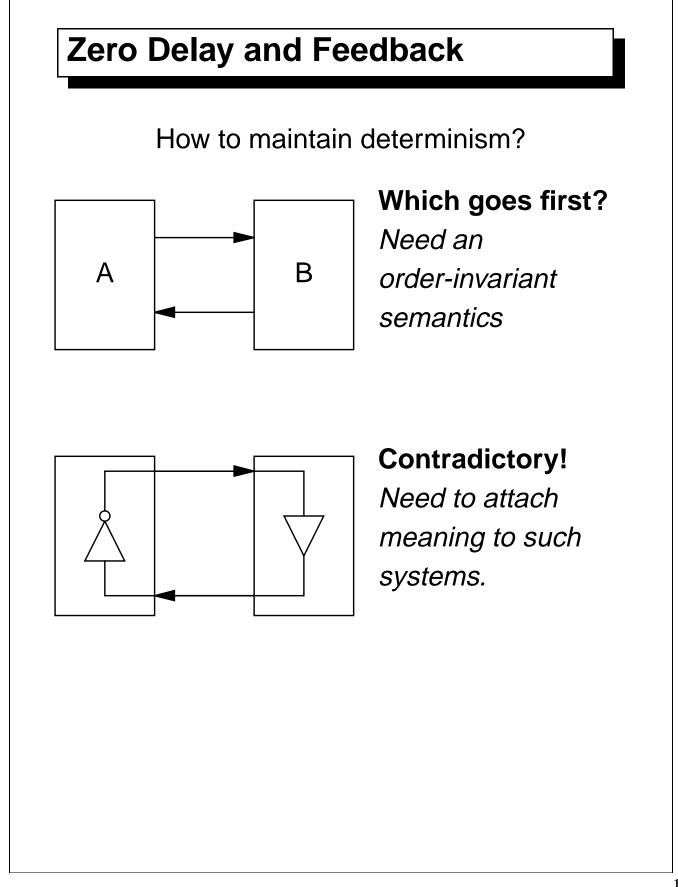
The SR Domain

- Reactive systems need concurrency
- The synchronous model makes for deterministic concurrency
 - No "interleaving" semantics
 - Events are totally-ordered
 - "Before," "after," "at the same time" all well-defined and controllable
- Embedded systems need boundedness; dynamic process creation a problem
- SR system: fixed set of synchronized, communicating processes



The SR Domain (2)

