

Homework #6

***Frequency Responses and Z-Transforms***

Assigned on Thursday, October 14, 2021

Due on Friday, October 22, 2021, by 11:59 pm via Canvas submission

*Late homework is subject to a penalty of two points per minute late.*

**Reading:** McClellan, Schafer & Yoder, *Signal Processing First*, 2003, Chapters 6 and 7.  
 Companion Web site with demos and other supplemental information: <http://dspfirst.gatech.edu/>  
 Web site contains solutions to selected homework problems from *DSP First*.

Office hours for Mr. Tabbara and Prof. Evans follow:

<b><i>Time Slot</i></b>	<b><i>Monday</i></b>	<b><i>Tuesday</i></b>	<b><i>Wednesday</i></b>	<b><i>Thursday</i></b>	<b><i>Friday</i></b>
<b>9:30 am</b>				Evans (Zoom)	
<b>10:00 am</b>				Evans (Zoom)	
<b>10:30 am</b>					
<b>11:00 am</b>		Evans (EER 1.516)		Evans (EER 1.516)	
<b>11:30 am</b>		Evans (EER 1.516)		Evans (EER 1.516)	
<b>12:00 pm</b>		Evans (EER 1.516)		Evans (EER 1.516)	
<b>12:30 pm</b>		Evans (Zoom)			
<b>1:00 pm</b>		Evans (Zoom)			
<b>1:30 pm</b>					
<b>2:00 pm</b>					Evans (Zoom)
<b>2:30 pm</b>					Evans (Zoom)
<b>3:00 pm</b>					Tabbara (Zoom)
<b>3:30 pm</b>			Tabbara (Zoom)		Tabbara (Zoom)
<b>4:00 pm</b>			Tabbara (Zoom)		Tabbara (Zoom)
<b>4:30 pm</b>			Tabbara (Zoom)		

Prof. Evans holds coffee/advising hours on Fridays 12:00-2:00pm in the EERC café.

[EE 313 tutoring](#) is available 7-10pm on Sundays through Thursdays online.

### 1. Frequency and Step Responses. 36 points.

For each of the following linear time-invariant (LTI) systems, determine the impulse response, step response, and frequency response. Plot the magnitude and phase of the frequency response using `freqz`:

- First-order unnormalized averaging filter (lowpass filter):  $y[n] = x[n] + x[n - 1]$  for  $n \geq 0$  and the initial condition  $x[-1] = 0$  to satisfy LTI properties.
- First-order difference filter (highpass filter):  $y[n] = x[n] - x[n - 1]$  for  $n \geq 0$  and the initial condition  $x[-1] = 0$  to satisfy LTI properties
- Second-order difference filter (highpass filter):  $y[n] = x[n] - 2x[n - 1] + x[n - 2]$  for  $n \geq 0$  and the initial condition  $x[-1] = 0$  and  $x[-2] = 0$  to satisfy LTI properties

### 2. Cascade of Three Systems. 28 points.

*Signal Processing First*, problem P-6.13, page 159.

### 3. Transfer Functions in the $z$ domain. 36 points.

For each of the following linear time-invariant (LTI) systems, derive the transfer function, compute the poles and zeros, and plot the poles and zeros using `zplane`:

- First-order unnormalized averaging filter (lowpass filter):  $y[n] = x[n] + x[n - 1]$  for  $n \geq 0$  and the initial condition  $x[-1] = 0$  to satisfy LTI properties.
- First-order difference filter (highpass filter):  $y[n] = x[n] - x[n - 1]$  for  $n \geq 0$  and the initial condition  $x[-1] = 0$  to satisfy LTI properties
- Second-order difference filter (highpass filter):  $y[n] = x[n] - 2x[n - 1] + x[n - 2]$  for  $n \geq 0$  and the initial condition  $x[-1] = 0$  and  $x[-2] = 0$  to satisfy LTI properties

As stated on the course descriptor, "Discussion of homework questions is encouraged. Please be sure to submit your own independent homework solution."

NOTE: In your solutions, please put all work for problem 1 together, then all work for problem 2 together, etc. Please see additional homework guidelines on the homework page.

Please read the [homework guidelines](#).