VAlloy Virtual Functions Meet a Relational Language

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Abstract. We propose VAlloy, an extension to the first order, relational language Alloy. Alloy is suitable for modeling structural properties of object-oriented software. However, Alloy lacks support for dynamic dispatch, i.e., function invocation based on actual parameter types. VAlloy introduces virtual functions in Alloy, which enables intuitive modeling of inheritance. Models in VAlloy are automatically translated into Alloy and can be automatically checked using the existing Alloy Analyzer. We illustrate the use of VAlloy by modeling object equality, such as in Java. We also give specifications for a part of the Java Collections Framework.

1 Introduction

Object-oriented design and object-oriented programming have become predominant software methodologies. An essential feature of object-oriented languages is *inheritance*. It allows a (sub)class to inherit variables and methods from superclasses. Some languages, such as Java, only support single inheritance for classes.

Subclasses can override some methods, changing the behavior inherited from superclasses. We use C++ term virtual functions to refer to methods that can be overridden. Virtual functions are dynamically dispatched—the actual function to invoke is selected based on the dynamic types of parameters. Java only supports single dynamic dispatch, i.e., the function is selected based only on the type of the receiver object.

Alloy [6] is a first order, declarative language based on relations. Alloy is suitable for specifying structural properties of software. Alloy *specifications* can be analyzed automatically using the Alloy Analyzer (AA) [5]. Given a finite *scope* for a specification, AA translates it into a propositional formula and uses SAT solving technology to generate *instances* that satisfy the properties expressed in the specification.

Alloy supports some features of object-oriented design. However, Alloy does not have built in support for dynamic dispatch. Recently, Jackson and Fekete [4] presented an approach for modeling parts of Java in Alloy, pointing out that modeling "the notion of equality is problematic".

In Java, the equals method, which allows comparing object values, as opposed to using the '==' operator, which compares object identities, is overridden in majority of classes. Good programming methodology suggests that equals be overridden in all immutable classes [19]. This method is pervasively used, for example in the Java Collections Framework [17] for comparing elements of collections. Any equals method must satisfy a set of properties, such as implementing an equivalence relation; otherwise, the collections do not behave as expected. However, getting equals methods right is surprisingly hard.

We present VAlloy, an extension to Alloy that enables intuitive modeling of dynamic dispatch. VAlloy introduces in Alloy virtual functions and related inheritance constructs. We give VAlloy a formal semantics through a translation to Alloy. The translation is similar to compilation of object-oriented languages, involving creation of virtual function tables. Since VAlloy models can be automatically translated to Alloy, they can also be automatically analyzed using the existing AA.

Having an easy way to model dynamic dispatch is important for several reasons. First, it enables automatic analysis of models of overridden methods. Second, it allows modeling comparisons based on object values and developing specifications for collections that use these comparisons, such as Java collections. Third, such specifications can be used to test the actual implementations, for example using the TestEra framework [12].

The rest of this paper is organized as follows. Section 2 gives an example that illustrates the key constructs of VAlloy. Section 3 defines a semantics for VAlloy through a translation to Alloy. Section 4 presents VAlloy specifications that partially model Java-like collections. Section 5 reviews related work. Section 6 discusses future work, and Section 7 presents our conclusions.

2 Example

We illustrate VAlloy by modeling and analyzing an (in)correct overriding of the equals method in Java. We first develop an Alloy specification that contains only one equals method, and then describe challenges that arise in modeling method overriding. Finally, we present how VAlloy tackles these challenges.

2.1 Modeling equals in Alloy

Consider the following equals method that appears in java.awt.Dimension in the standard Java libraries [17]:

```
class Dimension {
    int width;
    int height;
    public boolean equals(Object obj) {
        if (!(obj instanceof Dimension))
            return false;
        Dimension d = (Dimension)obj;
        return (width == d.width) && (height == d.height);
    }
}
```

We develop in Alloy (not yet VAlloy) a specification for the above method. An Alloy specification consists of a sequence of paragraphs that either introduce an *uninterpreted type* or express constraints over the types. We start with the following declarations:

```
sig Object {} // java.lang.Object
sig Dimension extends Object { // java.awt.Dimension
width: Integer,
height: Integer
}
```

Each *signature*, introduced by the keyword sig, denotes a set of atomic individuals. In this specification, atoms in sig Object model Java objects. The signature Dimension is declared it to be a subset of Object. Alloy subsets model Java subclassing with typing rules being as follows.

