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SUBJECTIVE AND OBJECTIVE QUALITY EVALUATION OF SYNTHETIC AND HIGH DYNAMIC RANGE IMAGES

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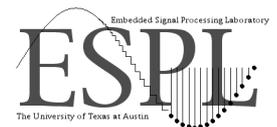
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Communications Group



Outline

- Introduction
- Image Quality Evaluation of Synthetic Scenes
- Image Quality Evaluation of High Dynamic Range Scenes
- Conclusion



Synthetic Scene



High Dynamic Range Scene

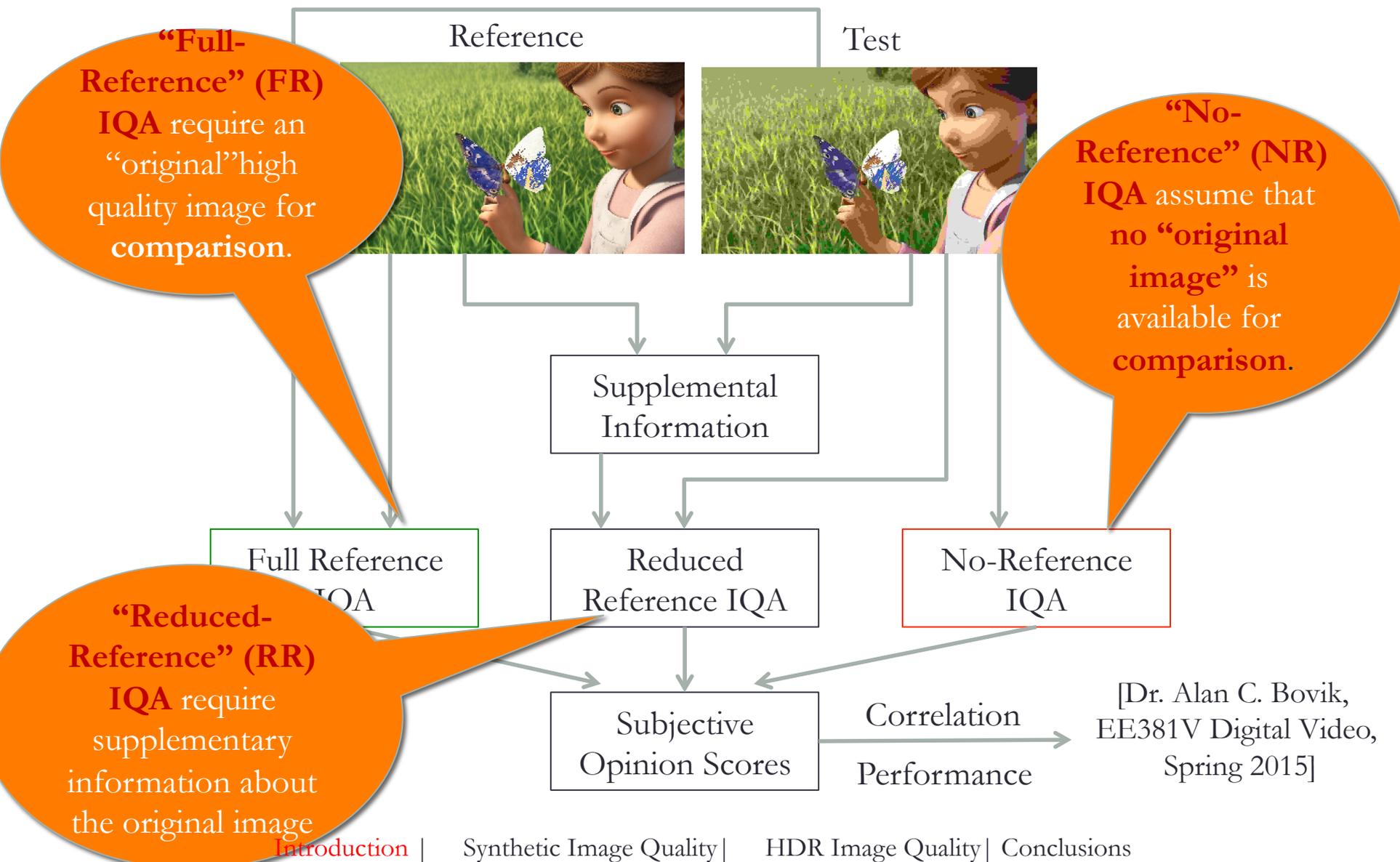
Motivation

- **Natural images captured by optical cameras**
 - 350M photos are uploaded to Facebook every day on average
- **Computer graphics generated content**
 - Massively multiplayer online gaming (23.4M subscribers worldwide)
 - Animated movies and synthetic still images
- **High Dynamic Range Images**
 - Capturing HDR images in recent cellphones (e.g. iPhones)
 - Displaying HDR videos for home (e.g. Samsung)
 - Streaming HDR content (e.g. Amazon Video, Netflix)
- **Image Quality Assessment very important**

Source: Statista.com



Image Quality Assessment (IQA) Algorithms



Thesis Statement and Contributions

Thesis Statement

Using scene statistics yields automatic visual quality assessment algorithms for synthetic images and high dynamic range images that have high correlation with human visual quality evaluation.

- Image Quality Evaluation of Synthetic Scenes
 1. Subjective Experiment
 2. Objective Quality Evaluation
- Image Quality Evaluation of High Dynamic Range Scenes
 3. Evaluation of Full-Reference Measures
 4. Crowdsourced Subjective Study
 5. Proposed No-reference Quality Measures

ESPL Synthetic Image Database [Kundu2015]

- 25 reference images + 500 distorted images
- 5 distortion categories, 4 levels of each distortion
- Single Stimulus Continuous Quality Scale (0-100) with hidden reference
- 52 observers: 12 among 64 subjects removed as outliers
- Annotated images with differential mean opinion scores (DMOS)
- Website: <http://signal.ece.utexas.edu/~bevans/synthetic/>

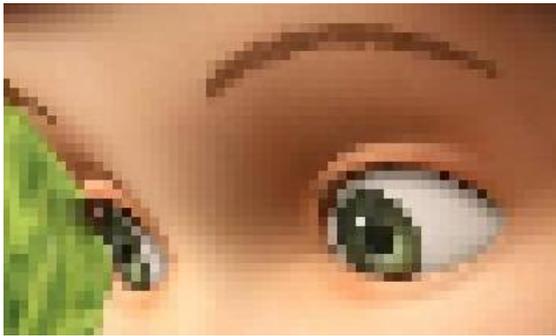


Reference (DMOS = 0)

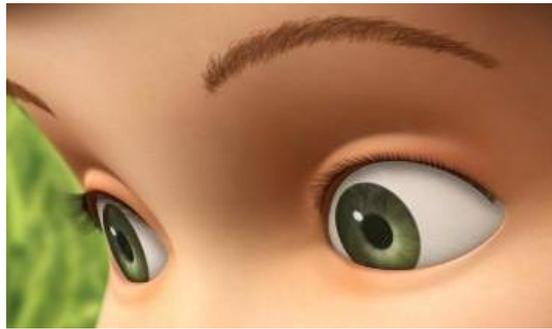


Distorted (DMOS = 74.68)

ESPL Database: Distortions



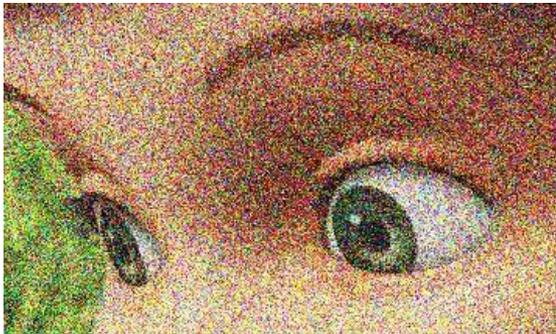
Interpolation
(DMOS = 63.23)



Original
(DMOS = 0)



JPEG Compression
(DMOS = 74.68)



Additive Noise
(DMOS = 60.33)



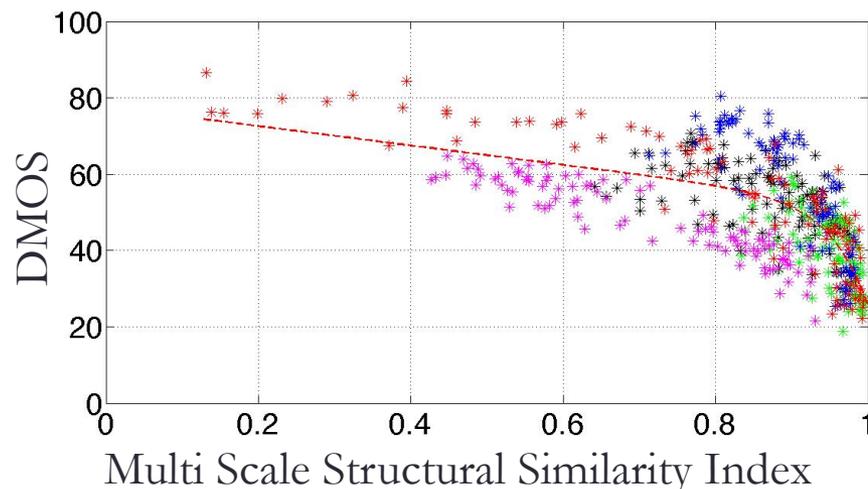
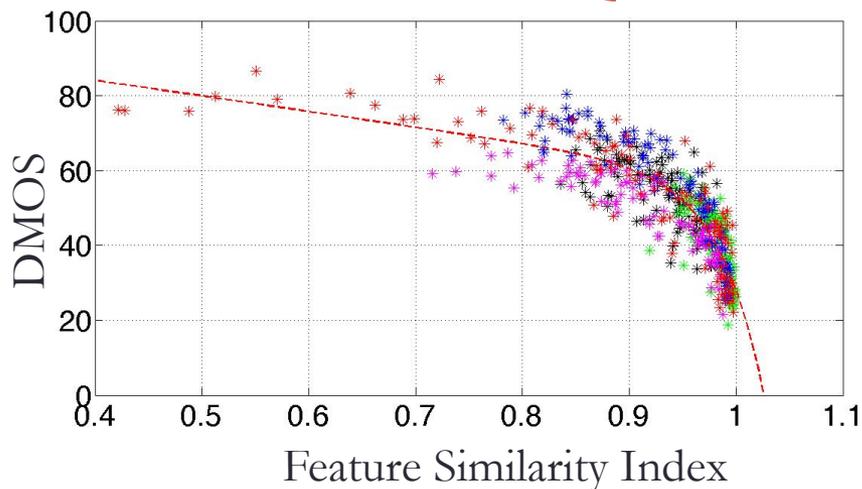
Blur
(DMOS = 50.89)



Fast Fading
(DMOS = 60.26)

Considered less severe distortions compared to what appears in natural images

ESPL Objective IQA: Correlation between DMOS and IQA scores



Scatter plot of two IQA algorithms vs. DMOS scores

- IQA algorithms evaluated for correlation with human scores
- Different correlation measures:
 - Spearman Rank Order Correlation Coefficient (SROCC)
 - Pearson Linear Correlation Coefficient (PLCC)
- Non-linear regression on objective IQA scores with logistic function

	Interp.
	Blur
	Noise
	JPEG
	Fading

ESPL Objective IQA: SROCC for Full-Reference IQAs

Algorithms	Inter- polation	Blur	Additive Noise	JPEG Blocking	Fast Fading	Overall
GMSD	0.727	0.827	0.923	0.918	0.922	0.892
SR-SIM	0.752	0.823	0.916	0.925	0.920	0.880
FSIM	0.692	0.801	0.902	0.940	0.907	0.876
MAD	0.788	0.813	0.909	0.933	0.927	0.863
SSIM-D	0.688	0.772	0.915	0.914	0.904	0.796
MS-SSIM	0.623	0.646	0.908	0.871	0.903	0.699
PSNR	0.565	0.481	0.864	0.695	0.846	0.590
SSIM	0.463	0.440	0.909	0.633	0.797	0.542

- GMSD: Gradient Magnitude Similarity Deviation [Xue2014]
- SR-SIM: Spectral Residual based Similarity Index [Zhang2012]
- FSIM: Feature Similarity Index [Zhang2011]
- MAD: Most Apparent Distortion Index [Larson2010]
- MS-SSIM: Multiscale-Structural Similarity Index [Wang2003]
- PSNR: Peak Signal-to-Noise Ratio [Wang2003]
- SSIM: Structural Similarity Index Metric [Wang2003]

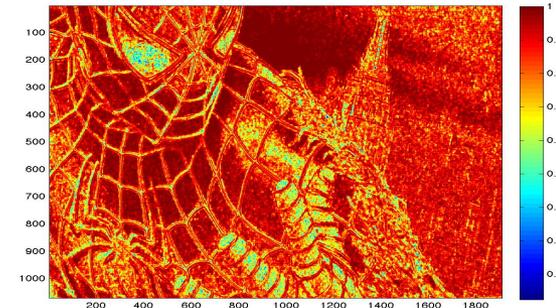
[No-reference](#)

ESPL Objective IQA: Some insights

- PSNR outperforms SSIM for all distortions
 - Need to choose appropriate scale for SSIM
 - Some users rated distorted image higher than reference
- Challenging distortions
 - Presence of [blur](#) may not always correspond to a lower subjective score
 - [Interpolation](#) caused near-threshold artifacts for low upsampling factors
- Efficient [pooling](#) strategies across image subblocks play important role

$\max(1, \text{round}(N/256))$
 $N = \text{Minimum image dimension}$

22 among 52 subjects rated the blurred version higher than the original one



Reference (DMOS = 0)

Blurred (5x5 Gaussian kernel, $\sigma = 1.25$ pixels)
(DMOS = 18.86)

SSIM map

ESPL Objective IQA: Synthetic Scene Statistics

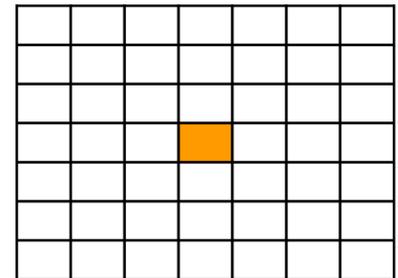
- Natural Scene statistics
 - Natural pristine images have statistics that occur irrespective of content
 - Statistics of images with [distortions](#) deviate from NSS
- Mean Subtracted Contrast Normalized ([MSCN](#)) pixels [Ruderman1993]

- Models divisive normalization in human visual systems
- Let $I(i, j)$ be the pixel located at (i, j) th spatial location

- MSCN, $\hat{I}(i, j) = \frac{I(i, j) - \mu(i, j)}{\sigma(i, j) + 1}$

- Mean $\mu(i, j) = \sum_{k=-K}^K \sum_{l=-L}^L w_{k,l} I(i+k, j+l)$

- Standard deviation $\sigma(i, j) = \sqrt{\sum_{k=-K}^K \sum_{l=-L}^L w_{k,l} [I(i+k, j+l) - \mu(i, j)]^2}$



7x7 window size
for local statistics

$W_{k,l}$: Gaussian
Weighting Factor

ESPL Objective IQA: SROCC for No-reference IQAs

Algorithms	Interpolation	Blur	Additive Noise	JPEG Blocking	Fast Fading	Correlation
G-IQA-1(L)	0.605	0.612	0.858	0.908	0.774	0.813
CORNIA	0.808	0.775	0.793	0.898	0.706	0.810
C-DIIVINE	0.702	0.730	0.847	0.841	0.738	0.798
BRISQUE	0.631	0.720	0.840	0.898	0.717	0.789
DESIQUE	0.595	0.590	0.886	0.934	0.714	0.773

- G-IQA-1(L): Gradient Image Quality Assessment-1 (Luminance) [Kundu2016]
- CORNIA: Codebook Rep for No-Ref Image Assessment (CORNIA) [Ye2012]
- C-DIIVINE: Complex Distortion Identification-based Image Verity and INtegrity Evaluation [Zhang2014]
- BRISQUE: Blind/Referenceless Image Spatial Quality Evaluator [Mittal2012]
- DESIQUE: DERivative Statistics-based Quality Evalulator [Zhang2013]

[Full-reference](#)



Full-reference Image Quality Evaluation of HDR Images

“It is a part of probability that many improbabilities will happen.”
— Aristotle

HDR creation pipeline

Tonemapping



Estimate
radiance map by
merging pixels
from different
exposures

Tonemap floating
point irradiance map to
SDR

Post-processing



Merge SDR exposure stack
directly to get fused image

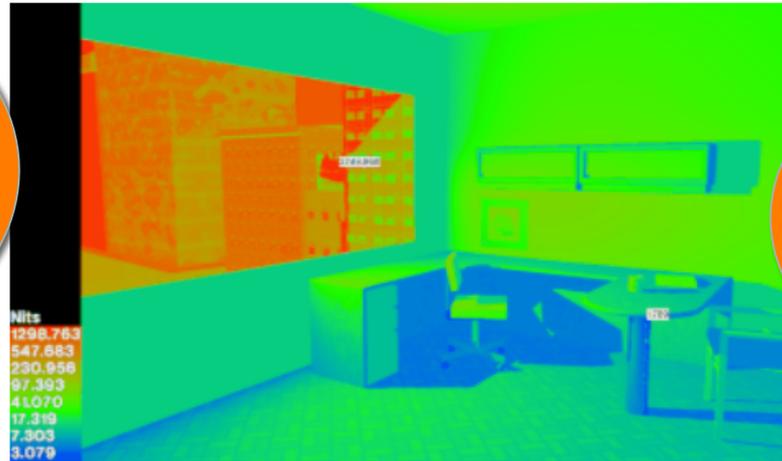
Post-processing

Multi-Exposure Fusion

Registered
exposure stack

HDR Tone-mapping operators [Larson, 1997]

Uniformly spaced quantization of luminances overexposes the view through the window



World luminance values for a window office in candelas per meter squared

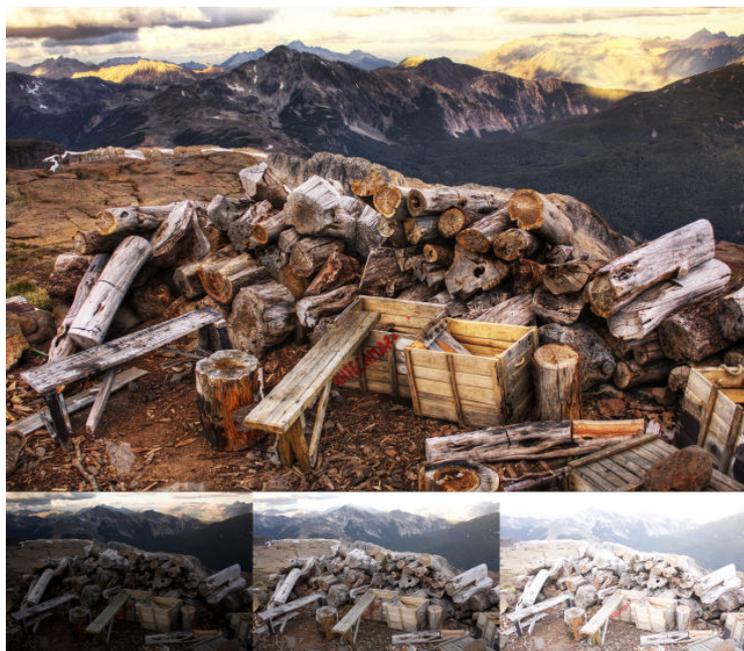
Luminances mapped to preserve visibility of both indoor & outdoor features using non-linear tone mapping



