

# Mobile Localization

- Safety

- ☞ Wireless E911 (FCC mandate by 2001)

- ☞ Emergency roadside service

- Tracking

- ☞ Fleet management for trucks

- ☞ Tracking children

- Billing

- ☞ Location sensitive billing

- ☞ Neighborhood cordless

- Information

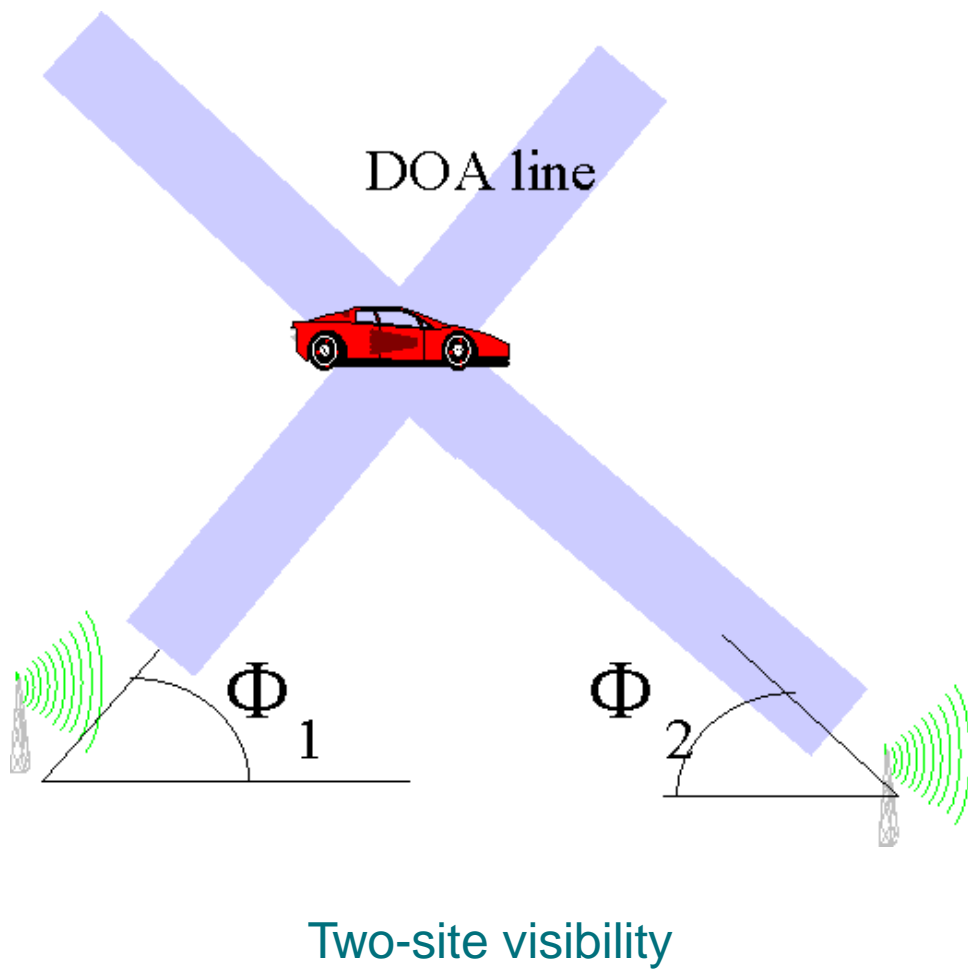
- ☞ Mobile yellow pages

- ☞ Driving directions

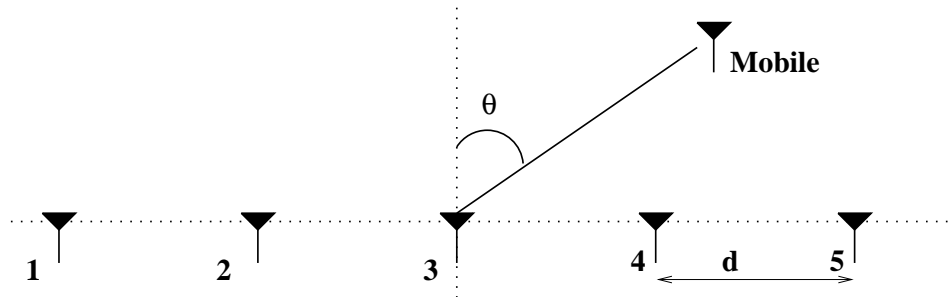
# System Requirements

- Mobile user requests its location
- Infrastructure-based solution
  - ☞ Support existing mobile phones
  - ☞ No additional cost to mobile phones
- Compatibility with different standards
  - ☞ Advanced Mobile Phone Service (AMPS)
  - ☞ Code Division Multiple Access (CDMA)
  - ☞ Global System for Mobile (GSM)