Signatures declared without extends are *basic* signatures. Basic signatures are disjoint from one another and represent Alloy types. Subsets do not introduce new Alloy types. The type of an atom is the basic signature it belongs to; all atoms in the above specification, including those in Dimension, have Alloy type Object. We can reconstruct Java type, i.e., class, of modeled Java objects based on their (sub)set membership.

Fields width and height introduce relations between Dimension atoms and Integer atoms, where Integer is predefined in Alloy. More precisely, each field introduces a function that maps Dimension atoms to Integer atoms.

We next add to the specification a model of the above equals method:

```
fun Dimension::equals(obj: Object) {
   obj in Dimension // instanceof
   this.width = obj.width && this.height = obj.height
}
```

The Alloy *function* equals records constraints that can be invoked elsewhere in the specification. This function has two arguments: obj and the implicit this argument, introduced with '::'. The function body constrains obj to be an atom of Dimension, effectively modeling Java's instanceof. This constraint is conjoined with the other that requires the fields to be the same. However, the above declaration does not constrain this to be an atom of Dimension; the declaration is equivalent to fun Object::equals(obj: Object).

We next use the Alloy Analyzer (AA) to automatically check properties of the above specification. Each equals method should satisfy a set of properties: implement an equivalence relation and be consistent with hashCode [17]. The following Alloy assertion requires the function equals, which models the method equals, to be an equivalence relation:

The operator '..' invokes Alloy functions (using static resolution). AA checks the above assertion and reports that there are no counterexamples.

2.2 Overriding

Consider Dimension3D, a subclass of java.awt.Dimension that adds a field depth and overrides equals:

```
class Dimension3D extends java.awt.Dimension {
    int depth;
    boolean equals(Object obj) {
        if (!(obj instanceof Dimension3D))
            return false;
        Dimension3D d = (Dimension3D)obj;
        return super.equals(obj) && depth = d.depth;
    }
}
```

In order to check the equals method in Dimension3D, we would like to add the following to the Alloy specification presented so far:

```
sig Dimension3D extends Dimension {
   depth: Integer
}
// duplicate function names are NOT allowed in Alloy
fun Dimension3D::equals(obj: Object) {
   obj in Dimension3D
   // super.equals needs to be inlined because
   // there is no built in support for super
   this.width = obj.width && this.height = obj.height
   this.depth = obj.depth
}
```

However, this does not produce the intended model of overriding. In fact, this is not even a legal Alloy specification—each Alloy specification must have unique function names.¹ We could try renaming one of the equals functions, but it does not directly solve the problem of modeling overriding. Namely, the invocations o..equals(o') should choose the function based on the Java type/class of o. Since Alloy has no built in support for dynamic dispatch, we would need to model it manually for each function. Instead, we propose that it be done automatically.

2.3 Modeling equals in VAlloy

VAlloy introduces a natural way to model dynamic dispatch in Alloy. The following VAlloy specification models the above Java classes:

```
class Object {}
virtual fun Object::equals(obj: Object) { this = obj }
class Dimension {
  width: Integer,
 height: Integer
virtual fun Dimension::equals(obj: Object) {
  obi in Dimension
  this.width = obj.width && this.height = obj.height
7
class Dimension3D extends Dimension {
 depth: Integer
}
virtual fun Dimension3D::equals(obj: Object) {
 obj in Dimension3D
  super..equals(obj) && this.depth = obj.depth
}
```

 $^{^{1}}$ That is why we do not initially add equals function for <code>Object</code>.

The class declaration in VAlloy corresponds to the Alloy declaration disj sig, where disj indicates that the declared subset is disjoint from other disj subsets of its parent set. As in Java, VAlloy classes by default extend Object.

The virtual function modifier² is the main VAlloy extension to Alloy. This modifier declares a function that is dynamically dispatched at invocation, based on the VAlloy class of the receiver. VAlloy allows virtual functions to have the same name. The above example also shows the keyword super that VAlloy provides for modeling super as found in Java.

2.4 Checking VAlloy specifications

Every VAlloy specification can be automatically translated into an Alloy specification. Section 3 presents the translation and the resulting Alloy specification for our running example.³

We use AA to automatically check the above assertion equalsIsEquivalence. Note that the invocations in the assertion do not need to change; the translation properly models dynamic dispatch. AA generates a counterexample:

```
Object_2: Dimension3D {
  width = 0,
  height = 1,
  depth = 3
}
Object_1: Dimension {
  width = 0,
  height = 1
}
```

These two objects violate the symmetry property: Object_1..equals(Object_2), but *not* Object_2..equals(Object_1). This is because equals of Dimension is oblivious of the field depth declared in Dimension3D. This counterexample shows that it is hard to extend the java.awt.Dimension class and preserve the properties of equals.