HDR IQA: Applications

Image quality assessment for HDR scenes for designing better

- **Tone-mapping operators** for standard dynamic range (SDR) displays
- [Multi-exposure fusion](#) algorithms
- **Compression** for HDR images (e.g., [JPEG-XR](#))
- **HDR rendering** for computer graphics



Multi-exposure fusion

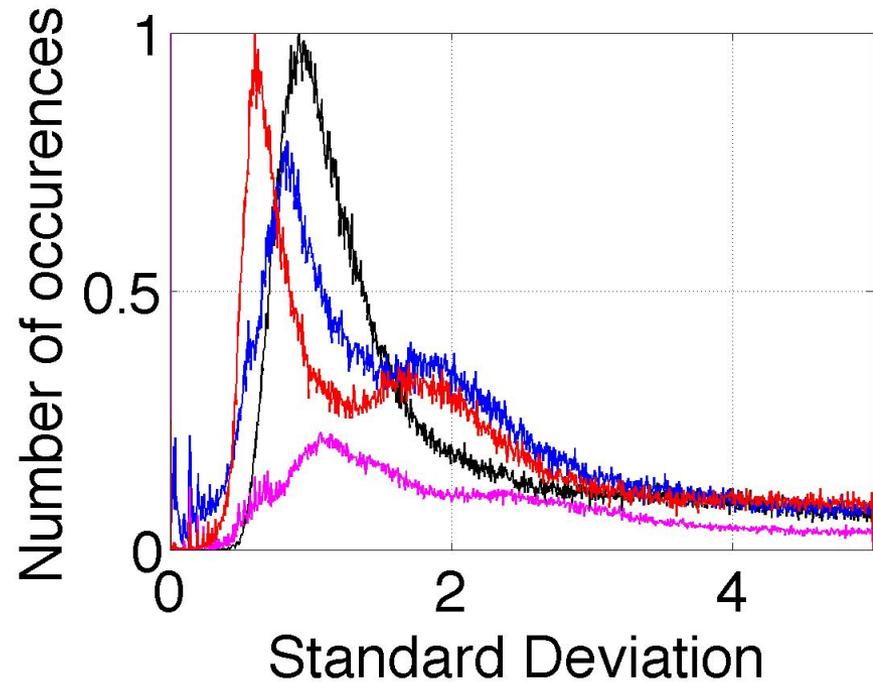
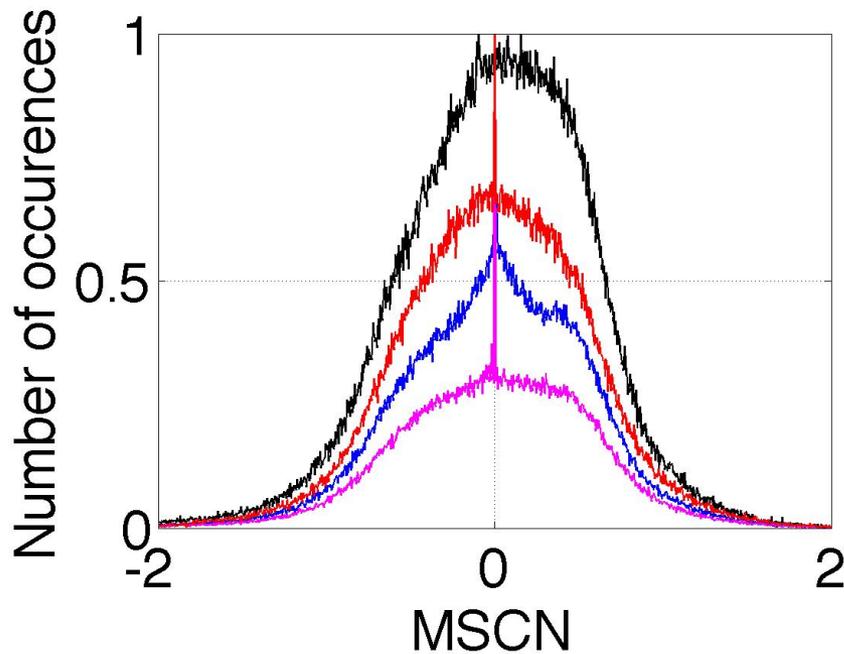


HDR rendering

Full-Reference IQA for Tonemapping

- Previous **FR-IQA** algorithms for tone mapping distortions
 - **Tone Mapped Quality Index (TMQI)**: inspired by SSIM [Yeganeh2013]
 - **Feature Similarity Index for Tone Mapped Images (FSITM)**: based on phase congruency [Nafchi2014]
- Image saliency by pooling IQA scores in each subblock
 - Attention based on Information Maximization based TMQI [Nasrinpour2015]
 - Itti and Koch's method generalized for HDR applications [Petit2010]
 - Simpler weighting measures needed for faster execution speed
- Finding better Natural Scene Statistics models to quantify “**naturalness**”
- Designing algorithms for other types of HDR distortions
 - Compression of HDR images

Spatial domain statistics for tonemapping



MSCN coefficient distribution and σ -field distribution for different tone-mapping operators

HDR IQA: MSCN based Scene Statistics

- Multiscale TMQI yield structural fidelity score (S)
- Proposed combination of structural fidelity and naturalness scores:

$$Q = aS^\gamma + \frac{1}{2}(1-a)\beta^{\delta_1} + \frac{1}{2}(1-a)\phi^{\delta_2}$$

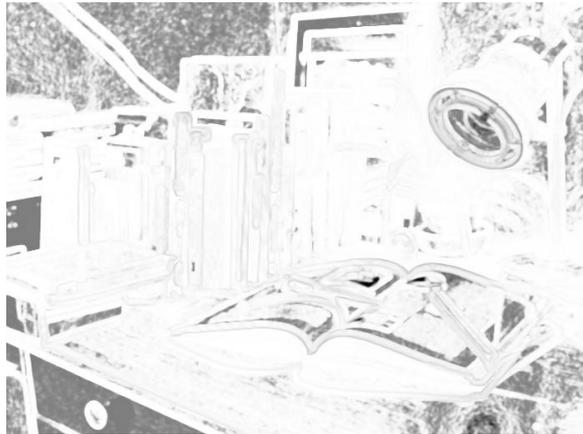
- β : **Scale parameter** of GGD fit of MSCN coefficients
- ϕ : **Standard deviation** of the σ -field
- $\gamma, \delta_1, \delta_2$ are the sensitivity parameters
- a indicates relative weighting of the terms

HDR IQA: Local pooling techniques

- Average pooling gives same importance to every pixel.
- Two non-uniform pooling strategies:
 - σ -map
 - Local entropy
- σ -map gives measure of **edge magnitude** and **high contrast** regions
- Local entropy indicates local randomness



Tone mapped image



Structural fidelity map



Structural fidelity with pooling

HDR IQA: TMQI Database Results [Yeganeh2013]

- 15 source HDR images
- Each HDR image mapped to SDR using 8 tone-mapping operators.
- Subjects ranked these 8 SDR images for every source image

FR-IQA Algorithms	SROCC	PLCC	Time(s)
TMQI-NSS-Sigma (Proposed)	0.8810	0.9439	0.3212
TMQI-NSS-Entropy (Proposed)	0.8810	0.9438	1.2759
TMQI-Itti (Proposed)	0.8810	0.9346	0.8010
FSITM-TMQI[Nafchi2014]	0.8571	0.9230	0.9428
STMQI[Nasrinpour2015]	0.8503	0.9382	1.538
TMQI-II[Ma2015]	0.8333	0.8790	0.2002
Feature Similarity Index for Tone-Mapped Images(FSITM) [Nafchi2014]	0.8333	0.8948	0.4741
Tone Mapped Image Quality Index (TMQI)[Yeganeh2013]	0.8095	0.9082	0.5206

Correlation measures are computed between predicted ranks of tone-mapped images and ground-truth rankings for each source image. Result shows median of correlations computed.



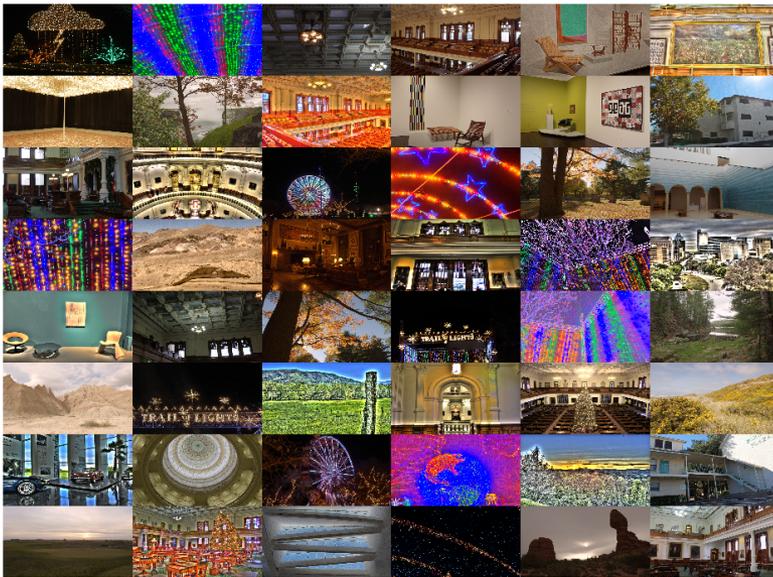
Crowdsourced Study of High Dynamic Range Images

“The desert has its holiness of silence, the crowd its holiness of conversation.”
— Walter Elliot

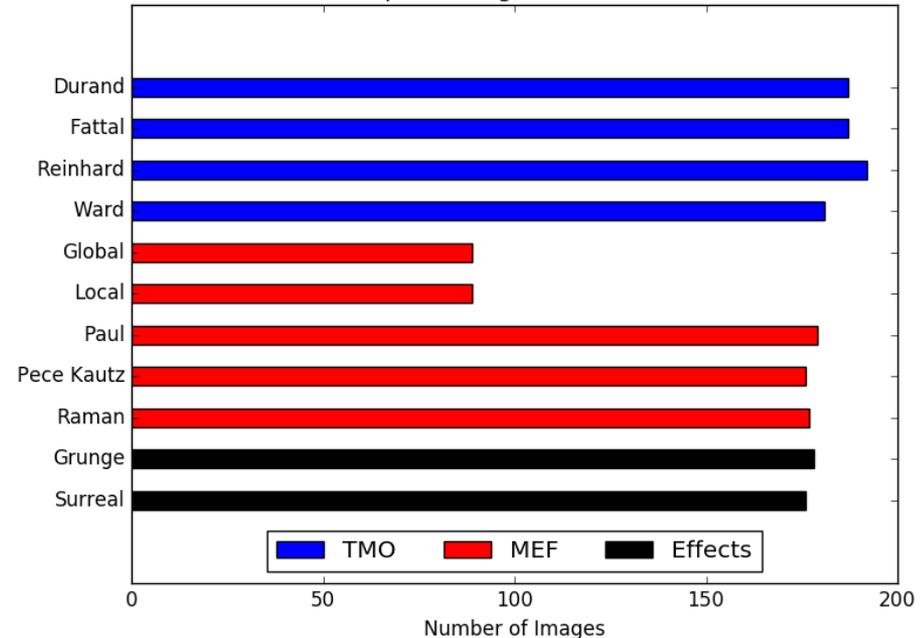
HDR-IQA: ESPL-LIVE Image Database

- 1,811 HDR images obtained from 605 source scenes
- Size: 960x540 for landscape and 540x304 for portrait orientation
- Single Stimulus Continuous Quality Scale (0-100)
- 327,720 raw quality scores from 5,462 subjects
- Images annotated with mean opinion scores (MOS)

Sample images



Distribution of HDR processing methods used in the database



HDR-IQA: Subjective Testing Methodology

- 12 subjects evaluated 27 images in laboratory setting
 - 5 ‘Gold Standard’ images
- Amazon Mechanical Turk used for crowdsourcing
 - Training images: 11
 - Test images: 49
 - ‘Gold Standard’ images: 5 (Viewed by every subject)
 - Randomly repeated images : 5
- At the end subjects answered questions on demographics, display parameters, and familiarity with HDR imaging



Source: Amazon.com

HDR-IQA: Processing of the raw scores

- **Subject rejection strategies:**
 - Only subjects with AMT confidence values greater than 0.75 participated
 - If scores assigned to multiple copies of the same image differed by more than 25.5 for three images, scores from that user was rejected
 - 388 subjects among 5,462 removed as outliers
- **Processing of remaining scores:**
 - On an average, every image evaluated by 110 subjects
 - Mean Opinion Scores: Mean of [Z-score](#) for every image
 - [Spans](#) 16.941 - 68.502.
 - Raw MOS scores span 5.623 – 84.661
- **Consistency with laboratory setting:**
 - Median PLCC between individual scores and MOS values for ‘Gold Standard’ images in laboratory setting was **0.9466**

[Details](#)



No-reference Image Quality Assessment Algorithm for High Dynamic Range images

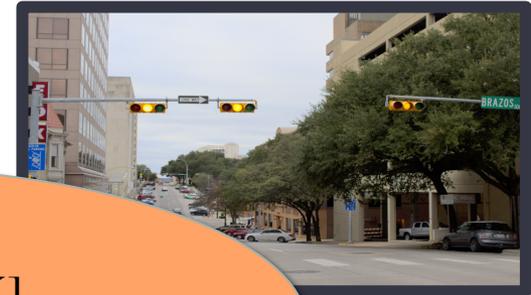
“An algorithm must be seen to be believed.”

— Donald Knuth

HDR IQA: MSCN and local σ -map distributions



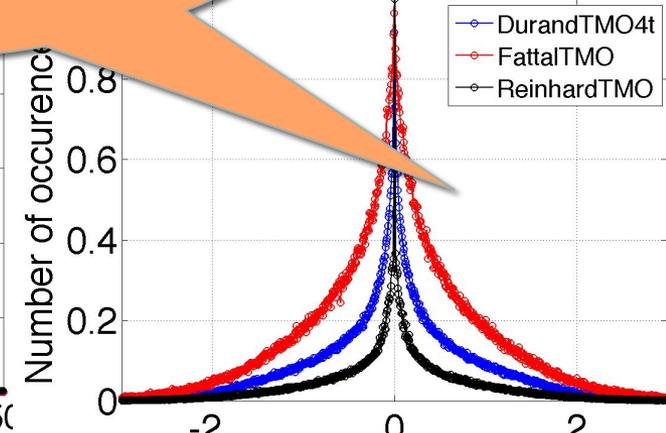
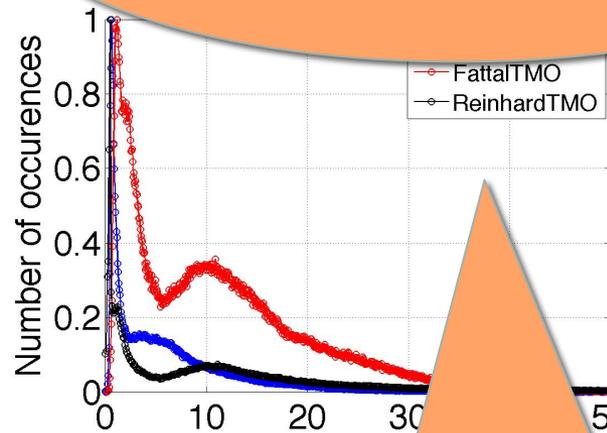
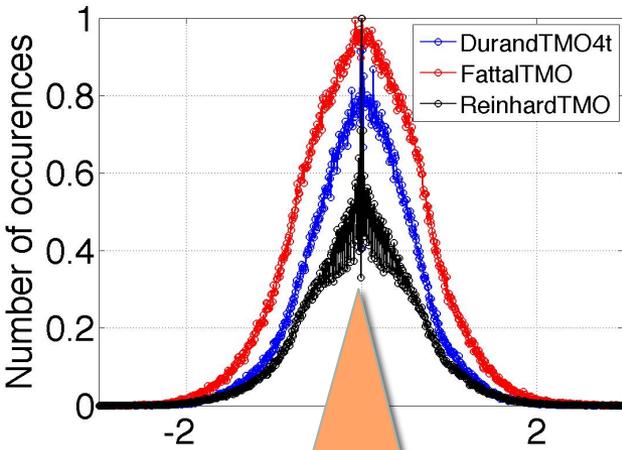
(a) MOS = 40.47