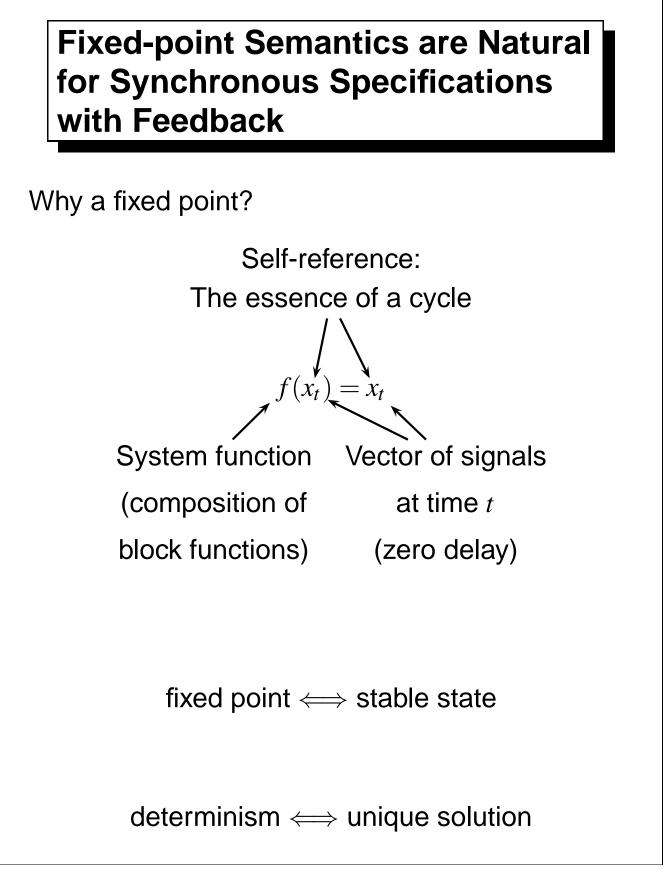




Dealing with Feedback

Why bother at all? Answer: *Heterogeneity*

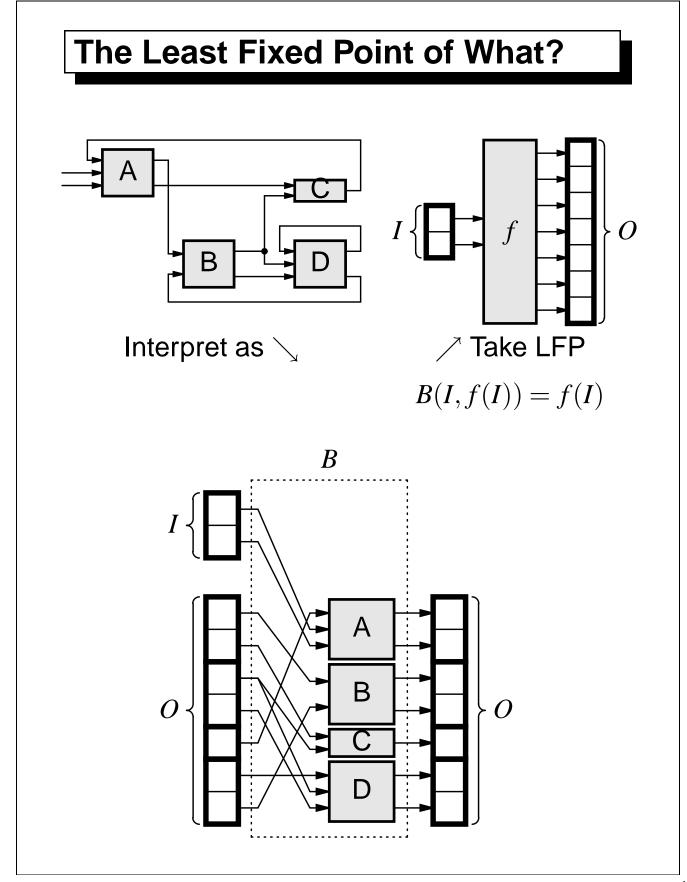
- Cycles are usually broken by delay elements at the lowest level
- Some schemes insist on this
- False feedback often appears at higher levels
- Data dependent cycles can appear when sharing resources
- Virtually all cycles are "false," yet must be dealt with.