- Solutions at basestation
  - ☞ Single antenna
  - ☞ Antenna array (usually linear but sometimes triangular or circular)

## Location Based on Direction of Arrival (DOA)



## Direction of Arrival Estimation



- Sampling in space

Narrowband  
Delay  $\implies$  Phase Shift  
Assumption

$$\mathbf{a}(\theta) = [1 \quad e^{j2\pi f \frac{d}{c} \sin \theta} \quad \dots \quad e^{j2\pi f \frac{4d}{c} \sin \theta}]^T$$

For  $P$  paths,

$$\mathbf{A} = [\mathbf{a}(\theta_1) \quad \mathbf{a}(\theta_2) \quad \dots \quad \mathbf{a}(\theta_P)]$$

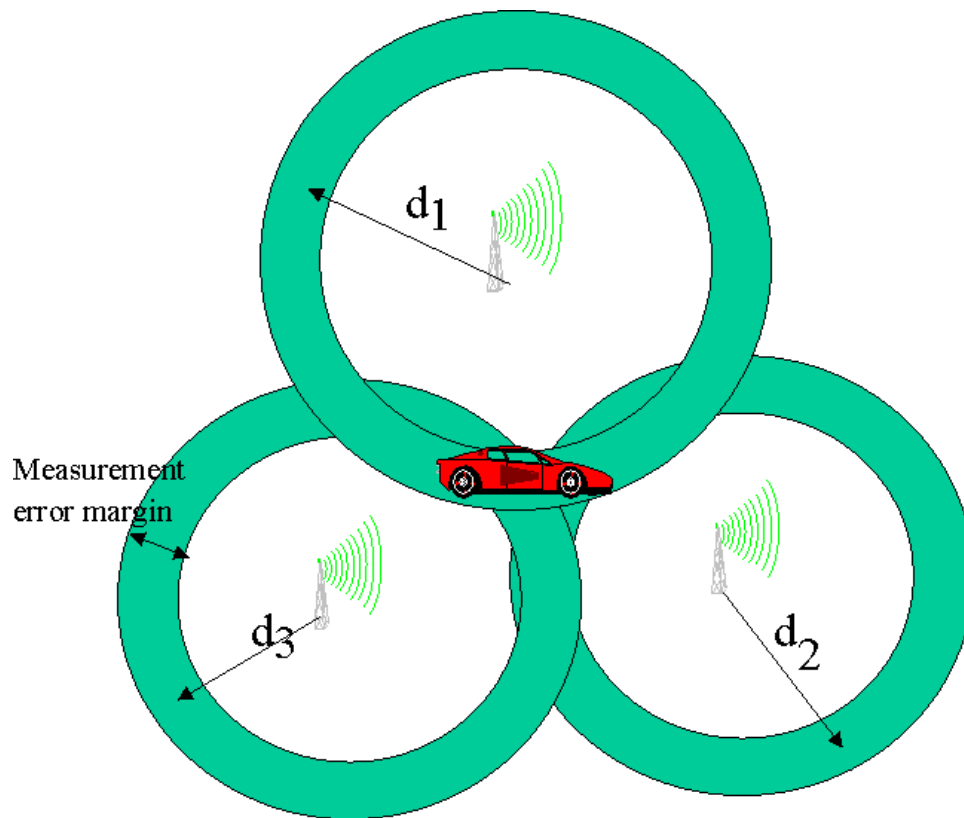
$\mathbf{A}$  is a Vandermonde matrix

- Estimate  $\theta_i$  using *Estimation of Signal Parameters using Rotational Invariance Techniques (ESPRIT)*