52.80

$$J(i, j) = \log[\hat{I}(i, j) + K]$$

$$\nabla_x J(i, j) = J(i, j+1) - J(i, j)$$

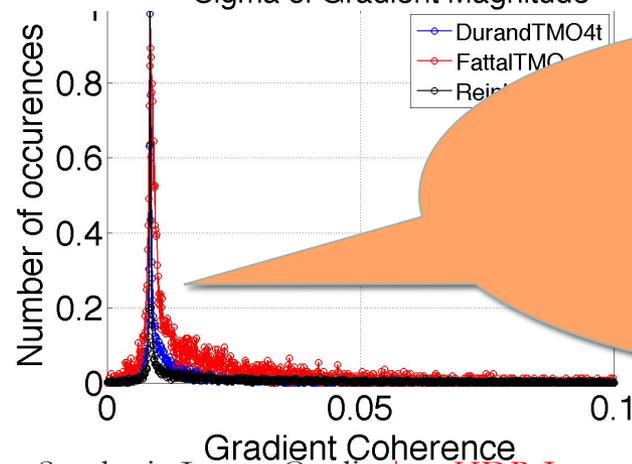
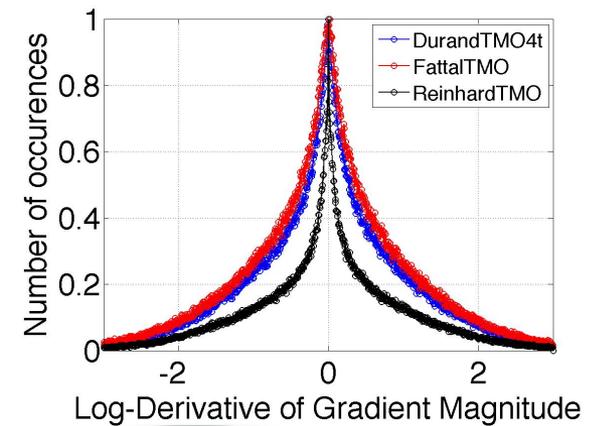
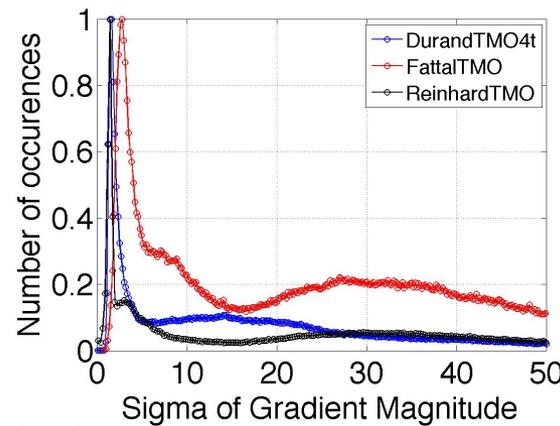
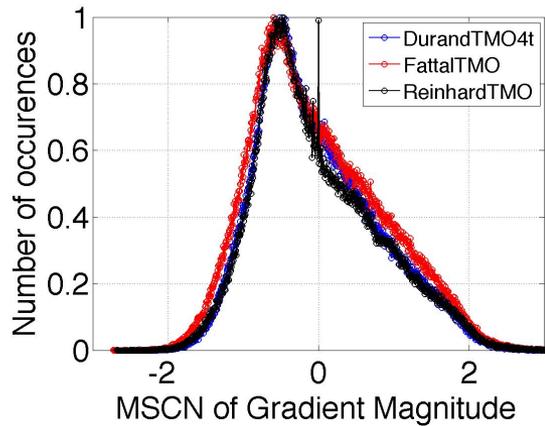


$$\hat{I}(i, j) = \frac{I(i, j) - \mu(i, j)}{\sigma(i, j) + 1}$$

$$\sigma(i, j) = \sqrt{\sum_{k=-K}^K \sum_{l=-L}^L w_{k,l} [I(i+k, j+l) - \mu(i, j)]^2}$$

Synthe

HDR IQA: Distribution of gradient domain features



$$J = \begin{bmatrix} f(G_x) & f(G_x G_y) \\ f(G_x G_y) & f(G_y) \end{bmatrix}$$

$$C = \left(\frac{\lambda_1 - \lambda_2}{\lambda_1 + \lambda_2} \right)^2$$

HDR IQA: SROCC between each feature and MOS

Domain	Feature Description	SROCC
Spatial [f1 – f2]	Shape and Scale parameters of <u>AGGD</u> fitted to MSCN coefficients	0.238
Spatial [f3 – f16]	Shape and Scale parameters of AGGD fitted to <u>log-derivative</u> of the seven types of neighbors	0.439
Spatial [f17 – f18]	Mean and standard deviation based features extracted from the σ -field	0.369
Gradient [f19 – f20]	Shape and Scale parameters of the AGGD fitted to the MSCN coefficients of gradient magnitude field	0.250
Gradient [f21 – f34]	Shape and Scale parameters of AGGD fitted to log-derivative of seven types of neighbors of gradient magnitude field	0.386
Gradient [f35 – f36]	Mean and standard deviation based features extracted from the σ -field of gradient magnitude field	0.388
Gradient [f37 – f40]	Mean, standard deviation, skewness, and kurtosis of <u>gradient structure tensor coherence</u>	0.420

G-IQA-1: [f1 – f36]

G-IQA-2: [f1 – f18, f37 f40]

Features computed across 2 levels and in LAB color space

ESPL-LIVE HDR objective IQA: No-reference SROCC

- Computed on ratings obtained from 4,715 subjects
- 80% training, 20% testing, 100 random train-test splits
- No content overlap to prevent artificial inflation of correlations

[More](#)

Algorithms	Tone Mapping	Multi Exposure Fusion	Post Processed	<u>Overall</u>
G-IQA-1	0.692	0.691	0.582	0.716
G-IQA-2	0.720	0.698	0.484	0.709
G-IQA-1 (L)	0.651	0.623	0.489	0.662
G-IQA-2 (L)	0.661	0.631	0.419	0.656
DESIQUE	0.503	0.550	0.476	0.565
GM-LOG	0.521	0.521	0.527	0.562
CurveletIQA	0.542	0.512	0.435	0.546
DIIVINE	0.485	0.456	0.335	0.480
BLIINDS-II	0.385	0.421	0.435	0.448
BRISQUE	0.267	0.431	0.431	0.402

Conclusion

Thesis Statement

Using scene statistics yields automatic visual quality assessment algorithms for synthetic images and high dynamic range images that have high correlation with human visual quality evaluation.

- Image Quality Evaluation of Synthetic Scenes
 1. Designed ESPL Synthetic Image Database
 2. Compared performance of state-of-the-art IQA algorithms for synthetic images
- Image Quality Evaluation of High Dynamic Range Scenes
 3. Used scene statistics and visual saliency measures for full-reference evaluation of HDR scenes
 4. Conducted a large scale subjective study for HDR images
 5. Proposed scene-statistics based NR-IQA algorithms for HDR images

Relevant Publications

- D. Kundu and B. L. Evans, “Spatial Domain Synthetic Scene Statistics”, *Proc. Asilomar Conf. on Signals, Systems, and Computers*, Nov. 2-5, 2014, Pacific Grove, CA USA.
- D. Kundu and B. L. Evans, “Full-reference visual quality assessment for synthetic images: A subjective study”, in *Proc. IEEE Int. Conf. on Image Processing*, September 2015. **Won Top 10% Paper Award.**
- D. Kundu and B. L. Evans, “No-reference synthetic image quality assessment using scene statistics,” in *Proc. Asilomar Conf. Signals, Systems and Computers.*, November 2015.
- D. Kundu, L. K. Choi, A. C. Bovik and B. L. Evans, “Subjective and Objective Quality Evaluation of Lightly Distorted Synthetic Images”, *IEEE Transactions on Image Processing*, to be submitted.
- D. Kundu and B. L. Evans, “Visual Attention Guided Quality Assessment of Tone-Mapped Images using Scene Statistics”, submitted to *IEEE Int. Conf. on Image Processing*, September 2016.

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Backup

IQA in Synthetic Scenes

- Frame rendering in video games
 - Better real-time algorithms for photo-realistic images on powerful GPUs
 - More realistic lighting calculations
- Cloud gaming (e.g. Nvidia Grid servers)
- Livestreaming game play (e.g. YouTube Gaming)



ESPL Database: Source Images

- 25 color images, 1920x1080 pixels in size
- Frames from video games
 - Multiplayer role playing games (such as War of Warcraft)
 - First person shooter games (such as Counter Strike)
 - Motorcycle and car racing games
- Frame from animated movies
 - The Lion King, Tinkerbell series, Avatar etc.



ESPL Database: Source Content Parameters

- **Spatial information** (SI) indicates edge energy.

$$s_r = \sqrt{s_v^2 + s_h^2}$$

- S_h and S_v : gray-scale images filtered with horizontal and vertical Sobel kernels respectively

$$SI = \sqrt{L / 1080} \sqrt{\sum s_r^2 / P}$$

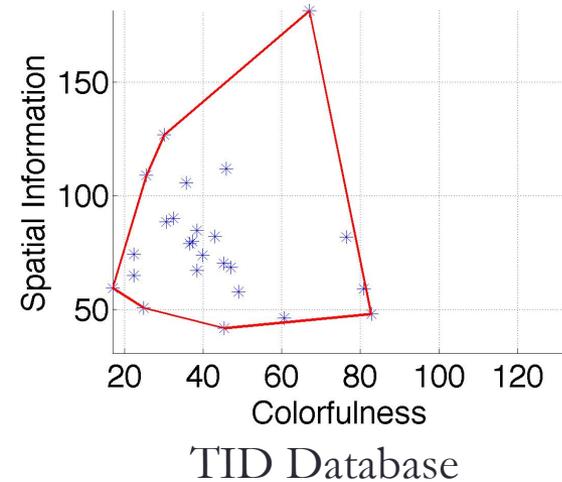
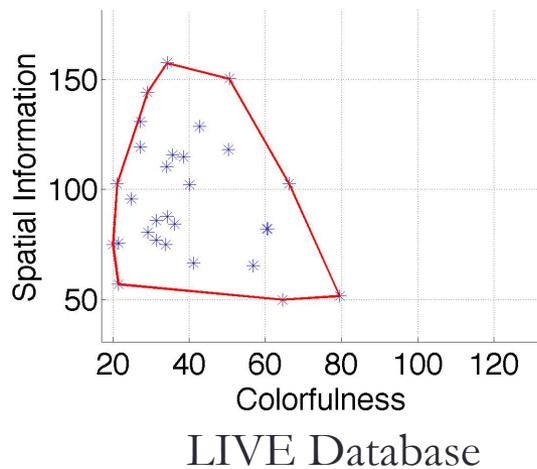
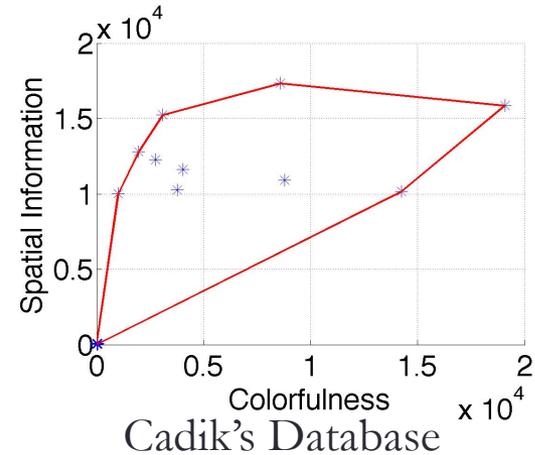
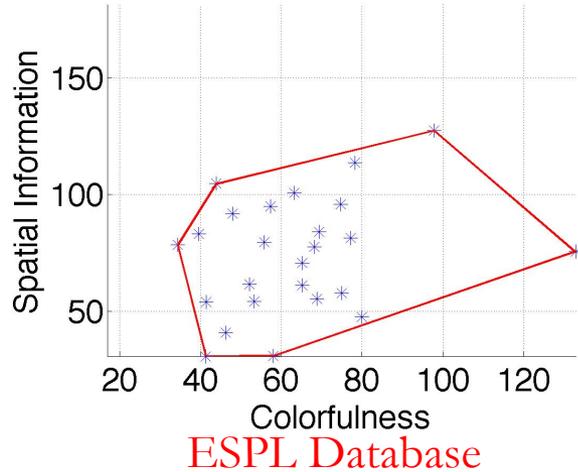
- P: Number of pixels in the filtered image
- L: Vertical resolution
- **Colorfulness** (CF) indicates variety and intensity of colors

$$CF = \sqrt{\sigma_{rg}^2 + \sigma_{by}^2} + 0.3 \sqrt{\mu_{rg}^2 + \mu_{by}^2}$$

- Using opponent color spaces: $rg = R - G$ and $yb = 0.5(R + G) - B$

ESPL Database: Source Complexity [Winkler2012]

- **Spatial Information:** Indicates edge energy
- **Colorfulness:** Indicates the variety and intensity of colors



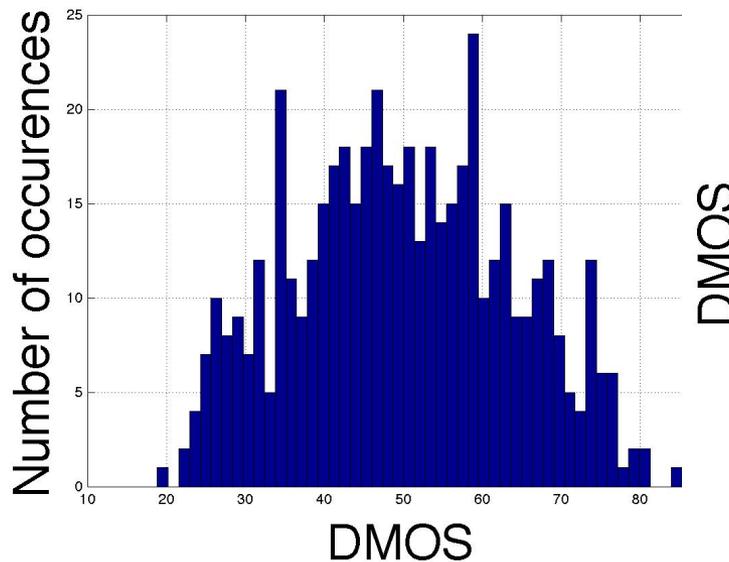
[Details](#)

ESPL Database: Processing of raw scores

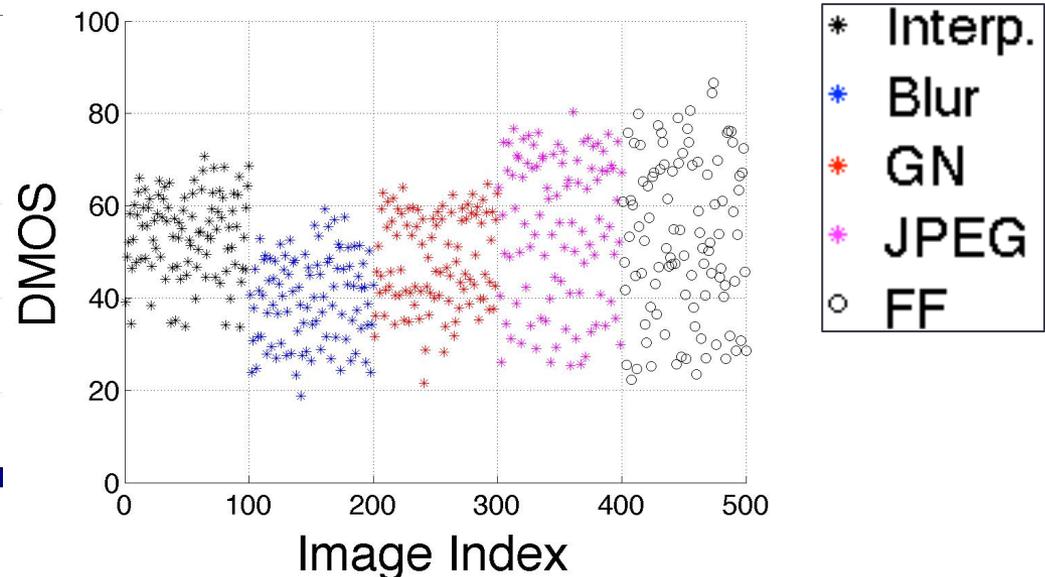
- Raw scores were first converted to raw quality difference scores:

$$d_{ij} = r_{iref(j)} - r_{ij}$$

- r_{ij} : Score assigned to j -th image by the i -th subject
- $r_{iref(j)}$: Score assigned by same subject to corresponding reference
- Difference scores normalized for each subject and averaged



Histogram of DMOS scores



Scatter plot of DMOS scores

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ESPL Database: Distortion Parameters

- Interpolation
 - Images downsampled by factors ranging from 3 to 6
 - Upsampled back using nearest neighbor interpolation
- Blur
 - RGB color channels filtered with circularly symmetric 2D Gaussian kernel
 - Standard deviation ranging from 1.25 to 3.5 pixels
 - Same kernel employed for each color channels
- Additive Noise:
 - Same noise variance used for all color channels
 - Noise standard deviation ranged from 0.071 to 0.316 pixels

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ESPL Database: Distortion Parameters (cont'd)

- JPEG compression
 - MATLAB `imwrite` function was used
 - Bits per-pixel (bpp) ranged from 0.0445 to 0.1843.
 - Higher bpp images were not considered to better simulate playing a cloud video game under restricted bandwidth conditions.
- Simulated Fast Fading Channel
 - Original images compressed into JPEG2000 bitstreams
 - Wireless error resilience features enabled and 64 x 64 tiles
 - Transmitted over a simulated Rayleigh-fading channel
 - Signal-to-noise ratio (SNR) was varied at the receiver from 14 to 17 dB [Back](#)
 - SNRs greater than 17 dB did not introduce perceptible distortions due to the error resilience feature of the JPEG2000 codec.