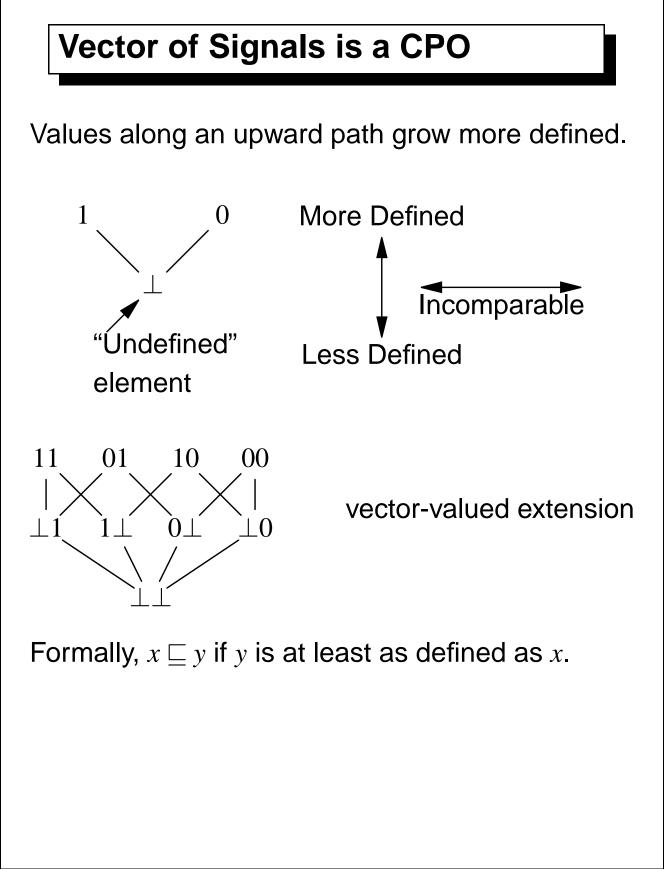


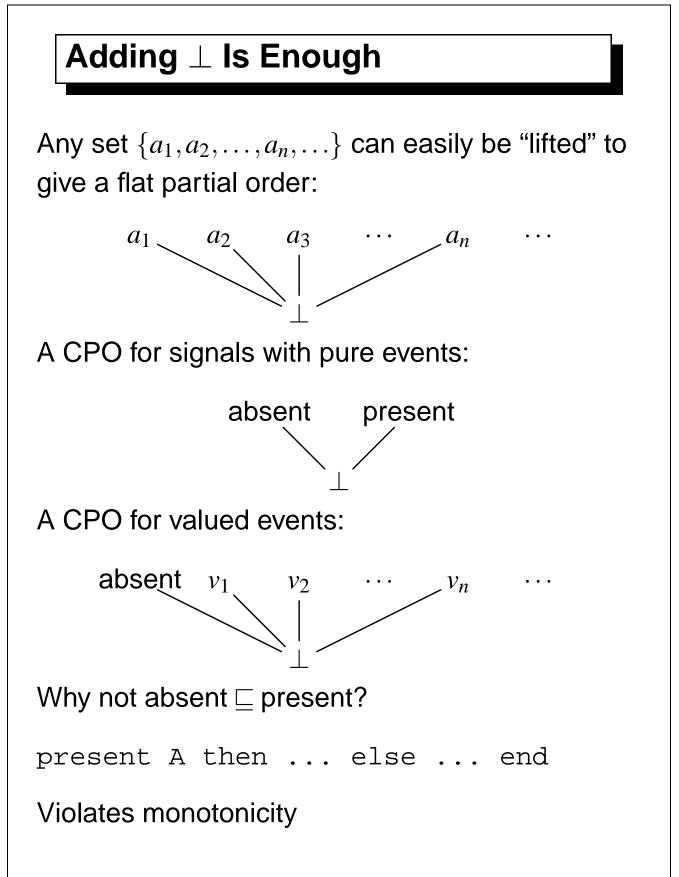
Unique Least Fixed Point Theorem

A monotonic function on a complete partial order (with \perp) has a unique least fixed point.

What does it mean to make the system function f monotonic and the signal values a CPO?