## Disadvantages of Using Direction of Arrival

- Few antenna elements at basestation (usually 4)
- Extremely sensitive to array calibration
  - ☞ Geometry of sensor layout
  - ☞ Mutual coupling of antenna elements
- No line-of-sight in urban environments
- Failure in absence of fading

## Location Based on Time of Arrival (TOA)



Three-site visibility required

## Time of Arrival Estimation

- Received signal  $\longrightarrow$  Sum of delayed versions of transmitted signal

$$\mathbf{S}(t) = [s(t - \tau_1) \ s(t - \tau_2) \ s(t - \tau_3) \ \dots \ s(t - \tau_P)]^T$$

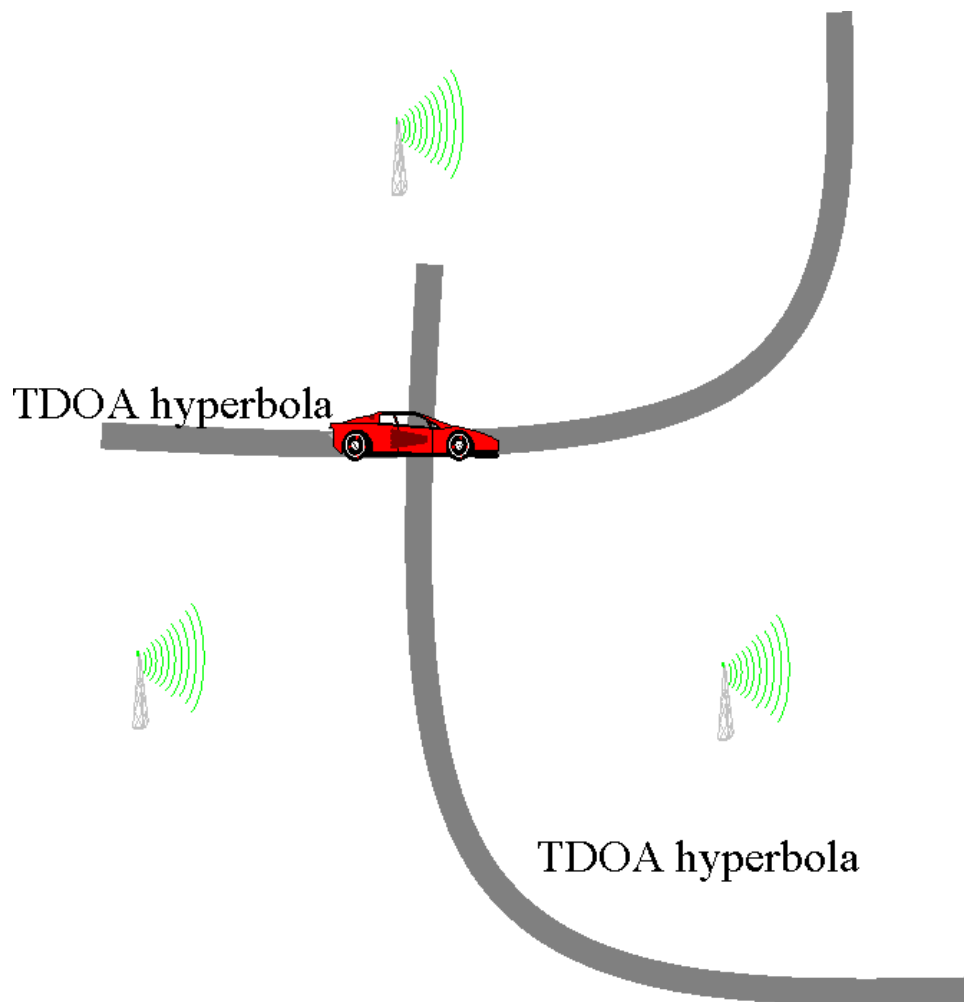
$$\begin{array}{ccc} \text{Delay } \tau_m & \xRightarrow{\text{Discrete}} & \text{Phase Shift } e^{j2\pi f \tau_m} \\ & \text{Fourier Transform} & \end{array}$$