ESPL Database: Methodology

- Single Stimulus Continuous Quality Scale (**SSCQS**) method
- Each subject evaluated each image
- **Three sessions**, of one hour each, separated by at least 24 hours.
 - Each session divided into two sub-sessions of 25 minutes
 - Separated by a break of five minutes.
- **64** subjects
 - Age range : **18 – 30 years**
 - Mostly **without prior experience** in participation of subjective tests
- Verbal confirmation of 20/20 (corrected) vision was obtained
- Viewed roughly **175 test images** during each session
 - Randomly ordered using a random number generator
- Testing sessions were preceded by **training** session of **10 images**

ESPL Database : Methodology (cont'd)

- User interface programmed on MATLAB using Psychology Toolbox
- NVIDIA Quadro NVS 285
- Dell 24 inches U2412M display
- 16:10 aspect ratio
- Normal office illumination
 - 540 lux measured with HS1010 digital light meter
- Each image displayed for 12 seconds
- Viewing distance: 2-2.25 times display height
- Scores between 0-100 was entered

ESPL Database: Processing of raw scores

- Raw scores were first converted to raw quality difference scores:

$$d_{ijk} = r_{iref(j)k} - r_{ijk}$$

- r_{ijk} : Score assigned to j -th image by the i -th subject in k -th session
 - $r_{iref(j)k}$: Score assigned by same subject to corresponding reference
- DMOS score is zero for reference images
- DMOS scores converted to Z-scores per session

$$\mu_{ik} = \frac{1}{N_{ik}} \sum_{j=1}^{N_{ik}} d_{ijk}$$

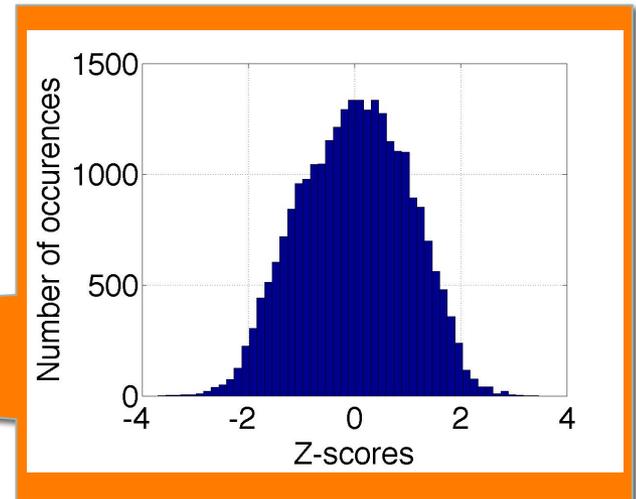
$$z'_{ij} = \frac{100(z_{ij} + 3)}{6}$$

$$\sigma_{ik} = \sqrt{\frac{1}{N_{ik} - 1} \sum_{j=1}^{N_{ik}} (d_{ijk} - \mu_{ik})^2}$$

$$DMOS_j = \frac{1}{M} \sum_{i=1}^M z'_{ij}$$

$$z_{ijk} = \frac{d_{ijk} - \mu_{ik}}{\sigma_{ik}}$$

N_{ik} : Number of videos seen by i -th subject in k -th session



ESPL Database: Outlier rejection

- Done as per ITU-R BT 500.11 recommendation
- Compute kurtosis of scores per subject to check Gaussianity
- If kurtosis falls between the values of 2 and 4 (Gaussian)
 - Subject rejected if more than 5% of his scores falls outside $\pm 2\sigma$ from mean.
- For non Gaussian distributions
 - Subject rejected if more than 5% of his scores falls outside $\pm 4.47\sigma$ from mean.
- 12 out of 64 subjects rejected
- Testing degree of consensus among subjects:
 - Subjects divided into two groups randomly
 - DMOS scores for all the image calculated individually from each group
 - Pearson's linear correlation coefficient was 0.9813 between the groups
 - Shows a high level of consensus among the subjects

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ESPL Database: Calculating correlations

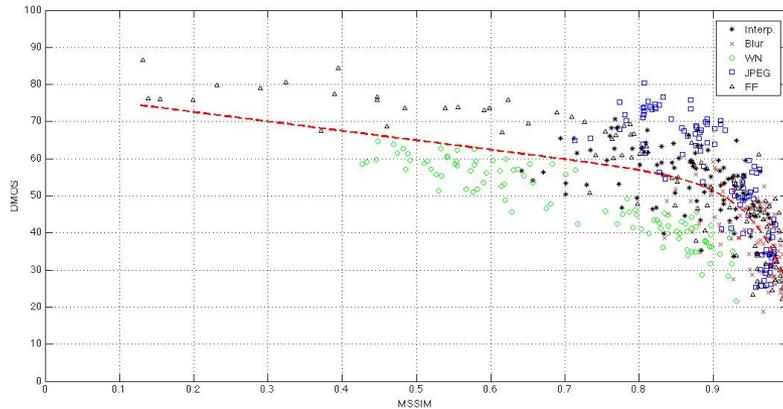
- Let Q_j be the quality predicted by the IQA algorithm for the j-th image.
- Four parameter monotonic logistic function fit IQA predictions to quality scores:

$$Q'_j = \beta_2 + \frac{\beta_1 - \beta_2}{1 + \exp\left[-\frac{Q_j - \beta_3}{|\beta_4|}\right]}$$

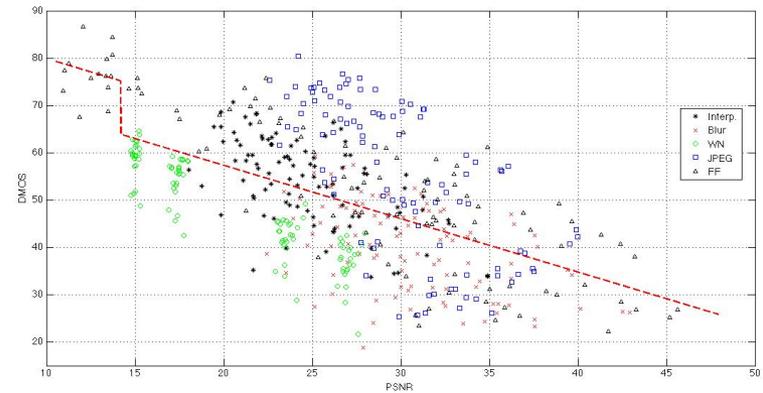
- Spearman's Rank-order correlation coefficient: $SRCC = 1 - \frac{6 \sum_{i=1}^N d_i^2}{N(N^2 - 1)}$
- where d_i is the difference between the i-th image's ranks is subjective and objective evaluations.
- Kendall's correlation coefficient: $KCC = \frac{N_c - N_d}{0.5N(N - 1)}$
- N_c and N_d are the number of concordant (of consistent rank order) and discordant (of inconsistent rank order) pairs in the data set respectively.

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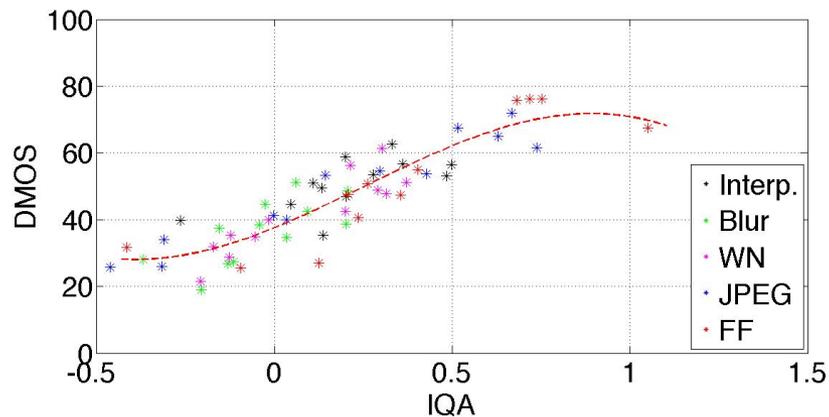
ESPL IQA: Scatter plot of DMOS vs IQA scores



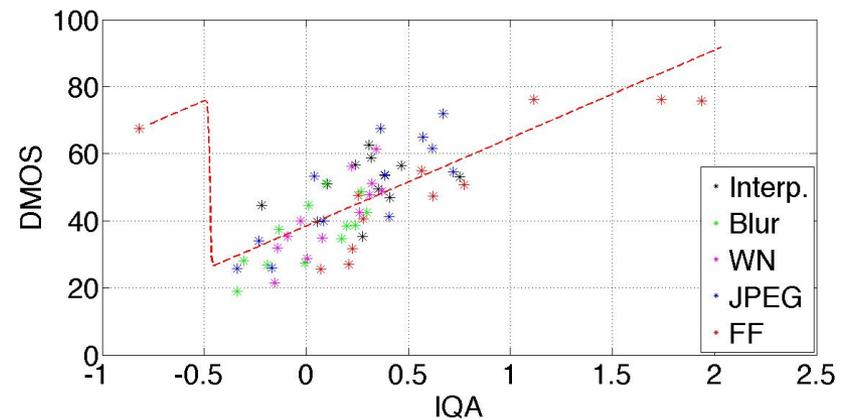
MSSIM



PSNR



G-IQA-1



BRISQUE

ESPL Objective IQA: Blur

- Blurred images led to a lower degree of correlation with human scores
- Lower degree of blur considered than natural images
- Some motion blur lead to aesthetically pleasing images [McGuire2012]
- Presence of blur may not always correspond to a lower subjective score

22 among 52 subjects rated the blurred version higher than the original one



Reference (DMOS = 0)



Blurred (5x5 Gaussian kernel. $\sigma = 1.25$ pixels)
(DMOS = 18.86)

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ESPL Objective IQA: Interpolation

- Lowest degree of correlation with human scores among all distortions
- Most Apparent Distortion measure achieves highest correlation
- It advocates multiple strategies for determining overall image quality
 - Based on whether the distortions are near-threshold or supra-threshold
- Low downsampling factors result in near-threshold artifacts
 - Almost imperceptible at normal viewing distances
- Higher downsampling factors result in supra-threshold artifacts



Reference (DMOS = 0)



Interpolated (DMOS = 56.40)

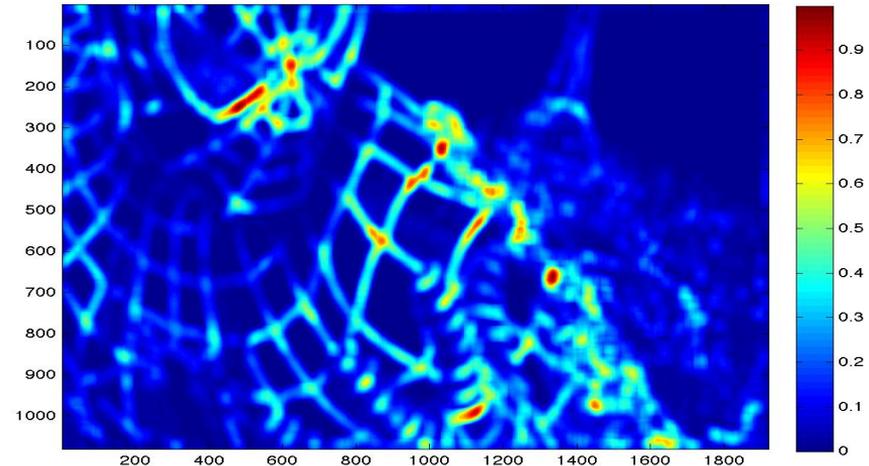
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ESPL Objective IQA: Role of Pooling

- Efficient pooling strategies play an important role
- Visual Saliency Index, Spectral Residual based Similarity Measure
 - Use visual fixations based pooling strategies
- Gradient Magnitude Similarity Index
 - Use standard deviation of gradient map
- Using visual fixations in synthetic scenes is promising direction



Reference



Spectral Residual Saliency

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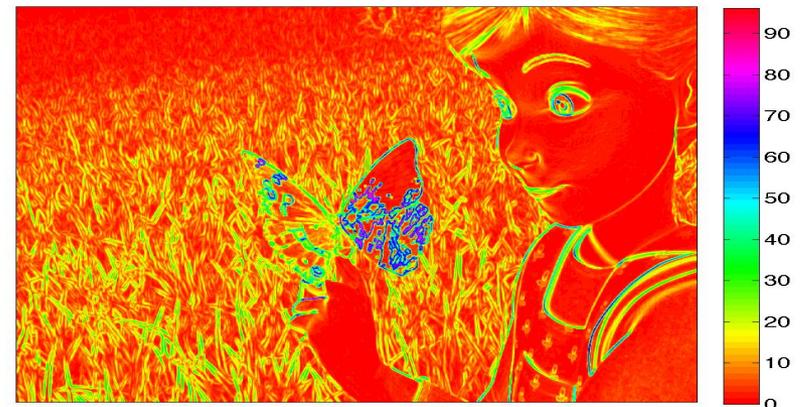
ESPL Objective IQA: MSCN Images



Original Image



MSCN Image



Standard Deviation Image

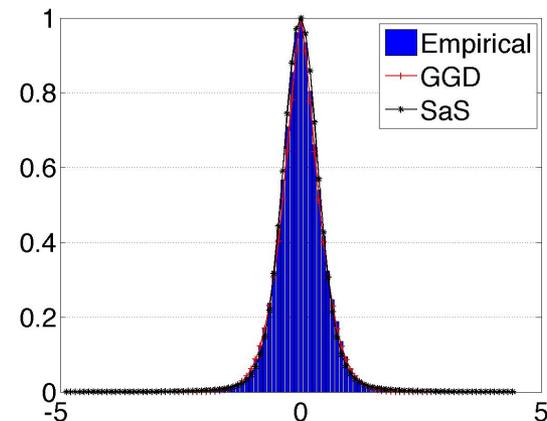
ESPL Objective IQA : Modeling MSCN Pixels

- MSCN coefficients modeled by the following distributions:
 - Generalized Gaussian ([GGD](#))
 - Symmetric Alpha Stable ([SaS](#)): For highly kurtotic empirical histograms

Mean square error, J-Divergence, and Pearson's Chi-squared values for distributions fitted to histograms of MSCN coefficients, averaged over 221 pristine synthetic images [Kundu 2014]

Chi-Squared value at 99% confidence interval = 6.635

	MSE	J	Chi Square
GGD	0.00257	0.0772	0.00252
SAS	0.00264	0.0948	0.00174



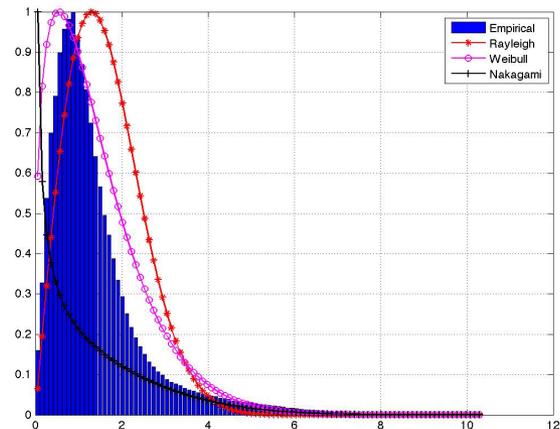
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ESPL IQA: Modeling of MSCN Gradients

- Distribution of the gradient magnitude of MSCN coefficients
 - Modeled using Rayleigh, Weibull and Nakagami distributions

Mean square error, J-Divergence, and Pearson's Chi-squared values for distributions fitted to histograms of MSCN coefficients, averaged over 221 pristine synthetic images [Kundu 2014]

	MSE	J	Chi Square
Rayleigh	0.00891	4.730	0.769
Weibull	0.0251	5.00432	0.663
Nakagami	0.00916	5.304	0.892



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Generalized Gaussian Density

- The **GGD** $p_g(r) = \frac{\beta}{2\sigma\Gamma(\beta^{-1})} \exp\left(\left(|r|/\sigma\right)^\beta\right)$ $r \in \mathfrak{R}, \sigma, \beta > 0$

includes the **special cases**

$\beta = 1$ (**laplacian** density)

$\beta = 2$ (**gaussian** density)

$\beta = \infty$ (**uniform** density)

- Many authors have observed the **GGD behavior** of **BP image** signals.
 - Wavelet coefficients
 - DCT coefficients
 - Usually** reported that $b \gg 1$ but **varies** ($0.8 < b < 1.4$).

[Ref: Dr. Alan C. Bovik,
EE381V Digital Video,
Spring 2015]

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[Back to FR-HDR](#)

[Back to NR](#)

Symmetric Alpha Stable

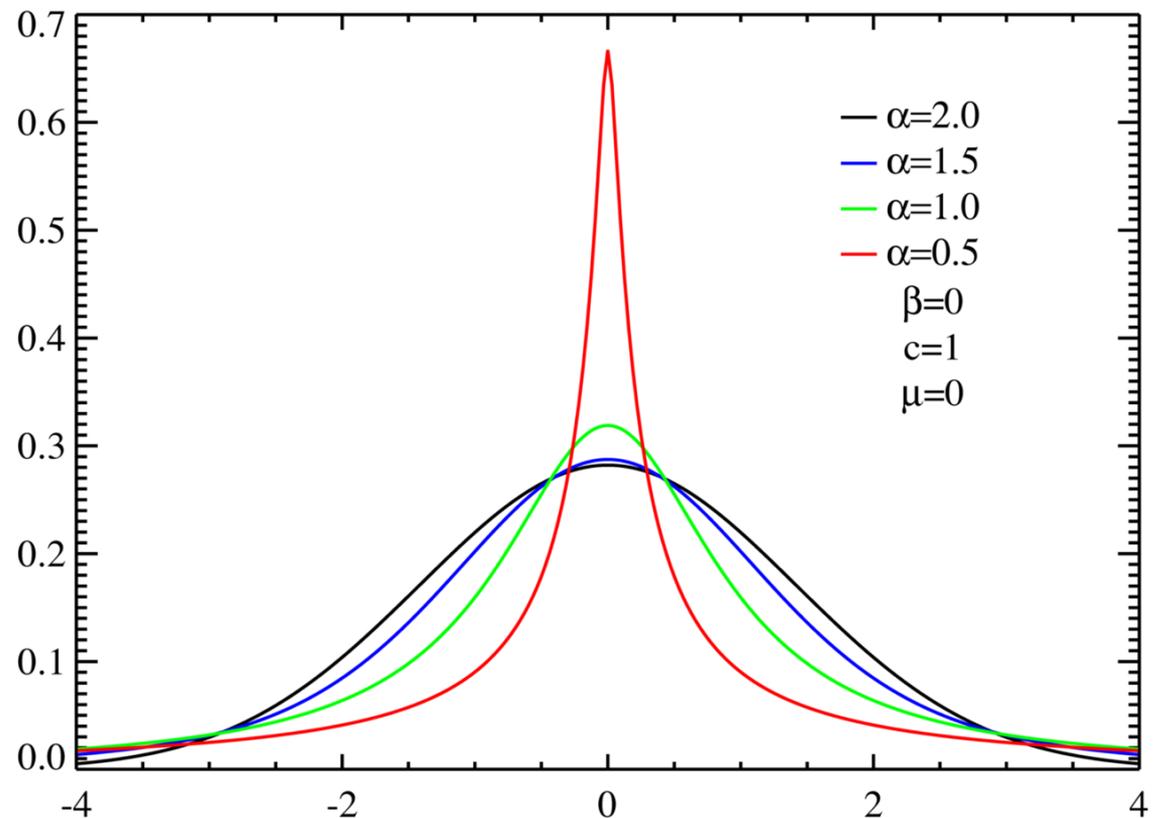
- A random variable X is called stable if its characteristic function can be expressed as:

$$\varphi(t; \alpha, \beta, c, \mu) = \exp [it\mu - |ct|^\alpha (1 - i\beta \operatorname{sgn}(t)\Phi)]$$

- $\operatorname{sgn}(t)$: sign of t

$$\Phi = \tan(\pi\alpha/2)$$

-



Steerable Filter

- Create **directional derivative** of **gaussian** in **arbitrary direction** by a **coordinate rotation** by \mathbf{q} :

$$h_{\theta}(\mathbf{x}) = \frac{-1}{2\pi\sigma^4} [(\cos \theta)x + (\sin \theta)y] \exp \left[\frac{-(x^2 + y^2)}{2\sigma^2} \right]$$

$$\mathfrak{F} \quad j \cdot [(\cos \theta)U + (\sin \theta)V] \cdot \exp \left[-2(\pi\sigma)^2 (U^2 + V^2) \right]$$