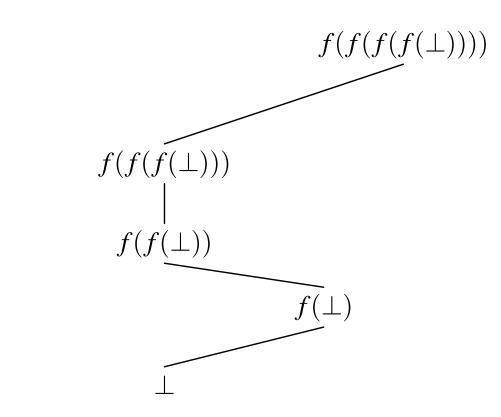






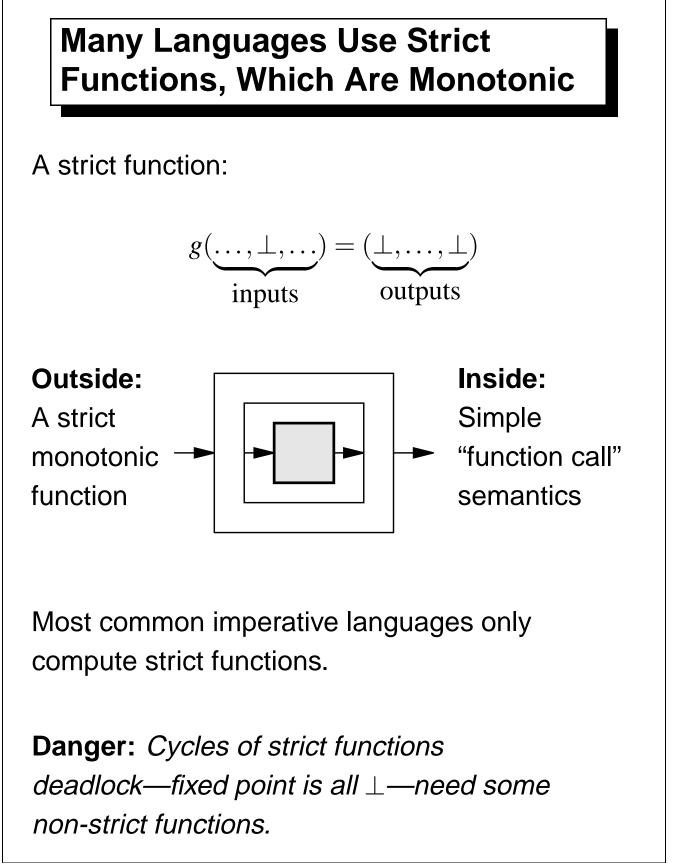
Monotonic Block Functions

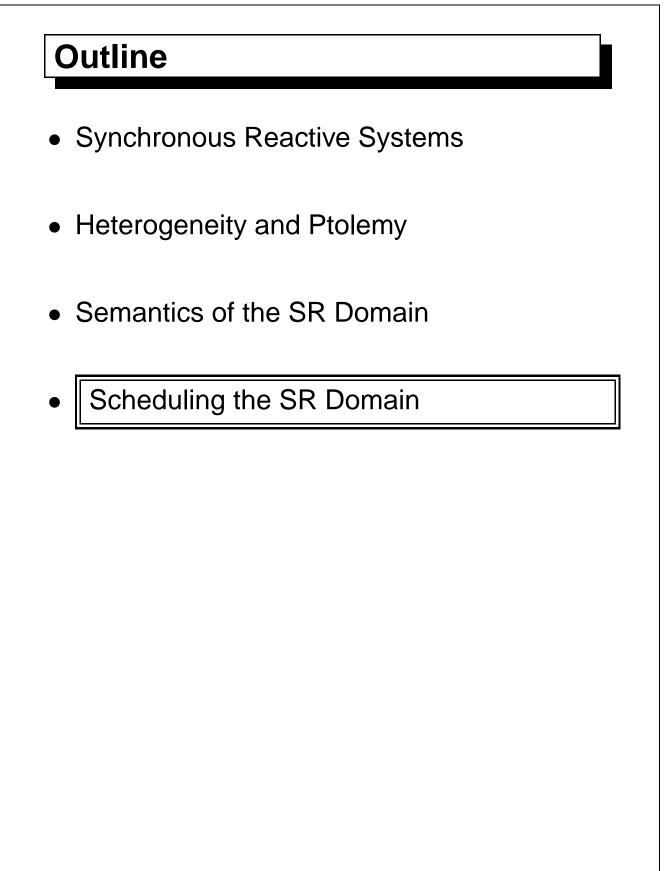
Giving a more defined input to a monotonic function always gives a more defined output.

