

Homework #6

***Frequency Responses and Z-Transforms***

Assigned on Saturday, October 20, 2018

Due on Friday, October 26, 2017, by 5:00 pm via Canvas submission

*Late homework is subject to a penalty of two points per minute late.*

**Reading:** McClellan, Schafer & Yoder, *Signal Processing First*, 2003, Chapters 6 and 7.  
 Companion Web site with demos and other supplemental information: <http://dspfirst.gatech.edu/>  
 Web site contains solutions to selected homework problems from *DSP First*.

The e-mail address for Mr. Houshang Salimian (TA) is [salimian.houshang@gmail.com](mailto:salimian.houshang@gmail.com).  
 Office hours for Mr. Salimian and Prof. Evans follow:

<i>Time Slot</i>	<i>Monday</i>	<i>Tuesday</i>	<i>Wednesday</i>	<i>Thursday</i>	<i>Friday</i>
<b>11:00 am</b>		<b>Salimian (EER 0.814 Table #4)</b>		<b>Salimian (EER 0.814A)</b>	<b>Salimian (EER 0.814D)</b>
<b>11:30 am</b>		<b>Salimian (EER 0.814 Table #4)</b>		<b>Salimian (EER 0.814A)</b>	<b>Salimian (EER 0.814D)</b>
<b>12:00 pm</b>		<b>Salimian (EER 0.814 Table #4)</b>		<b>Salimian (EER 0.814A)</b>	<b>Salimian (EER 0.814D)</b>
<b>12:30 pm</b>		Evans (EER 1.516)		Evans (EER 1.516)	<b>Salimian (EER 0.814D)</b>
<b>1:00 pm</b>		Evans (EER 1.516)		Evans (EER 1.516)	
<b>1:30 pm</b>		Evans (EER 1.516)		Evans (EER 1.516)	
<b>2:00 pm</b>		Evans (EER 6.882)	Evans (EER 6.882)	Evans (EER 6.882)	
<b>2:30 pm</b>		Evans (EER 6.882)	Evans (EER 6.882)	Evans (EER 6.882)	
<b>3:00 pm</b>		Evans (EER 6.882)	<b>Salimian (EER 1.810)</b>	Evans (EER 6.882)	
<b>3:30 pm</b>			<b>Salimian (EER 1.810)</b>		
<b>4:00 pm</b>			<b>Salimian (EER 1.810)</b>		
<b>4:30 pm</b>					

***Prof. Evans' coffee hours this week will be from 12:00-1:00pm on Friday in the EERC café.***

EE 313 tutoring is available on Sundays through Thursdays from 7:00pm to 10:00pm in EER 0.814:

<http://www.ece.utexas.edu/undergraduate/tutoring>

**1. Applying Discrete-Time Four-Point Averaging Filter to a Discrete-Time Signal. 30 points.**

*Signal Processing First*, problem P-6.14, page 160.

For part (b), please express the frequency response for the four-point averaging filter in terms of the Dirichlet function described in Section 6-7 on page 145.

For part (c), you should be able to see that the averaging filter is a lowpass filter with a “null” bandwidth of  $2\pi/N$  rad/sample, which is the distance from 0 rad/sample to the first null (zero) of the magnitude response at  $2\pi/N$  rad/sample.  $N-1$  frequencies will be zeroed out in the range  $(-\pi, \pi)$ .

**2. Applying Discrete-Time Four-Point Averaging Filter to a Continuous-Time Signal. 20 points.**

*Signal Processing First*, problem P-6.15, page 160.

**3. Transfer Functions in the  $z$  domain. 25 points.**

For each of the following linear time-invariant (LTI) systems, determine the impulse response, derive the transfer function, compute the poles and zeros, plot the poles and zeros using `zplane`:

- a) First-order unnormalized averaging filter (lowpass filter):  $y[n] = x[n] + x[n - 1]$  for  $n \geq 0$  and the initial condition  $x[-1] = 0$  to satisfy LTI properties.
- b) First-order difference filter (highpass filter):  $y[n] = x[n] - x[n - 1]$  for  $n \geq 0$  and the initial condition  $x[-1] = 0$  to satisfy LTI properties
- c) Second-order difference filter (highpass filter):  $y[n] = x[n] - 2x[n - 1] + x[n - 2]$  for  $n \geq 0$  and the initial condition  $x[-1] = 0$  and  $x[-2] = 0$  to satisfy LTI properties

**4. Using  $z$ -transforms to Compute Discrete-Time Convolution. 25 points.**

*Signal Processing First*, problem P-7.10, page 193.

As stated on the course descriptor, “Discussion of homework questions is encouraged. Please be sure to submit your own independent homework solution.”

NOTE: In your solutions, please put all work for problem 1 together, then all work for problem 2 together, etc. Please see additional homework guidelines on the homework page.

Please read the homework guidelines at

<http://users.ece.utexas.edu/~bevans/courses/signals/homework/index.html>