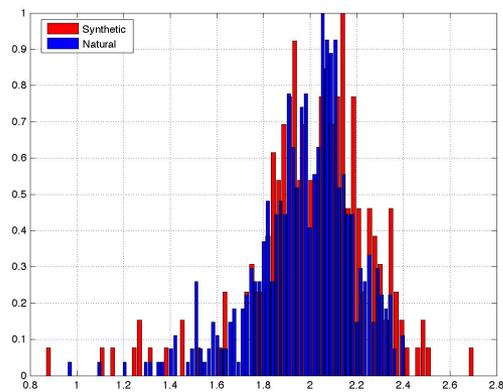
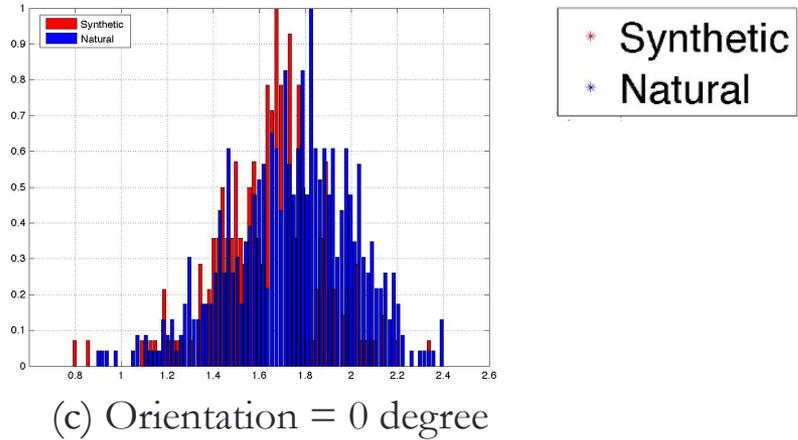
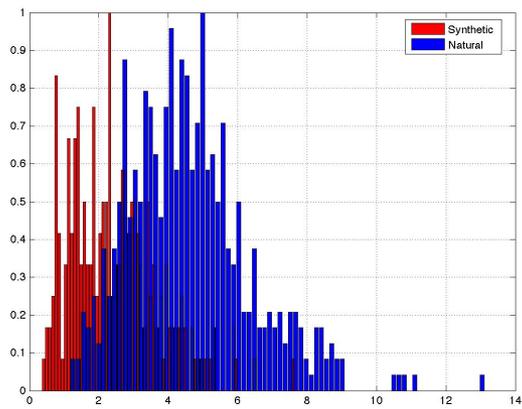
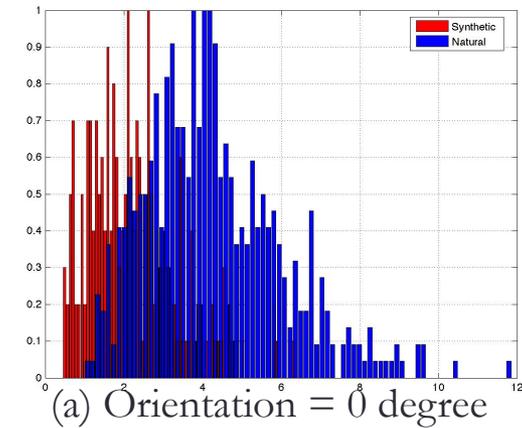
- In particular:

$$h_{\theta}(\mathbf{x}) = (\cos \theta)h_0(\mathbf{x}) + (\sin \theta)h_{\frac{\pi}{2}}(\mathbf{x}) \quad \mathfrak{F} \quad (\cos \theta)H_0(\mathbf{u}) + (\sin \theta)H_{\frac{\pi}{2}}(\mathbf{u}) = H_{\theta}(\mathbf{u})$$

- A **derivative-of-gaussian** filter of **any orientation** (derivative direction) is exactly a **linear combination of two** orthogonal derivative-of-gaussian filters

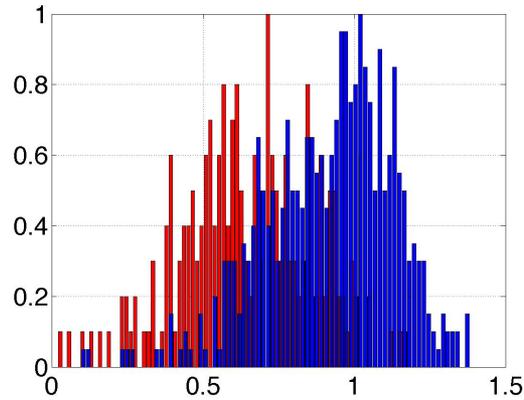
[Ref: Dr. Alan C. Bovik, EE381V Digital Video, Spring 2015]

ESPL IQA: Steerable Pyramid comparison

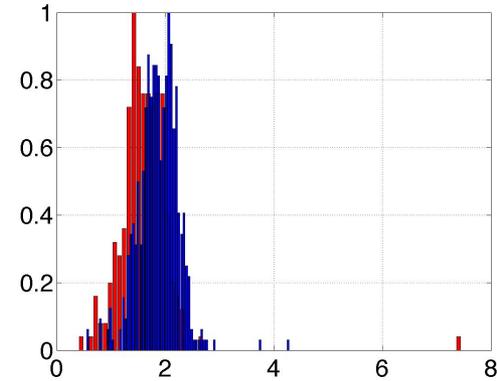


Histogram of scale (a)(b) and shape parameters(c)(d) of the steerable pyramid decomposition of synthetic images (221 images) and natural images [Martin2001] (500 images from Berkeley Segmentation Dataset)

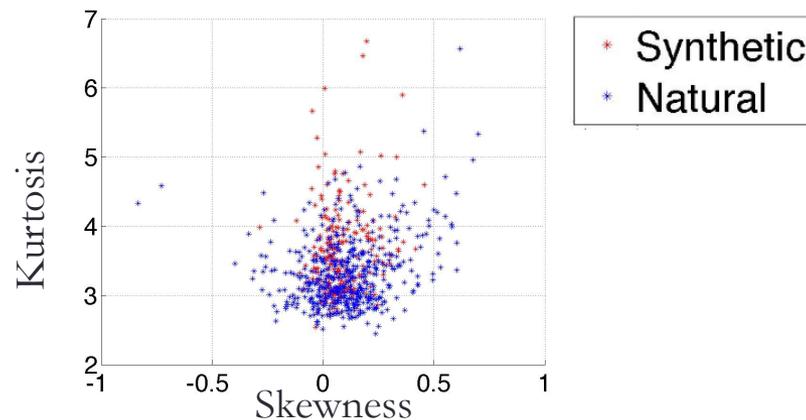
ESPL IQA: Comparison with Natural Scenes



Histogram of scale parameter
(JS divergence = 1.5655)



Histogram of shape parameter
(JS divergence = 1.0503)

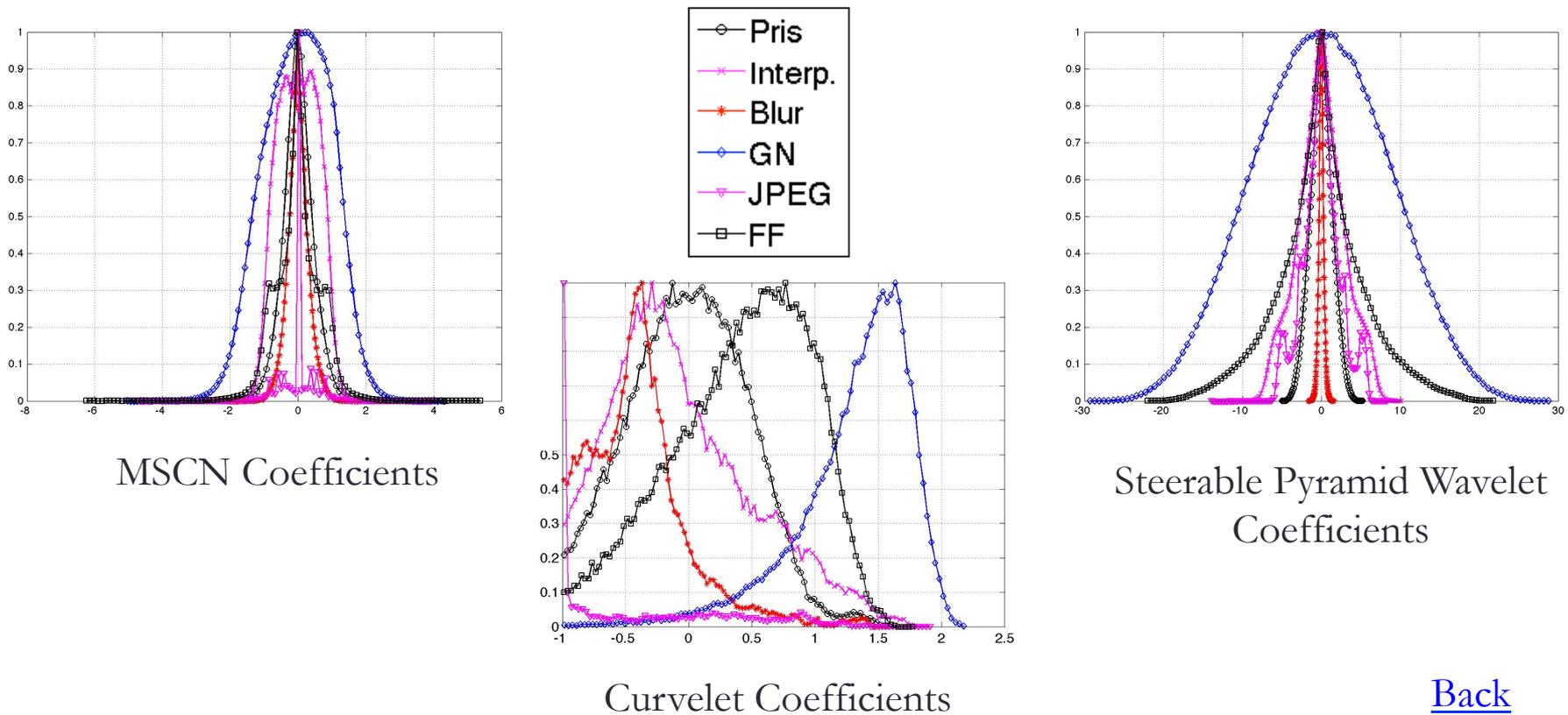


Skewness-kurtosis scatter plot

of MSCN coefficients of synthetic images [Kundu2014] (221 images) and natural images [Martin2001] (500 images from Berkeley Segmentation Dataset)

ESPL IQA: Distorted Image Statistics in Different Domains

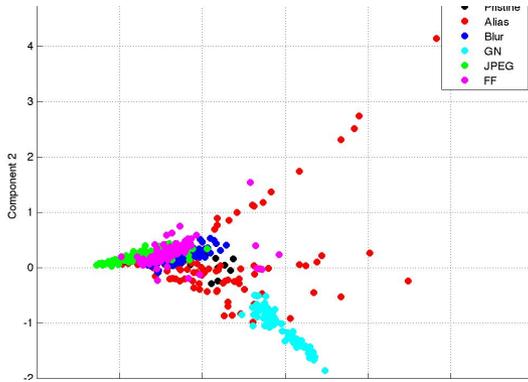
- Different **distortions affect scene statistics** characteristically
- Can be used for distortion classification and blind quality prediction



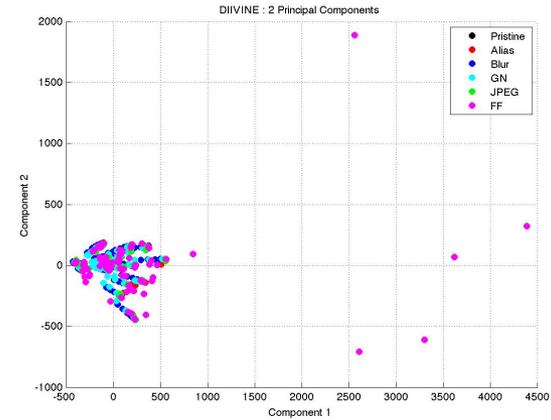
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ESPL Objective IQA: Classification using NSS

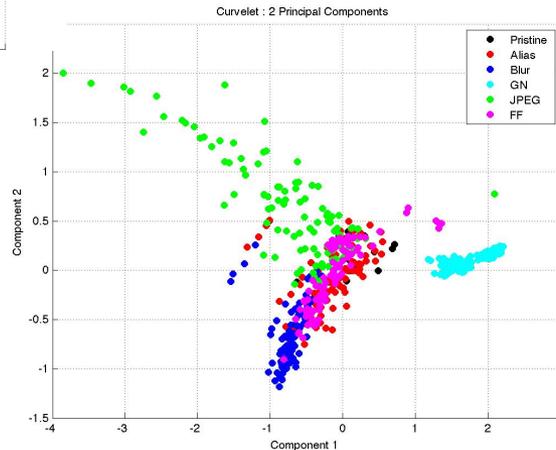
- Singular value decomposition of blind IQA features in 2-D



BRISQUE features (MSCN)



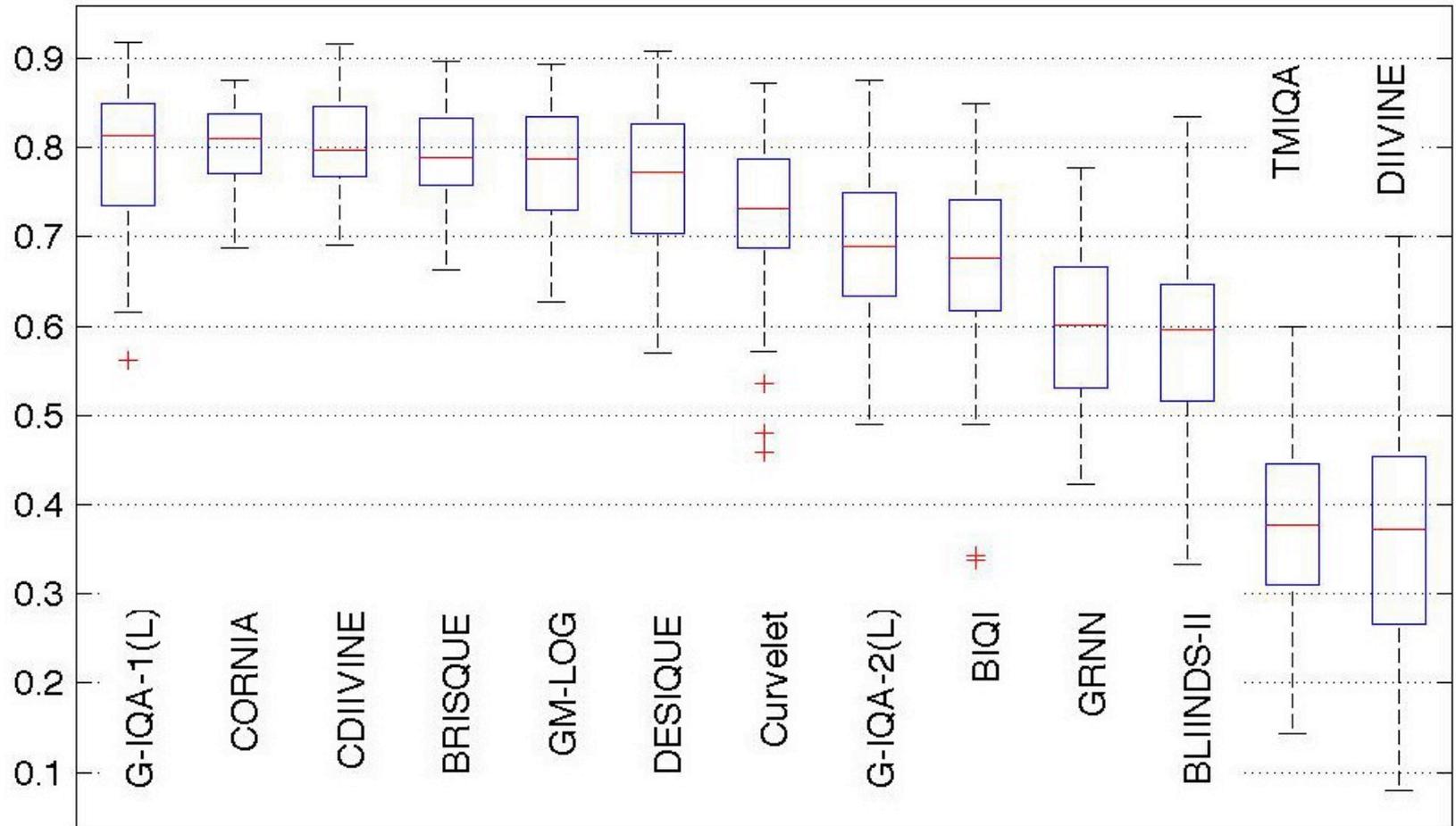
DIIVINE features (Wavelets)



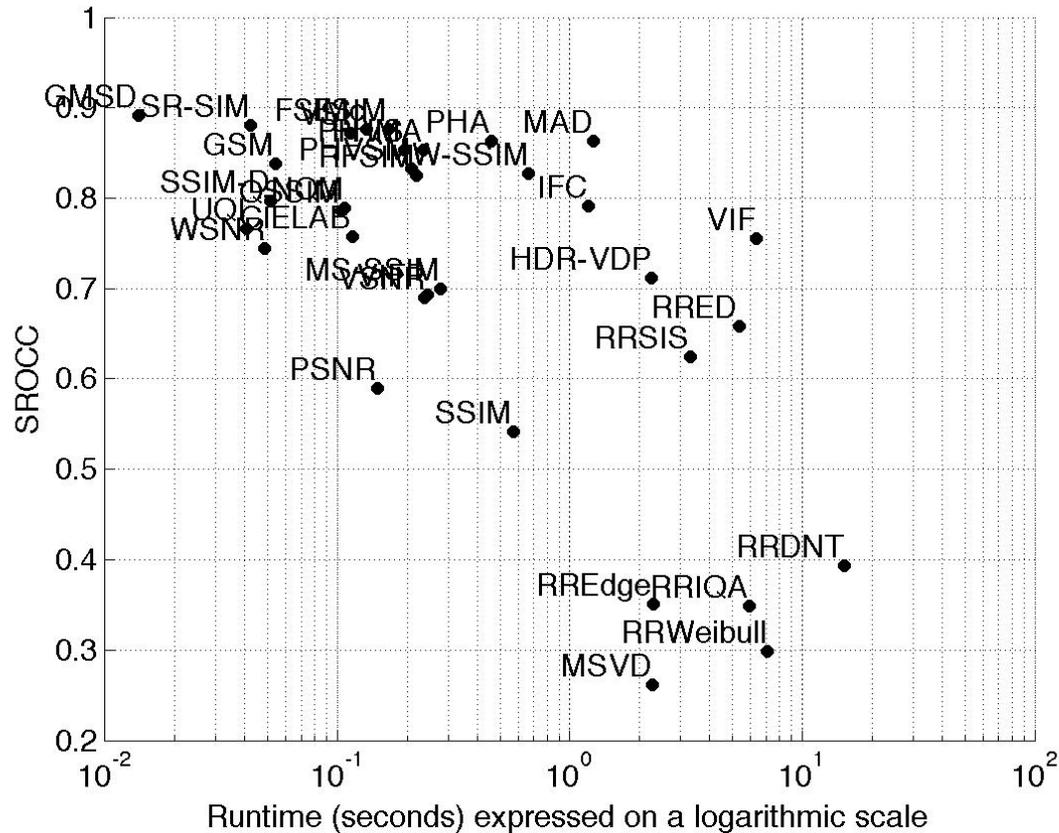
CurveletQA features (Curvelets)