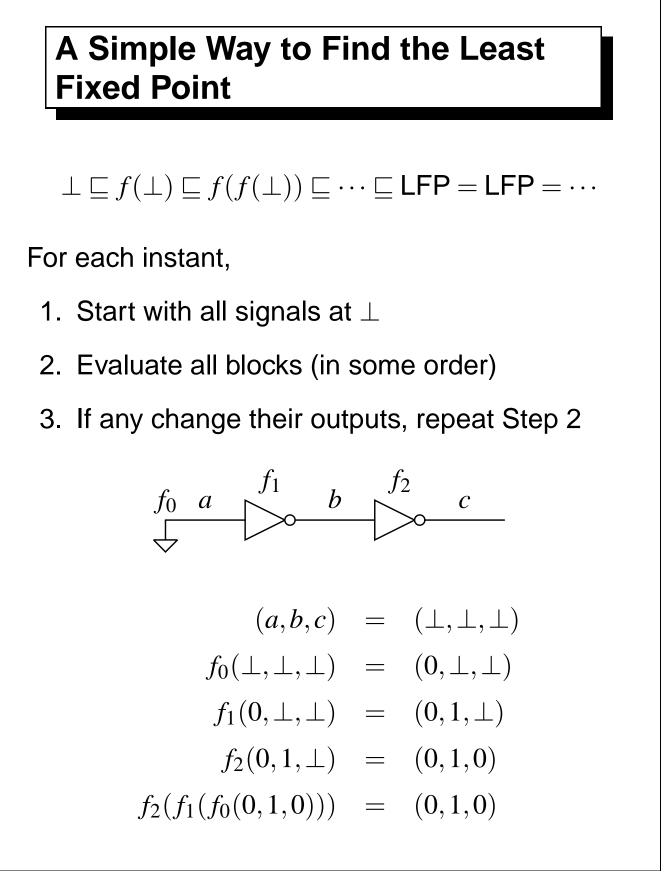


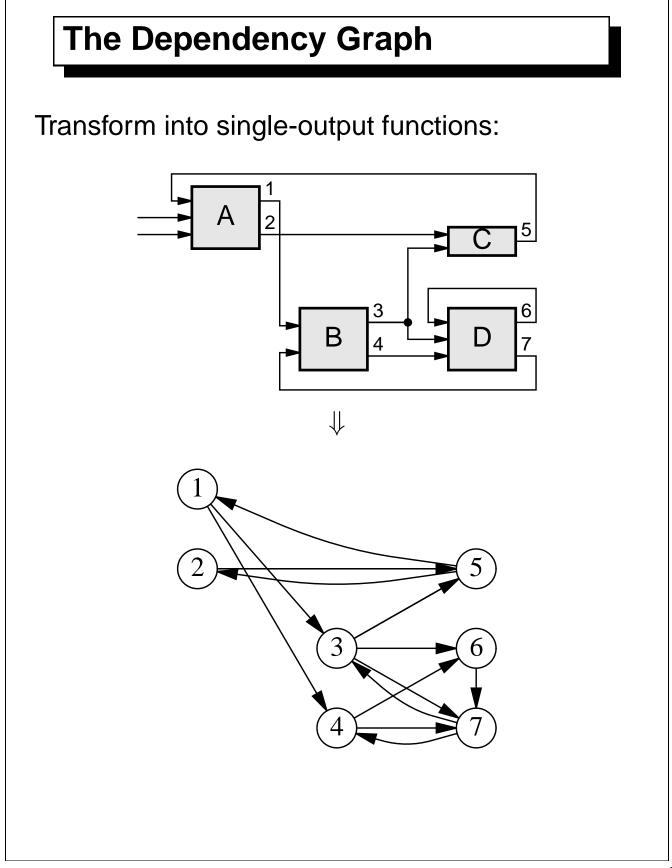
Formally, $x \sqsubseteq y$ implies $f(x) \sqsubseteq f(y)$.

A monotonic function never recants ("changes its mind").