$$\hat{\mathbf{S}} = [e^{j2\pi f \tau_1} \ e^{j2\pi f \tau_2} \ \dots \ e^{j2\pi f \tau_P}]^T \hat{s}(f)$$

where  $\hat{s}(f) = \mathcal{F}\{s(t)\}$

- Estimate time delays  $\{\tau_i\}$  using ESPRIT

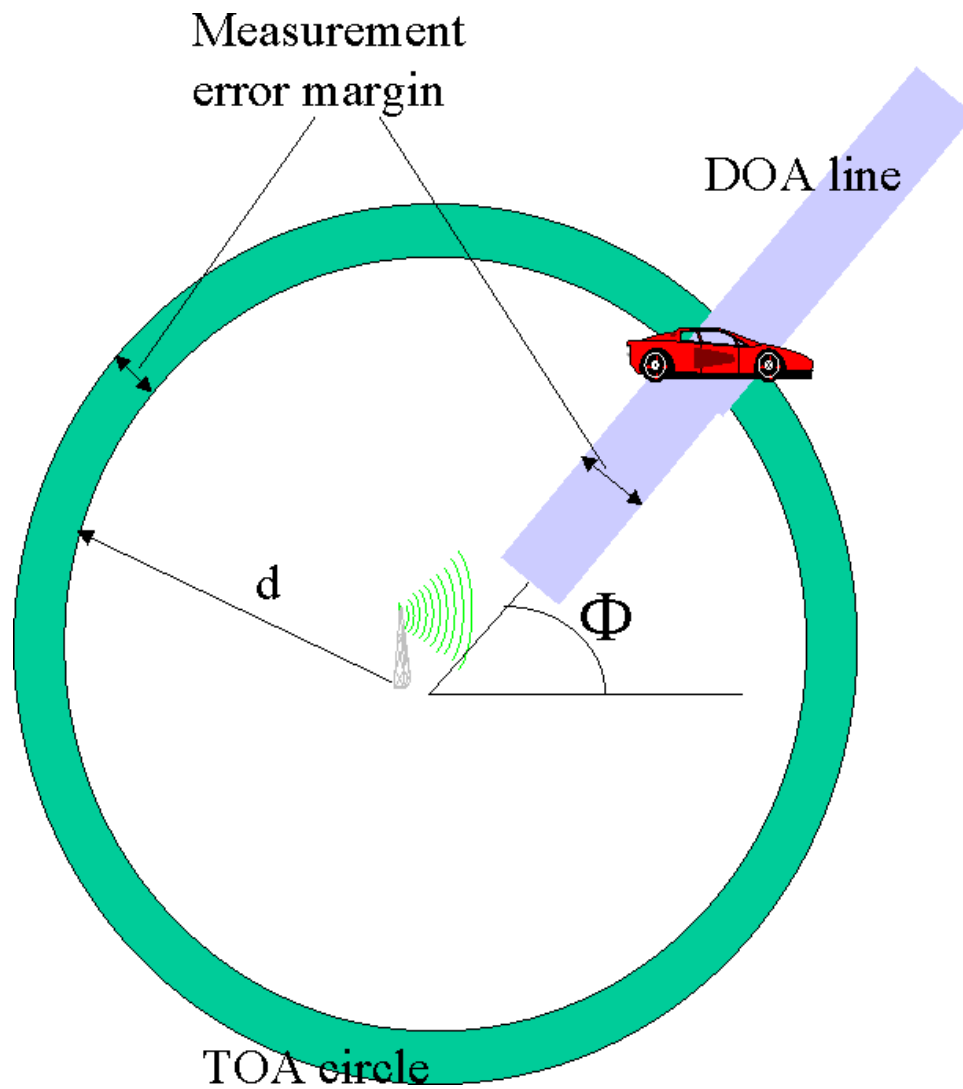
## Location Based on Time Difference of Arrival (TDOA)