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ESPL IQA : Box plot of No-reference SROCC

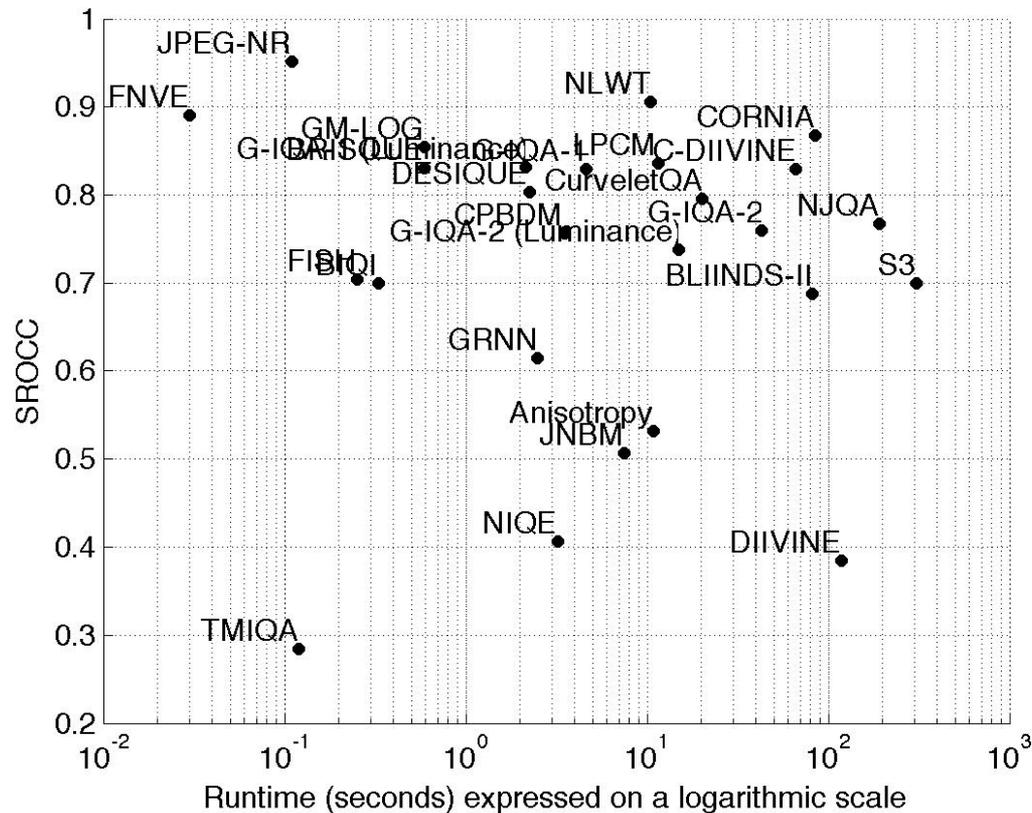


ESPL IQA: Performance-Time Complexity Tradeoff (FR, RR-IQAs)



- FR-IQA: **SR-SIM, GMSD** show good performance-complexity tradeoff

ESPL IQA: Performance-Time Complexity Tradeoff (NR-IQAs)



- Some **NR-IQA** metrics comparable with the best FR-IQA algorithms.

HDR IQA: Multi Exposure Fusion

$$Y(i) = \sum_{k=1}^K W_k(i) X_k(i)$$

- K : Number of multi-exposure input images
- Y : Fused Image
- $X_k(i)$: Luminance (or coefficient amplitude in transform domain) at i -th pixel in k -th exposure image
- $W_k(i)$: Weight at i -th pixel in k -th exposure image
 - Spatially adaptive
 - Varies according to perceptual importance of different exposure levels.
- Requires
 - Camera calibration
 - Motion compensation

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HDR IQA: Tone Mapped Quality Index (TMQI)

[Yeganeh, 2013]

- Based on Structural Similarity (SSIM) Index
- Does not penalize **change in signal strength** between HDR and SDR image patches
- Only penalized cases when signal strength is **significant** in one image patch but not in the other
- Local standard deviation nonlinearly mapped so that:
 - Significant signal strength mapped to 1
 - Insignificant signal strength mapped to 0
- CDF of Gaussian distribution is used for non-linear mapping:
$$p(s) = \frac{1}{\sqrt{2\pi}\theta_s} \int_{-\infty}^s \exp\left[-\frac{(x - \tau_s)^2}{2\theta_s^2}\right] dx$$
- Structural fidelity computation over **multiple scales**

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HDR IQA: Naturalness Measure

- TMQI combines structural similarity score (S) with naturalness (N) measure

$$Q = aS^\gamma + (1 - a)N^\delta$$

$$N = \frac{1}{K} P_m P_d$$

- P_m : Gaussian fit to means of natural images $P_m(m) = \frac{1}{\sqrt{2\pi}\sigma_m} \exp\left[-\frac{m - \mu_m}{2\sigma_m^2}\right]$
- P_d : Beta fit to standard deviations of natural images:

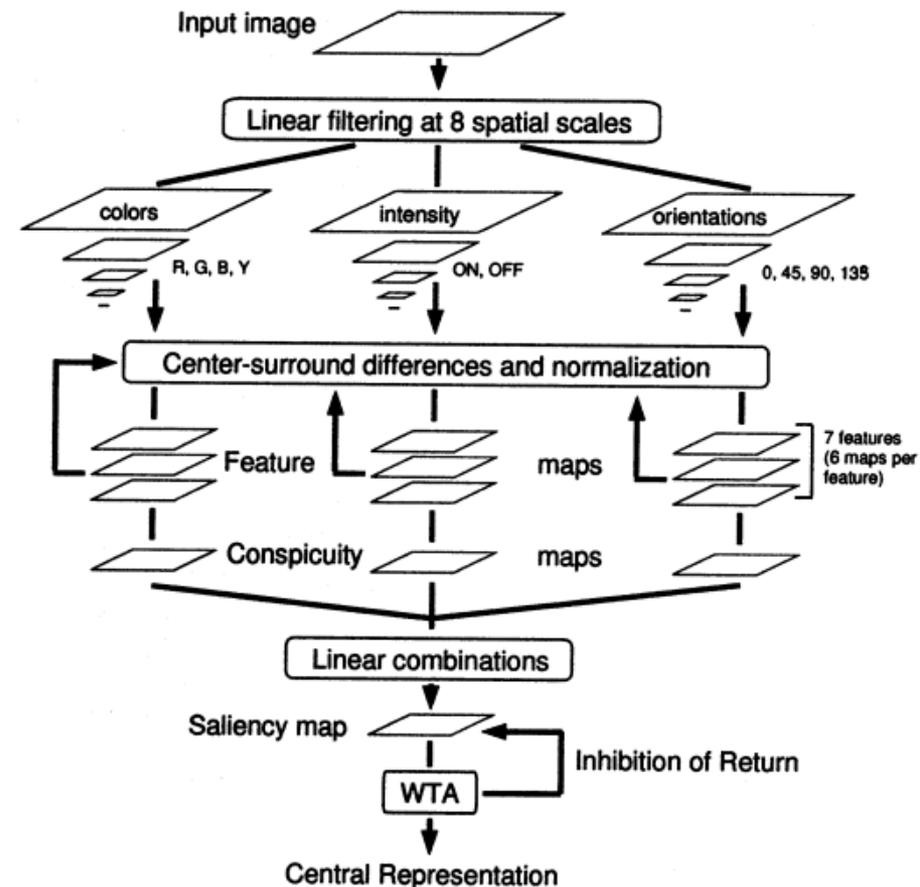
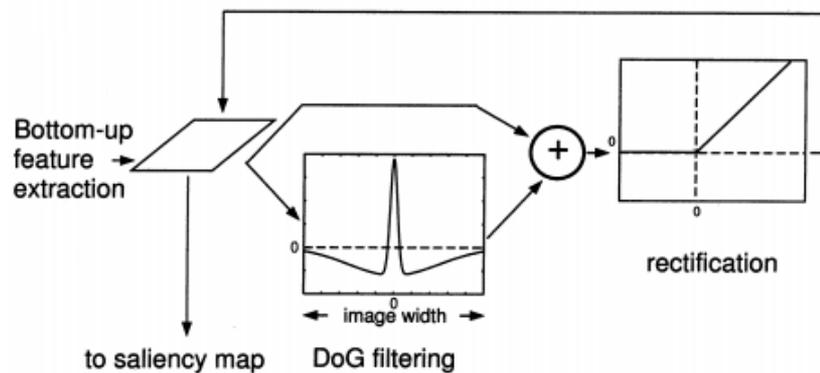
$$P_d(d) = \frac{(1 - d)^{\beta_d - 1} d^{\alpha_d - 1}}{B(\alpha_d, \beta_d)}$$

- γ, δ are sensitivity parameters

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HDR IQA: Itti and Koch's Saliency

- Different scales: Implemented as Gaussian Pyramid
- Center Surround mechanism:
 - Implemented with DoG
- LPF repeated over multiple scales
- 3 scales, 4 orientations used



HDR IQA: Local weighing using local entropy

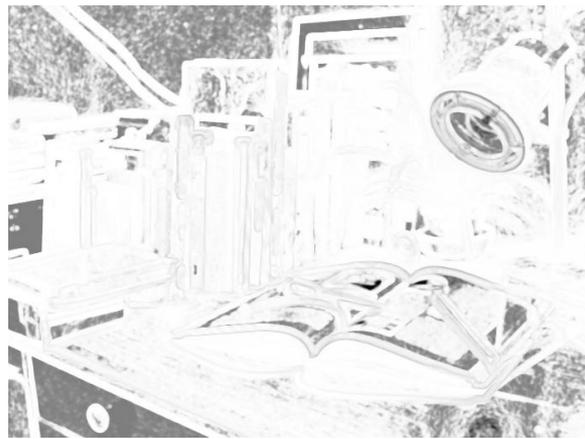
- **Local entropy filtering** at every pixel leads to detecting high contrast regions
- Gives a measure of local **randomness**

$$H(I) = - \sum_i p(h_i) \log[p(h_i)]$$

- $p(h)$ is the probability of intensity h



Tone mapped image



Structural fidelity map



Structural fidelity with pooling

HDR IQA: Results on HDR-JPEG database [Narwaria2013]

- 10 source HDR images
- Each source image has 14 degraded versions
- JPEG coding with 7 different bit rates.
- SSIM and MSE are two optimization criteria used

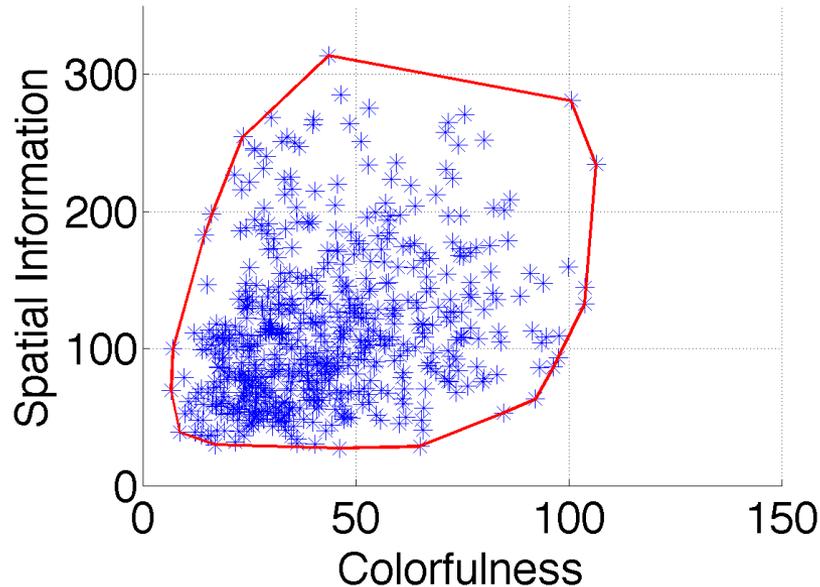
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FR-IQA Algorithms	SROCC	PLCC	Time(s)
SHDR-TMQI (Proposed)	0.8510	0.8533	3.0003
TMQI-NSS-Sigma (Proposed)	0.8485	0.8520	1.6470
TMQI-NSS-Entropy (Proposed)	0.8454	0.8645	6.7424
Tone Mapped Image Quality Index (TMQI)[Yeganeh2013]	0.7947	0.8057	3.4394
FSITM-TMQI[Nafchi2014]	0.6300	0.6584	8.3486
TMQI-II[Ma2015]	0.5096	0.5137	1.3424
Feature Similarity Index for Tone-Mapped Images(FSITM) [Nafchi2014]	0.4720	0.5167	5.2617
STMQI[Nasrinpour2015]	0.3464	0.3244	11.9965

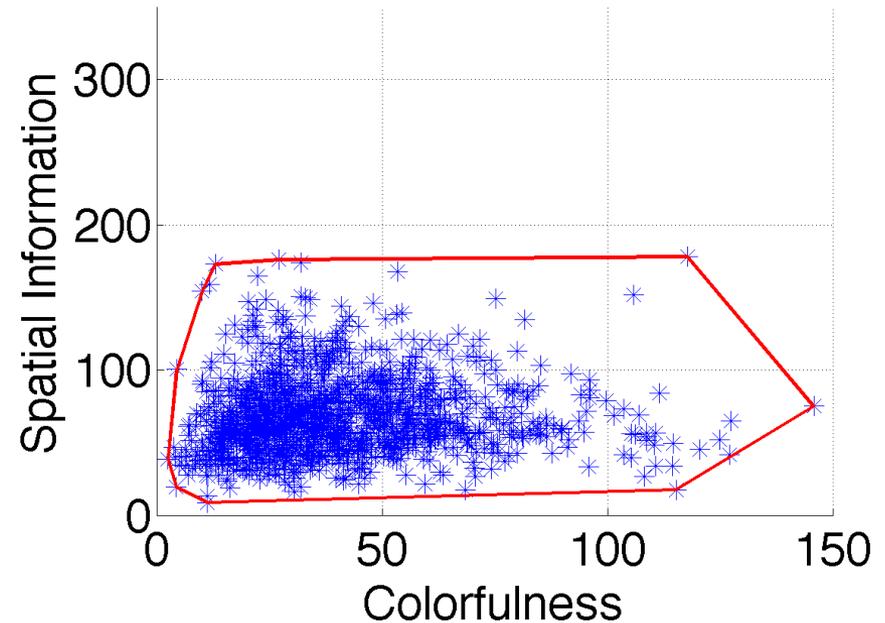
ESPL-LIVE HDR Database: Source Complexity

- **Spatial Information**: Indicates edge energy
- **Colorfulness**: Indicates the variety and intensity of colors
- Computed on medium exposure image in source exposure stack

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ESPL-LIVE HDR Database

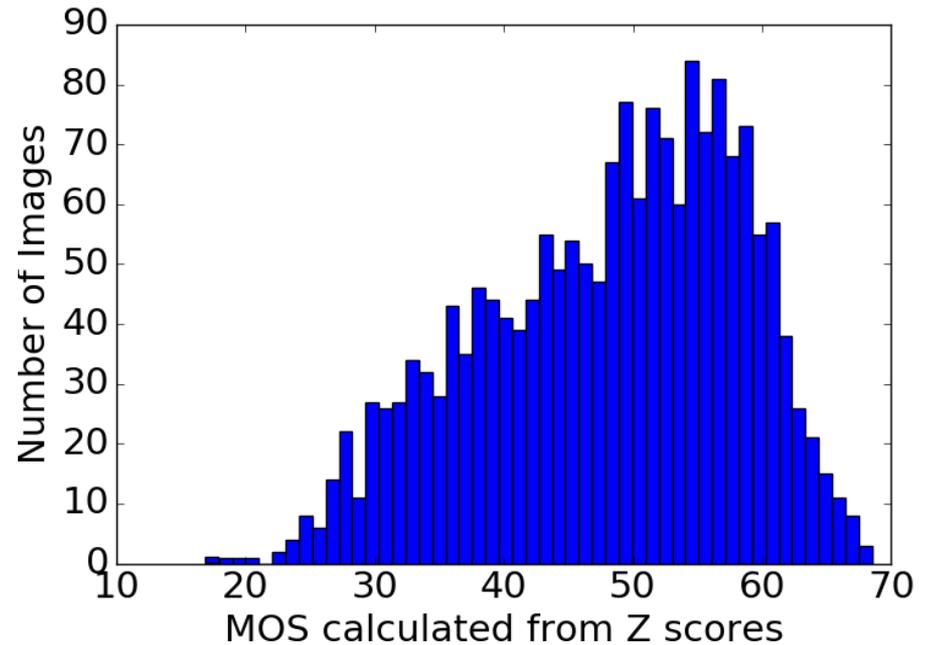
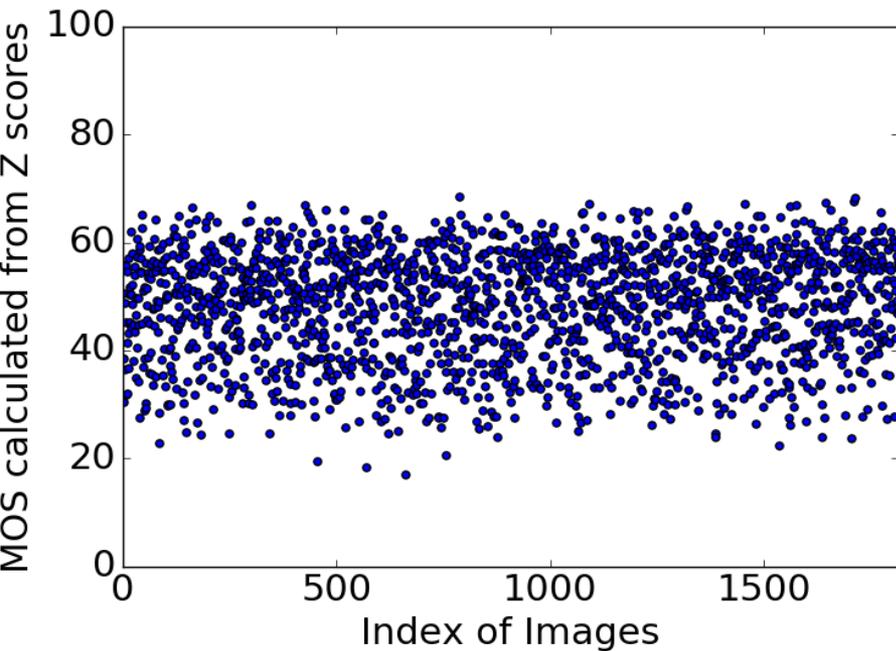


LIVE Challenge Database[Ghadiyaram2016]