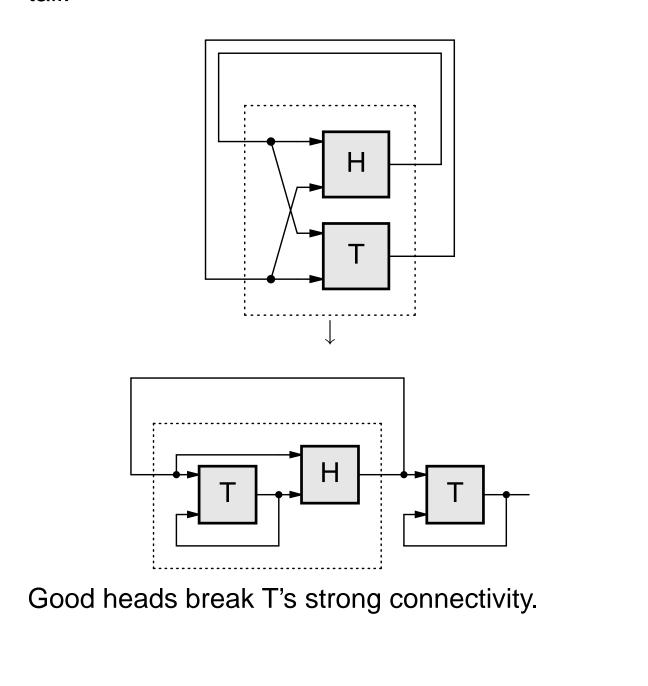


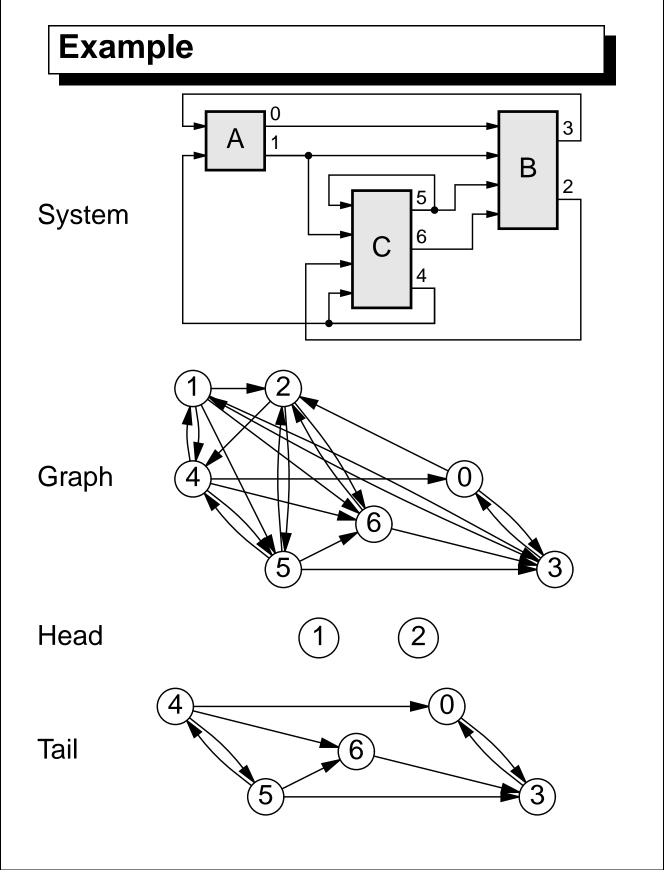
The Scheduling Algorithm

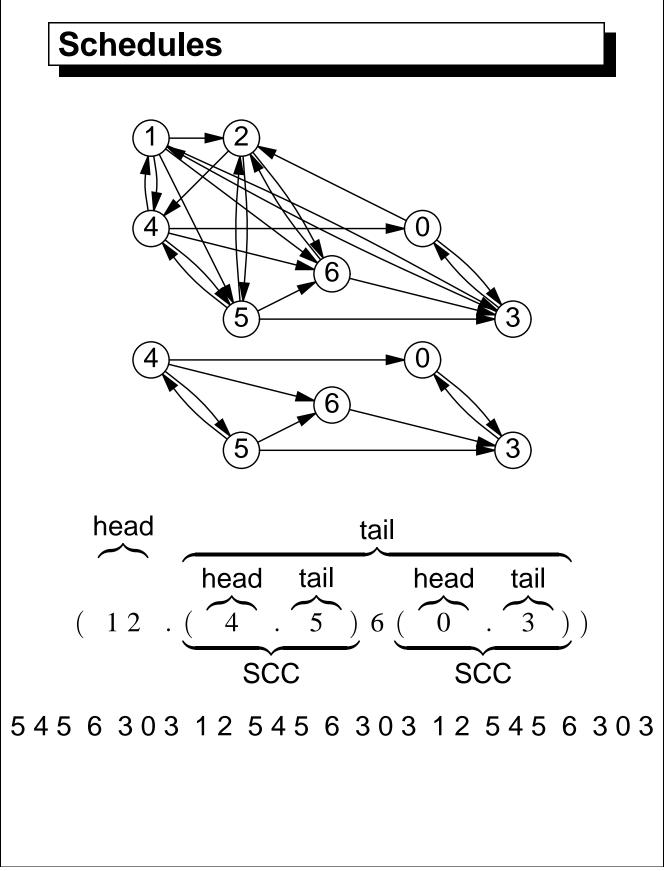
- 1. Decompose into strongly-connected components
- 2. Remove a head (set of vertices) from each SCC, leaving a tail
- 3. Recurse on each tail

Evaluating SCCs

Split a strongly-connected graph into a head and tail:

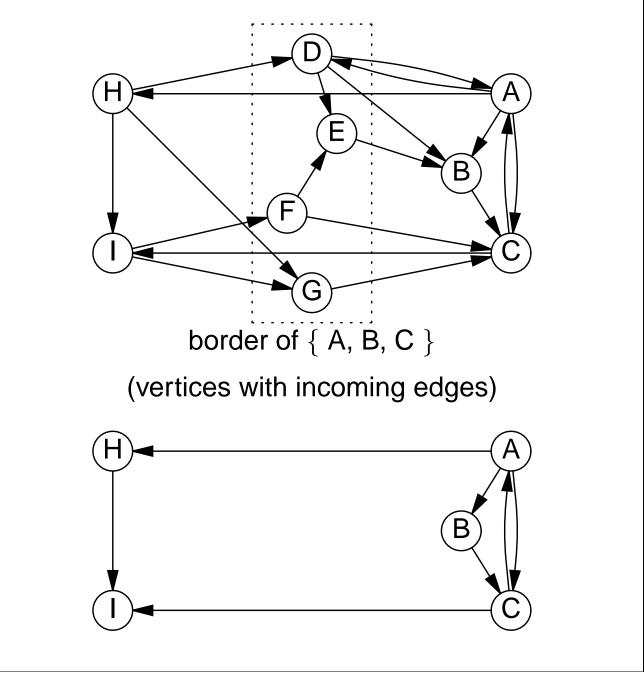






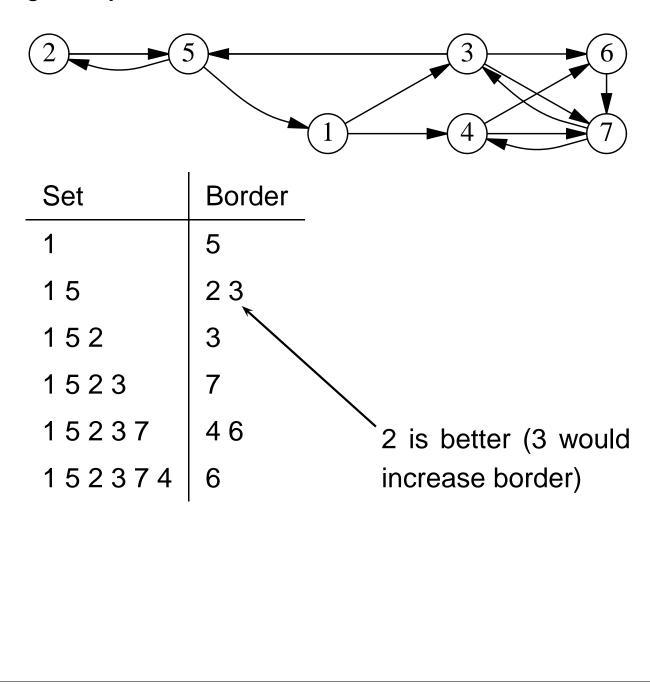
Finding Good Heads

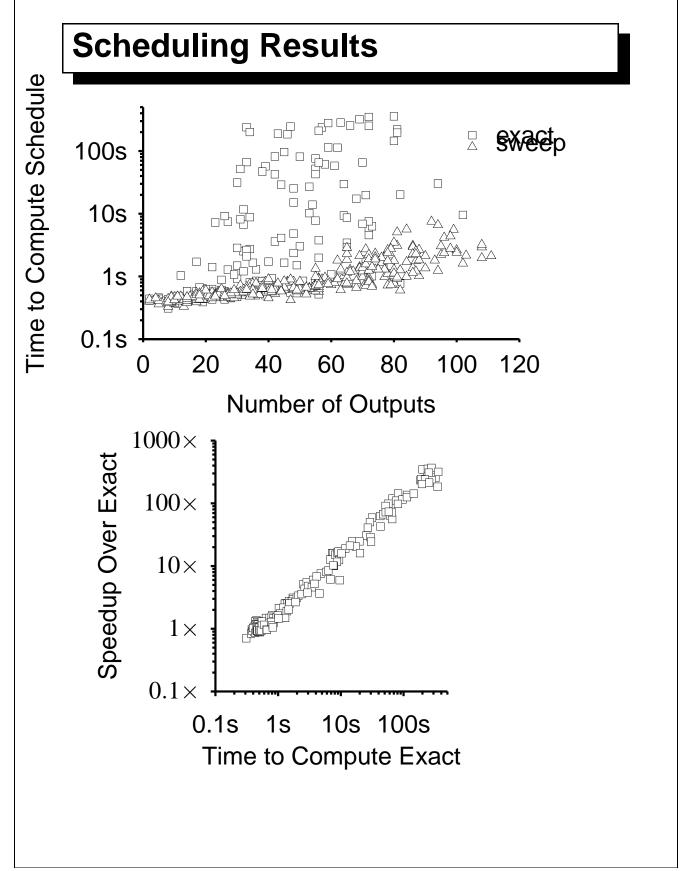
Must break strong connectivity—remove a border of a set of vertices:

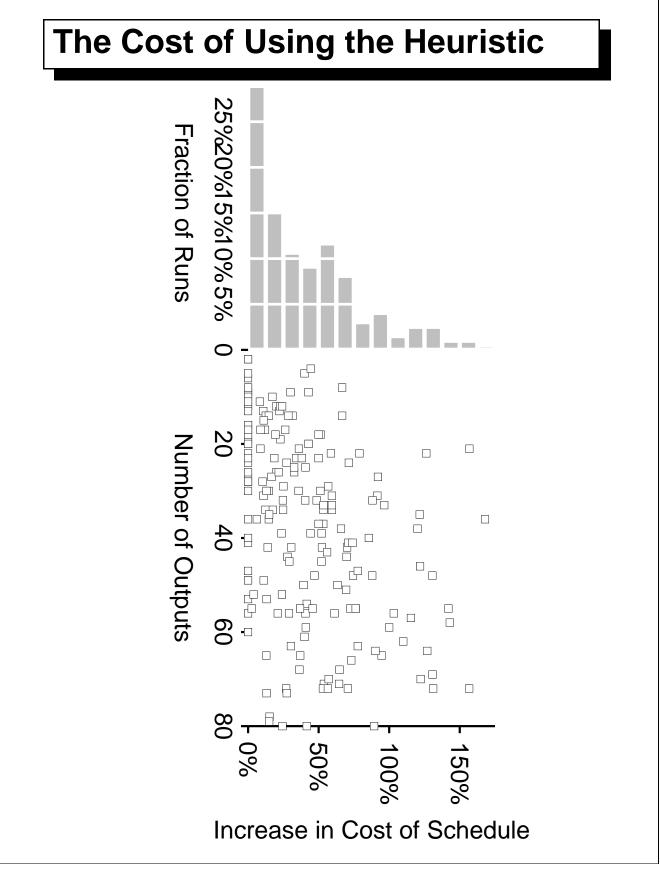


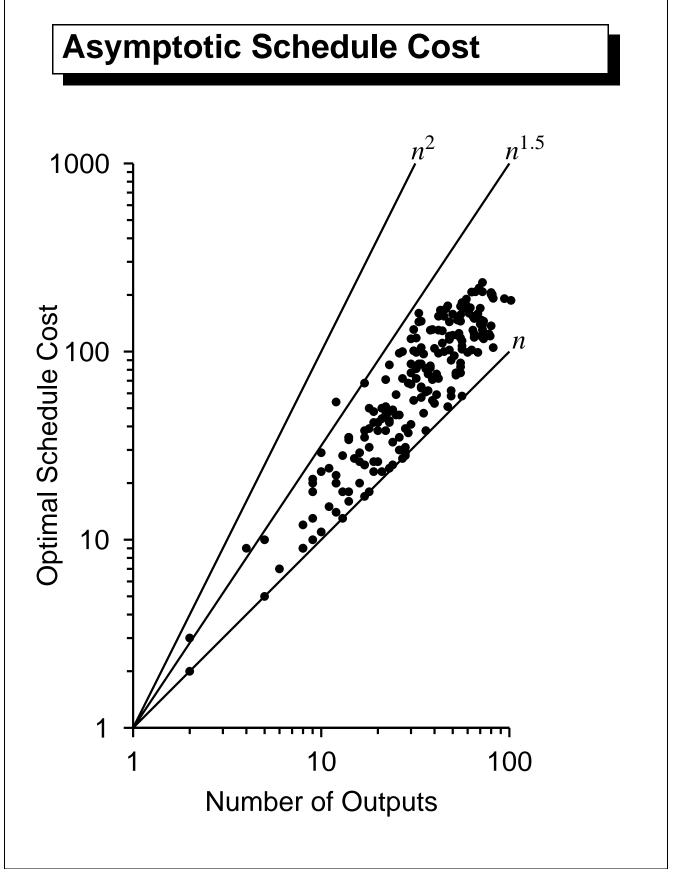
Choosing Good Border Sets

Heuristic: "Grow" a set starting from a vertex and greedily include the best border vertex:









Conclusions

- Reactive embedded systems
 - Run at the speed of their environment
 - When as important as what
 - Concurrent, deterministic, bounded, discrete-valued
- The synchronous approach
 - Discrete instants, globally synchronized
 - Assumes instantaneous computation
- Heterogeneity in Ptolemy
 - Domain: Blocks and Scheduler
 - Hierarchical heterogeneity through domain embedding

Conclusions (2)

- The SR domain
 - Concurrent zero-delay blocks
 - Semantics: the least fixed point of a monotonic function on a CPO
 - Values include "undefined" (\perp)
- Scheduling the SR Domain
 - Use single-output dependency graph
 - Decompose into SCCs; remove a head from each; recurse
 - Head is the border of the tail
 - Choose a head by greedily growing a set of vertices
 - Fast, efficient. $O(n^{1.25})$ execution