Three-site visibility required



## Location Based on a Combination of DOA and TOA



Single-site visibility (35-40% of the cases)

# Joint Angle and Delay Estimation (JADE)

- 1-D ESPRIT

- ☞ Sequential estimation of DOAs and TOAs

- ☞ Classification problem

- JADE - ESPRIT

- ☞ Joint estimation of DOAs and TOAs

- ☞ Automatic pairing of DOAs and TOAs for each user

- Form a 2-D Vandermonde matrix

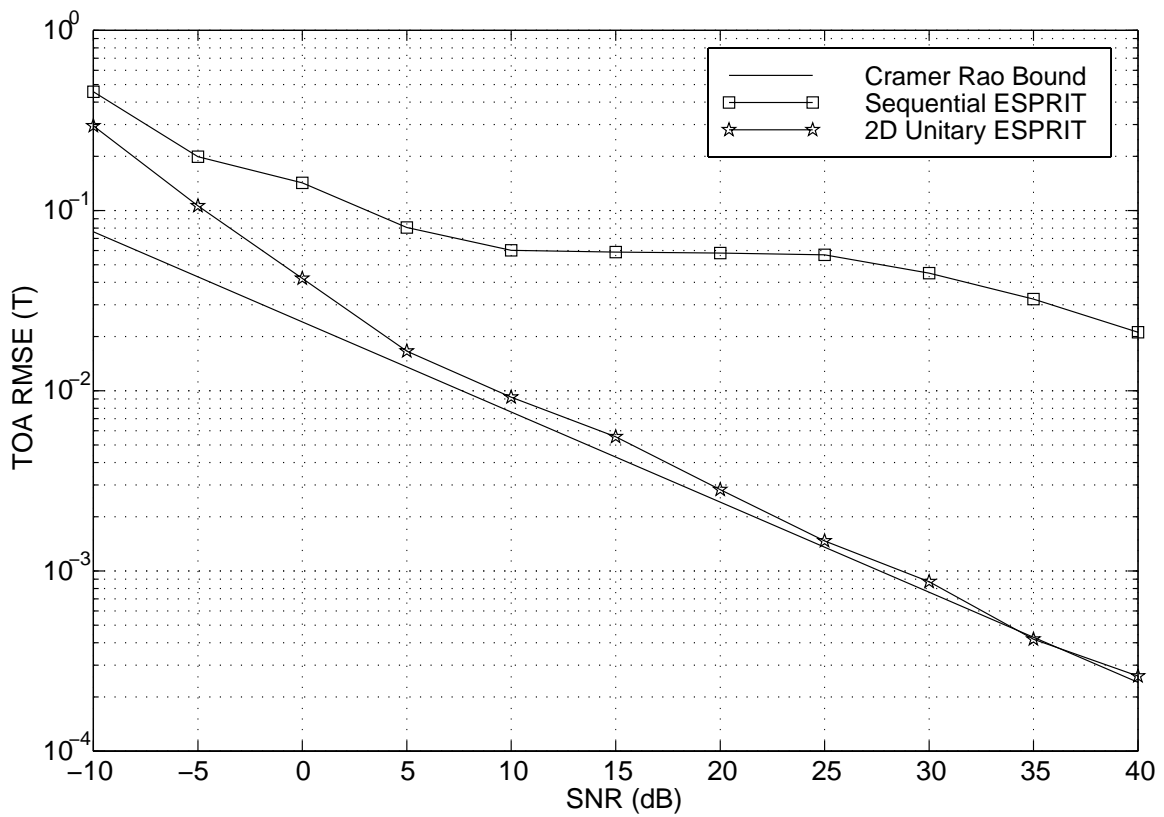
- ☞ Angle-of-arrival along columns

- ☞ Time-of-arrival along rows

- Large number of time samples → better accuracy

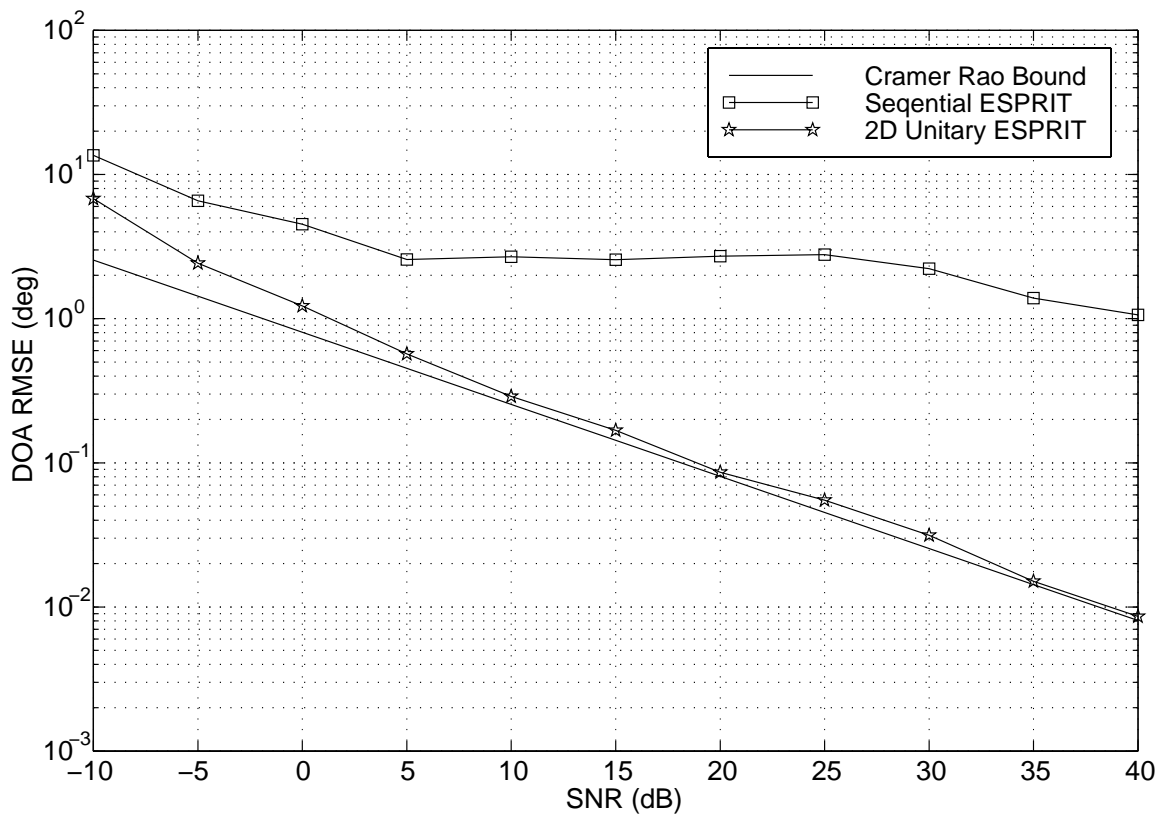
- Works in both fading and non-fading environment

# Simulation Results



Root mean square TOA error vs. SNR at the basestation

# Simulation Results



Root mean square DOA error vs. SNR at the basestation