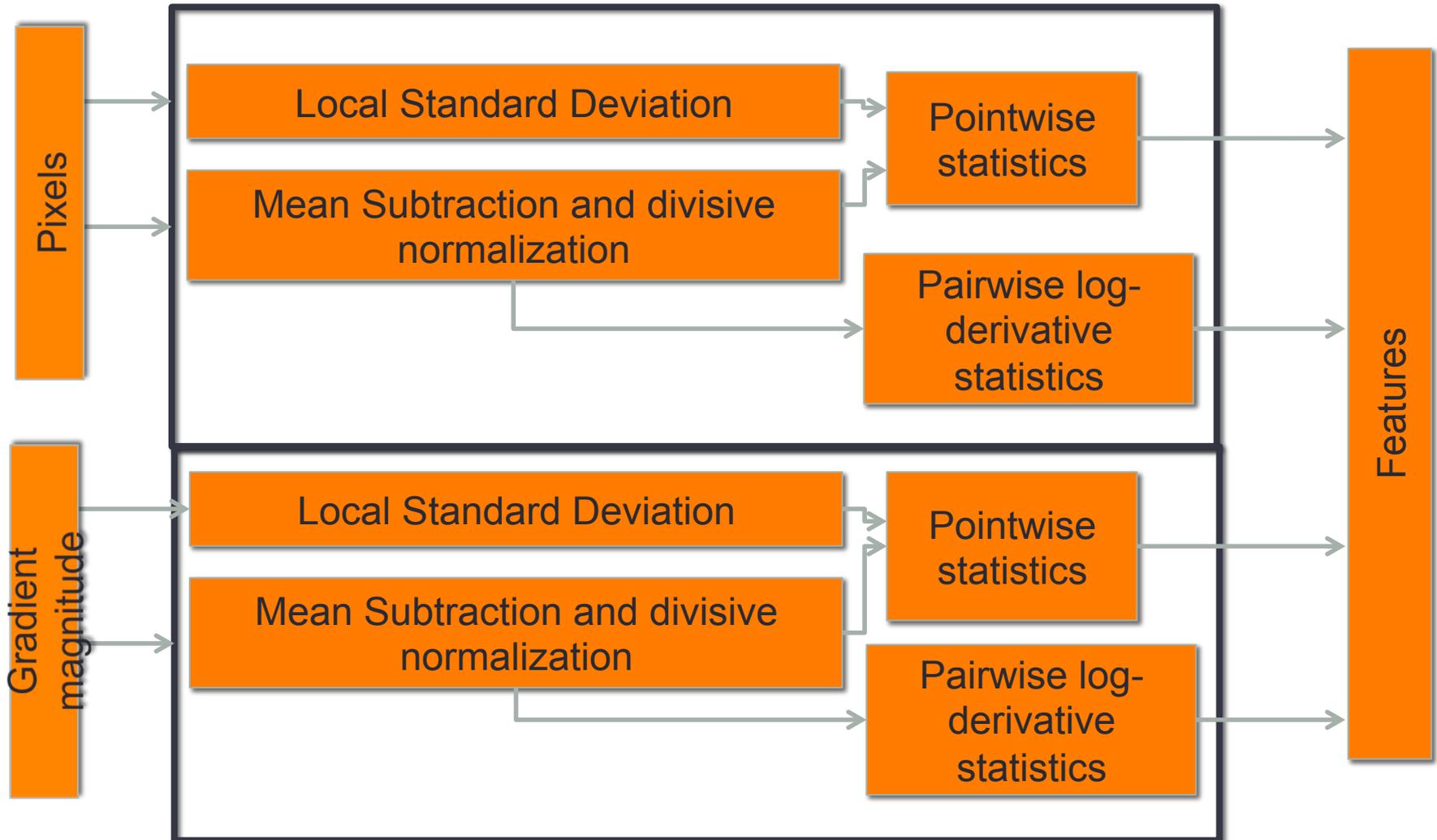
[Details](#)

HDR-IQA: Z-Scores Distributions

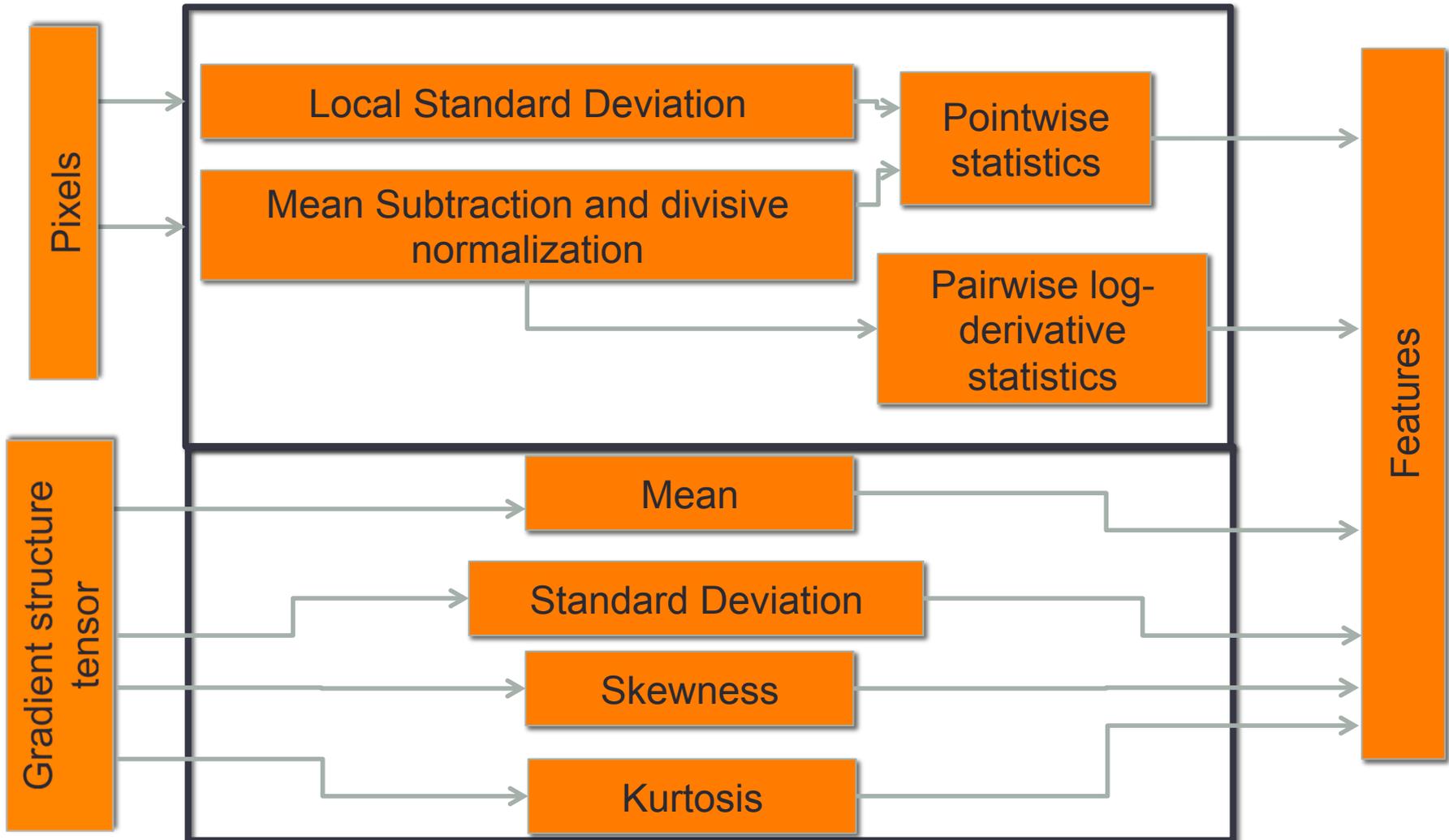
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Gradient Image Quality Assessment-1

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Gradient Image Quality Assessment-2

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HDR IQA: Log Derivative Computation

- Logarithm of each MSCN coefficient is computed

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$$\hat{I}(i, j) = \frac{I(i, j) - \mu(i, j)}{\sigma(i, j) + 1}$$

$$J(i, j) = \log[\hat{I}(i, j) + K]$$

- Seven types of **log-derivatives** defined

$$D1 : \nabla_x J(i, j) = J(i, j+1) - J(i, j)$$

$$D2 : \nabla_y J(i, j) = J(i+1, j) - J(i, j)$$

$$D3 : \nabla_{xy} J(i, j) = J(i+1, j+1) - J(i, j)$$

$$D4 : \nabla_{yx} J(i, j) = J(i+1, j-1) - J(i, j)$$

$$D5 : \nabla_x \nabla_y = J(i-1, j) + J(i+1, j) - J(i, j-1) - J(i, j+1)$$

$$D6 : \nabla_{cx} \nabla_{cy} J(i, j)_1 = J(i, j) + J(i+1, j+1) - J(i, j+1) - J(i+1, j)$$

$$D7 : \nabla_{cx} \nabla_{cy} J(i, j)_2 = J(i-1, j-1) + J(i+1, j+1) - J(i-1, j+1) - J(i+1, j-1)$$

Gradient Structure Tensor Coherence

- G_x : Vertical component of gradient
- G_y : Horizontal component of gradient
- Computed by convolving with difference-of-Gaussians
- Gradient structure tensor is defined as:

$$J = \begin{bmatrix} f(G_x) & f(G_x G_y) \\ f(G_x G_y) & f(G_y) \end{bmatrix}$$

$$f(V) = \sum_{l,k} w[l,j] V(i-k, j-k)^2$$

- λ_1 and λ_2 are the two eigenvalues of gradient structure tensor
- C: Gradient structure tensor coherence:

$$C = \left(\frac{\lambda_1 - \lambda_2}{\lambda_1 + \lambda_2} \right)^2$$

- Computed over 9x9 non-overlapping blocks
- Features are: mean, standard deviation, skewness and kurtosis of C

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No-reference IQAs on LIVE Database

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Algorithms	JP2K	JPEG	GN	Blur	FF	Overall
GM-LOG	0.882	0.878	0.978	0.915	0.899	0.914
G-IQA-1	0.905	0.883	0.983	0.917	0.836	0.906
G-IQA-2	0.904	0.867	0.982	0.920	0.841	0.904
BRISQUE	0.878	0.852	0.962	0.941	0.863	0.902
BLIINDS-II	0.907	0.846	0.939	0.906	0.884	0.897
DESIQUE	0.875	0.824	0.975	0.908	0.829	0.878
CurveletQA	0.816	0.827	0.969	0.896	0.826	0.863
DIIVINE	0.824	0.759	0.937	0.854	0.759	0.827
<i>MS-SSIM</i>	<i>0.963</i>	<i>0.979</i>	<i>0.977</i>	<i>0.954</i>	<i>0.939</i>	<i>0.954</i>
<i>SSIM</i>	<i>0.939</i>	<i>0.947</i>	<i>0.964</i>	<i>0.905</i>	<i>0.939</i>	<i>0.913</i>
<i>PSNR</i>	<i>0.865</i>	<i>0.883</i>	<i>0.941</i>	<i>0.752</i>	<i>0.874</i>	<i>0.864</i>

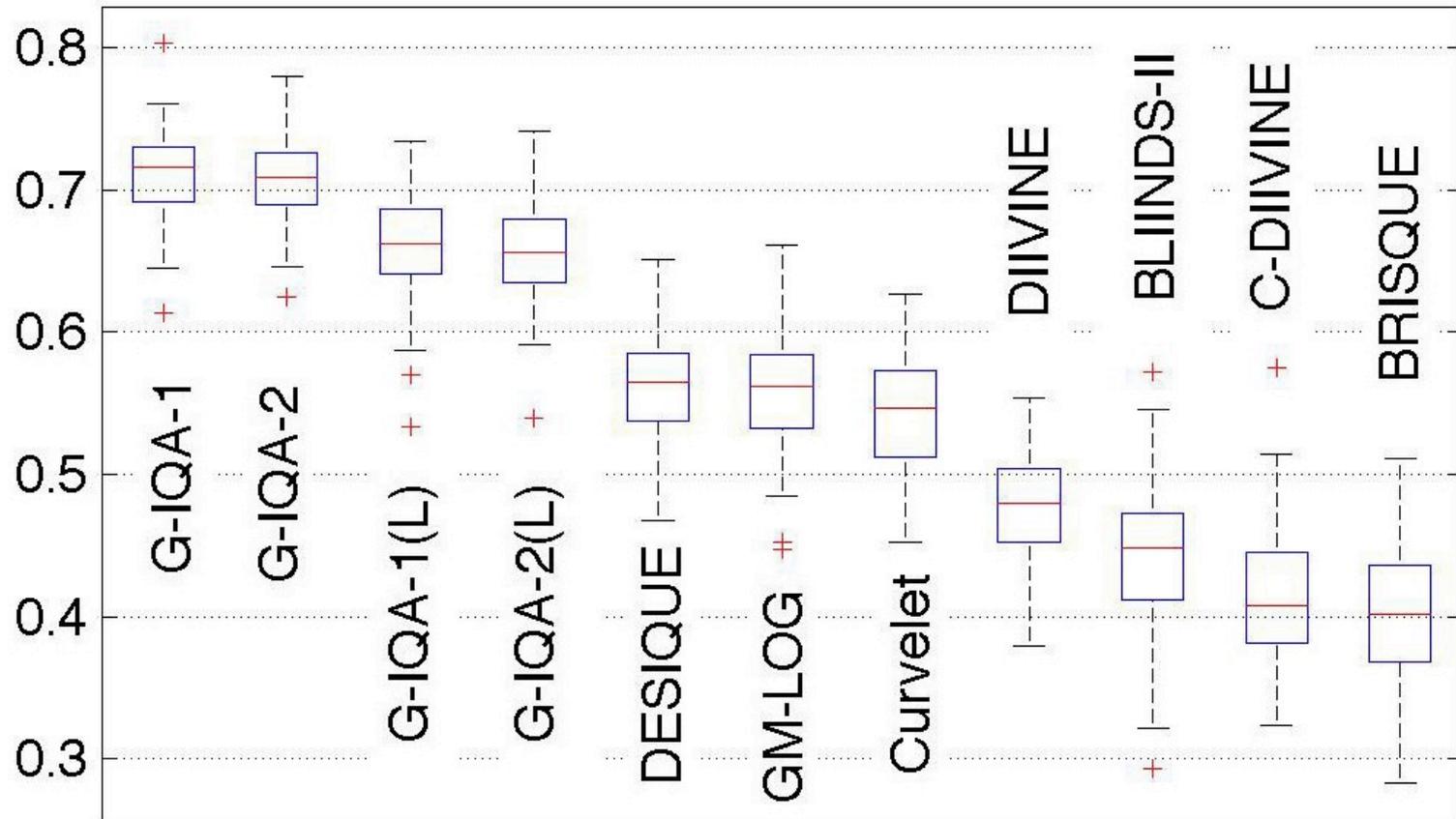
Italics indicate full-reference algorithms

F-test on residuals between IQAs and DMOS [Back](#)

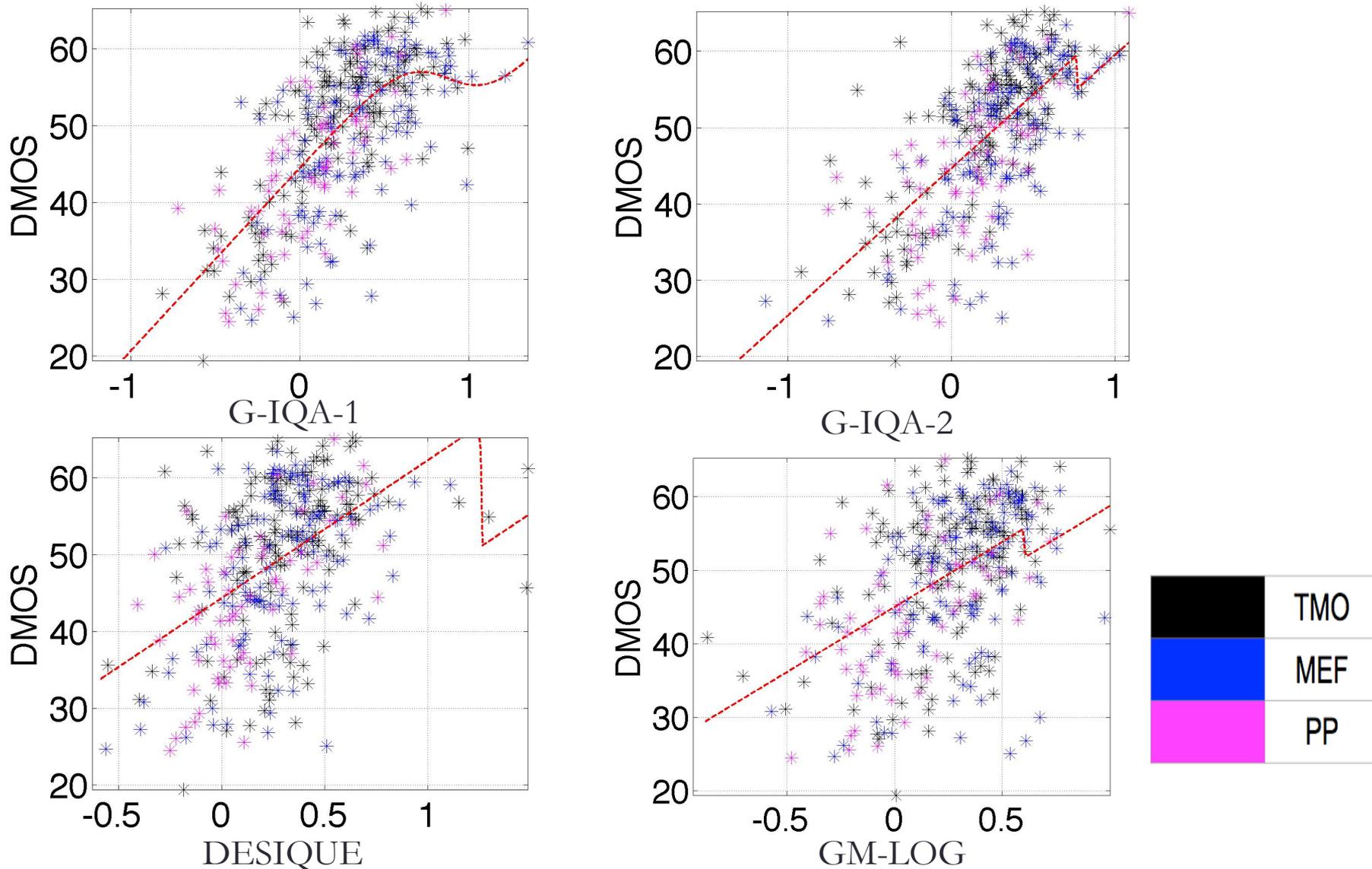
	A	B	C	D	E	F	G	H	I
A	----	----	1--1	1--1	1--1	1--1	1--1	1-11	---1
B	----	----	1--1	1--1	1--1	1--1	1--1	11-1	1--1
C	0--0	0--0	----	----	----	----	----	----	0---
D	0--0	0--0	----	----	----	----	----	----	0---
E	0--0	0--0	----	----	----	----	----	----	----
F	0--0	0--0	----	----	----	----	----	----	0---
G	0--0	0--0	----	----	----	----	----	----	----
H	0-00	00-0	----	----	----	----	----	----	0--0
I	---0	0--0	1---	1---	----	1---	----	1--1	----

A : G-IQA-1, B : G-IQA-2, C : DESIQUÉ, D : BRISQUE. E : GM-LOG
 F : C-DIIVINE, G : DIIVINE, H : BLINDS-II, I : CurveletQA

HDR-IQA: Box plot of No-reference SROCC

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HDR IQA: Scatter plot of MOS vs IQA scores



HDR IQA: Estimating irradiance map

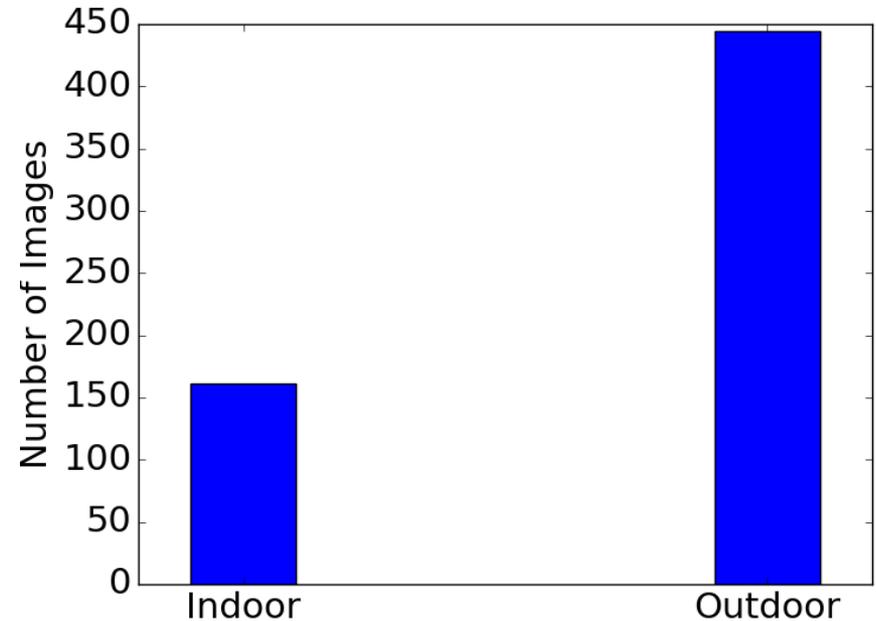
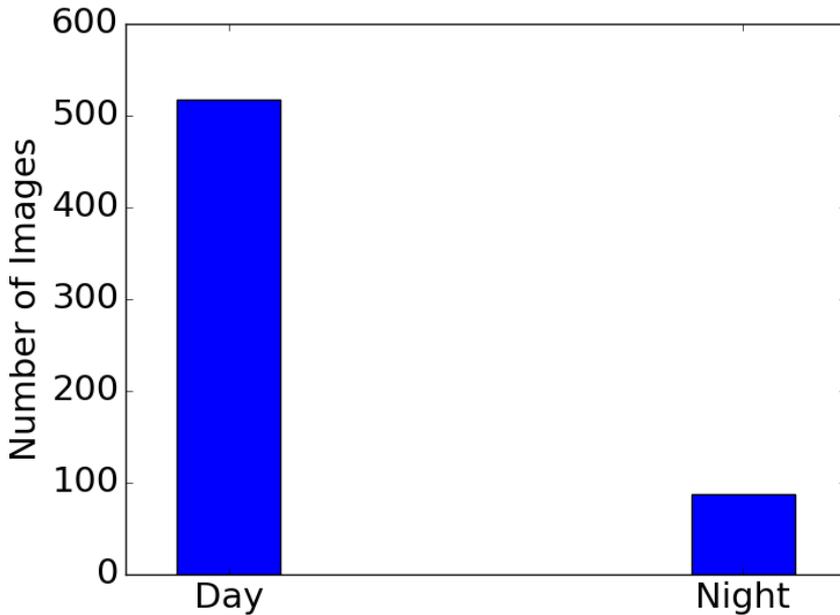
$$Z_{ij} = f(E_i t_j)$$

$$f^{-1}(Z_{ij}) = E_i t_j$$

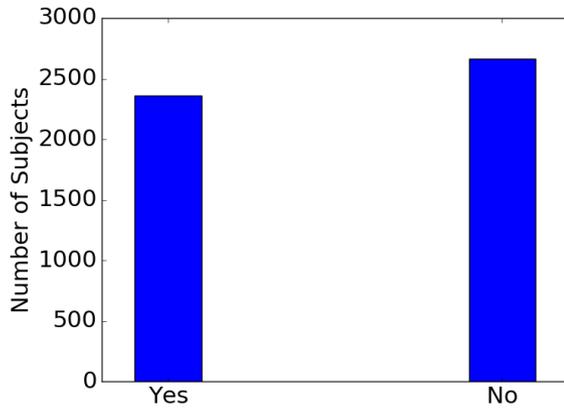
$$\ln f^{-1}(Z_{ij}) = \ln(E_i) + \ln(t_j)$$

$$\ln f^{-1}(Z_{ij}) = \ln(E_i) + \ln(t_j)$$

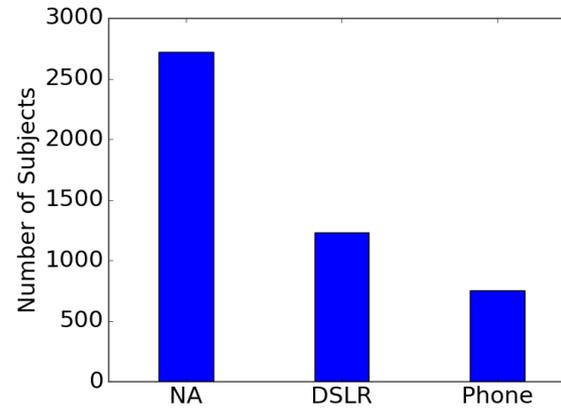
HDR IQA: Source Image Content



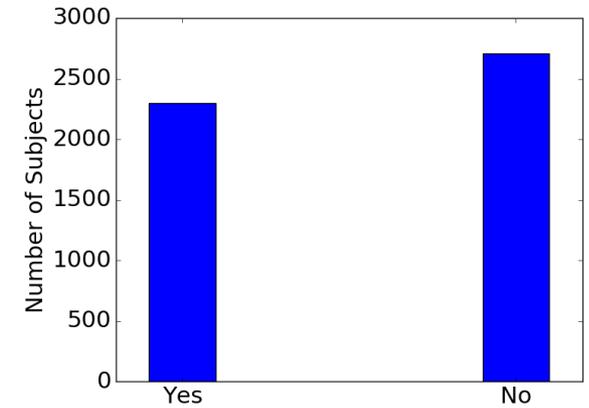
HDR IQA: Demographics and Display parameters



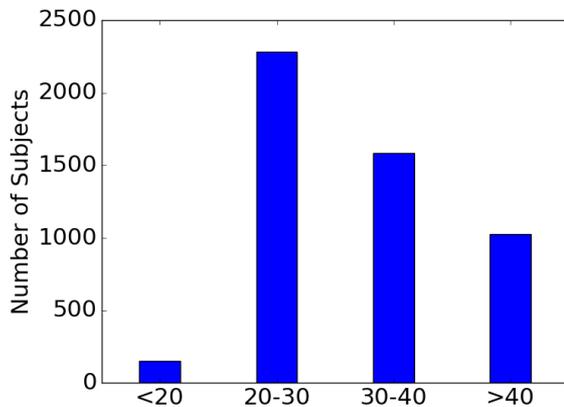
HDR familiarity



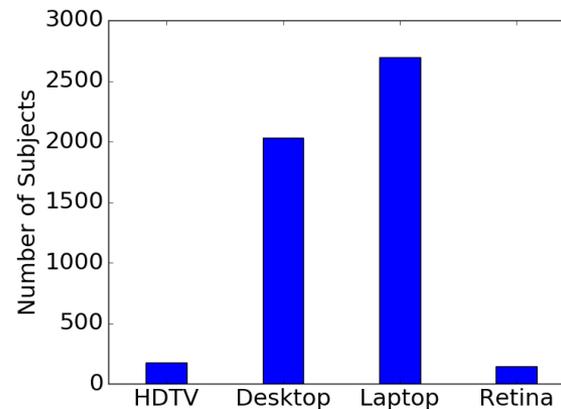
HDR Device used



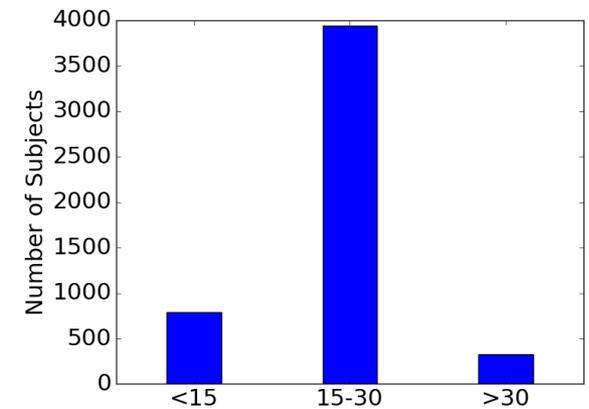
HDR software familiarity



Age of subjects



Display used



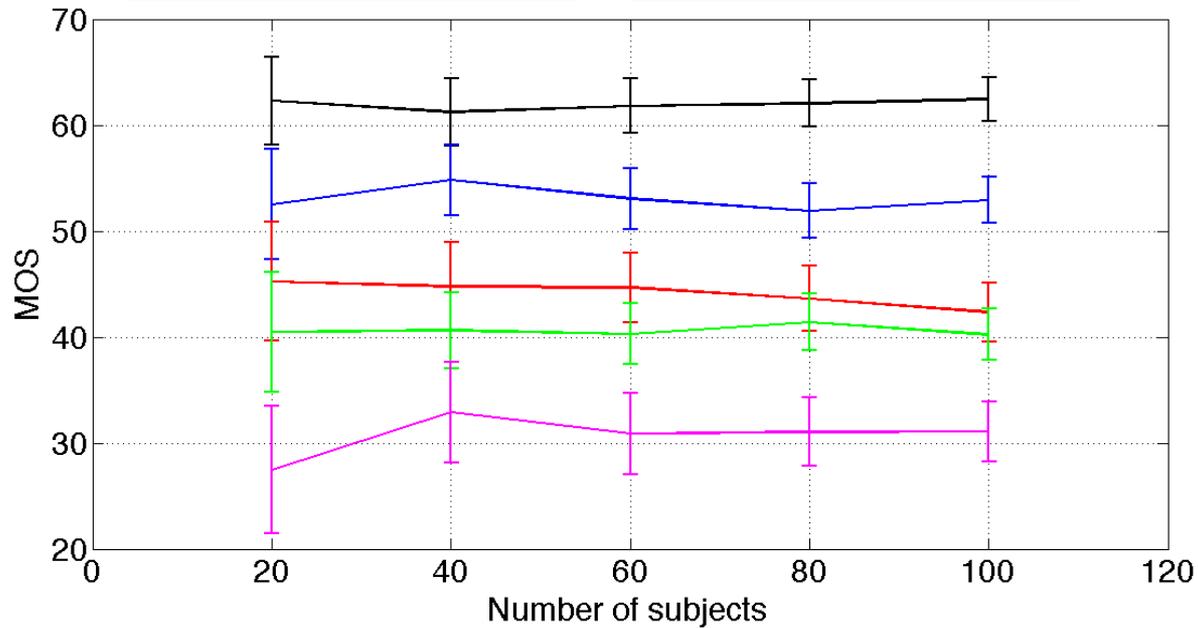
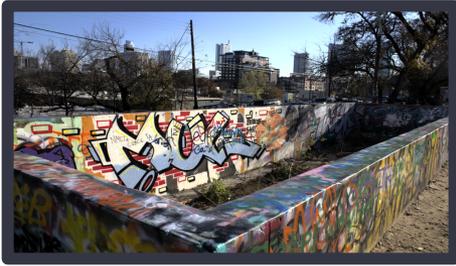
Distance from display

HDR-IQA: Processing of the raw scores (Cont'd)

- **Rating consistency:**
 - **Inter subject consistency** : PLCC between MOS obtained by dividing the workers into two disjoint groups was **0.9677** (randomized over 25 trials)
 - **Intra subject consistency**: Median PLCC between individual scores and MOS values for 'Gold Standard' images was **0.8697**
 - **Consistency with laboratory study**: Median PLCC between individual scores and MOS values for 'Gold Standard' images in laboratory setting was **0.9466**

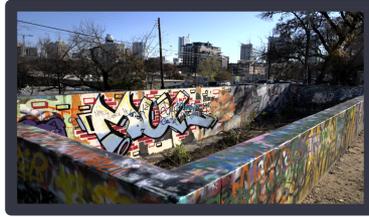
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HDR-IQA: MOS vs. Number of subjects



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HDR-IQA: Parameter variations



1



2



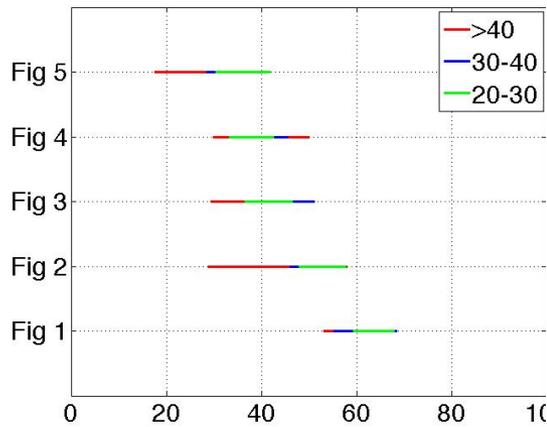
3



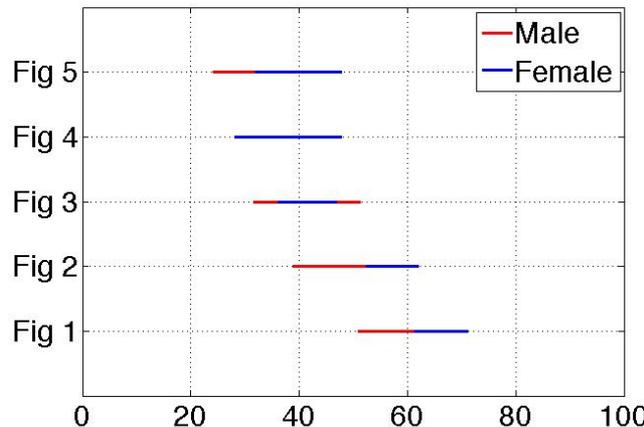
4



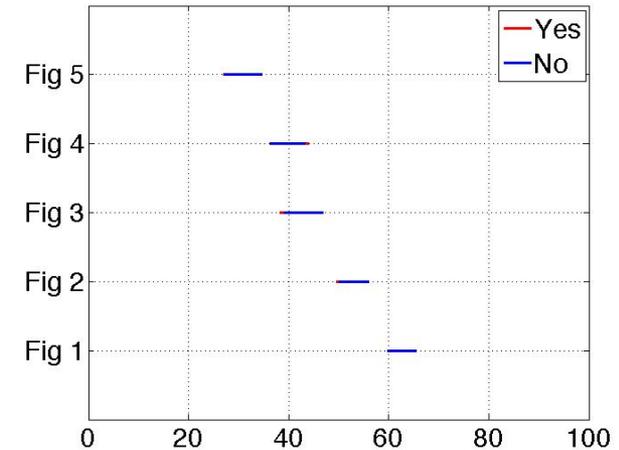
5



Variation with age



Variation with gender



Variation with HDR awareness

HDR-IQA: Parameter variations (cont'd)



1



2



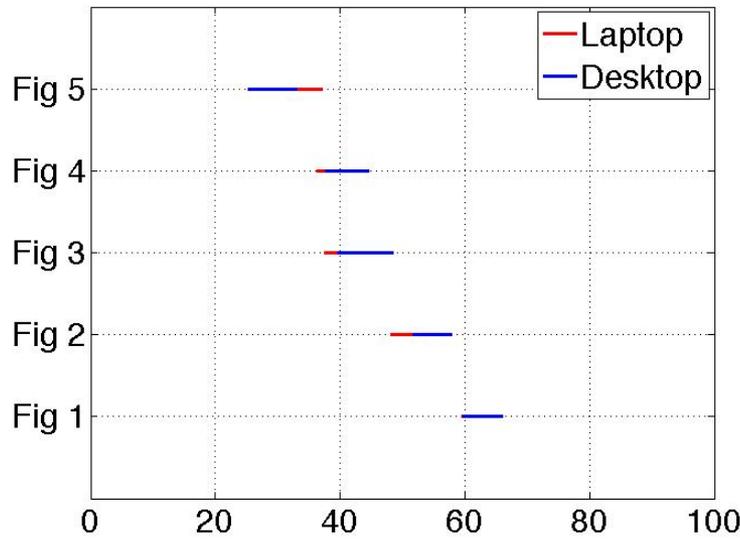
3



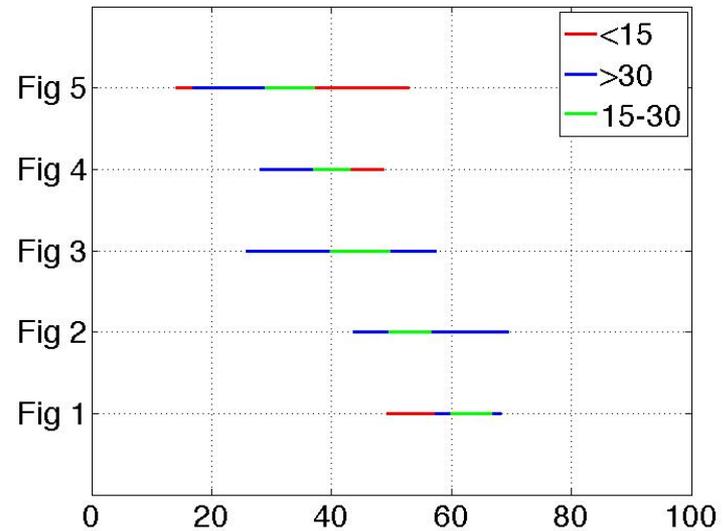
4



5



Variation with display



Variation with distance from display