A way to provide an overridable implementation of equals in Java is to use the getClass method instead of the instanceof primitive [14]. In the running example, it requires changing equals of java.awt.Dimension to use the expression obj.getClass() == this.getClass() instead of obj instanceof Dimension. A similar change should be made in Dimension3D, unless it is declared final, and therefore cannot be extended.

Modeling this change in VAlloy is straightforward: change obj in Dimension with obj..getClass() = this..getClass() in the function Dimension::equals. VAlloy provides the function getClass that models the final method getClass from the class java.lang.Object. We translate the changed VAlloy specification into Alloy and again use AA to check the equivalence assertion. This time AA reports that there are no counterexamples.

 $^{^2}$ VAlloy borrows the modifier name from C++.

³ We have not yet implemented the translation; we perform it manually.

3 VAlloy

This section presents VAlloy as an extension to Alloy. We define a formal semantics for VAlloy by giving a translation of VAlloy specifications to Alloy specifications. Details of Alloy semantics can be found in [6].

VAlloy adds the following to Alloy:

- virtual function modifier that declares a function whose invocation depends on the class of the receiver;
- · class declaration that introduces VAlloy classes;
- super keyword that directly correspond to Java;
- getClass function that corresponds to the getClass method of the class java.lang.Object.

These constructs are syntactically added to Alloy in the obvious way.

3.1 Translation Example

We give a semantics to the new constructs through a translation into Alloy. The translation algorithm operates in six steps, which we first describe through examples. Figures 1 and 2 show the Java code and VAlloy specification from Section 2. For this example, the translation proceeds as follows.

Step 1. Compute the hierarchy of class declarations:

```
Object
+-- Dimension
+-- Dimension3D
```

Step 2. Construct sig Class and sig Object based on the above hierarchy:

Atoms in Class and the *fact* Hierarchy represent the VAlloy class declarations. (A fact in Alloy expresses constraints that must hold for all instances of the specification.) For each atom c in Class, c.ext gives the Class atom that corresponds to the superclass of c.⁴ The keyword static constraints each of the

⁴ For simplicity, we only present single inheritance, where the hierarchy can only be a tree. In multiple inheritance, each class can have a set of superclasses.

```
class Object {
    boolean equals(obj: Object) {
                                                sig Class { ext: option Class }
        return this == obj;
                                                static part sig
   }
                                                  Object_Class, Dimension_Class,
                                                  Dimension3D_Class extends Class {}
class Dimension {
                                                fact Hierarchy {
    int width:
                                                  no Object_Class.ext
    int height;
                                                    Dimension_Class.ext = Object_Class
    boolean equals(obj: Object) {
                                                      Dimension3D_Class.ext = Dimension_Class
        if (obj.getClass() != this.getClass())
                                               1
            return false;
                                                sig Object { class: Class }
        Dimension d = (Dimension)obj;
                                                fact ObjectClasses {
        return width == d.width &&
                                                  (Object - Dimension).class = Object_Class
               height == d.height;
                                                    (Dimension - Dimension3D).class =
   }
                                                       Dimension_Class
                                                      Dimension3D.class = Dimension3D Class
class Dimension3D extends Dimension {
                                                3
    int depth:
                                                fun Object::getClass(): Class {
    boolean equals(obj: Object) {
                                                  result = this.class
        if (obj.getClass() != this.getClass())
                                               1
           return false:
                                                fun Object::equals(obj: Object) {
        Dimension3d d = (Dimension3d)obj;
                                                  this.class = Object_Class =>
        return super.equals(obj) &&
                                                  this..Object_equals(obj)
               depth == d.depth;
                                                    this.class = Dimension_Class =>
   }
                                                    this..Dimension_equals(obj)
}
                                                      this.class = Dimension3D_Class =>
                                                      this..Dimension3D_equals(obj)
             Fig. 1. Java code
                                                7
                                                fun Object::Object_equals(obj: Object) {
class Object {}
                                                  this = obj
                                                r
virtual fun Object::equals(obj: Object) {
 this = obj
3
                                                disj sig Dimension extends Object {
                                                  width: Integer,
class Dimension {
                                                  height: Integer
  width: Integer,
                                                3
 height: Integer
                                                fun Object::Dimension_equals(obj: Object) {
                                                  obj..getClass() = this..getClass()
virtual fun Dimension::equals(obj: Object) {
                                                  this.width = obj.width
  obj..getClass() = this..getClass()
                                                  this.height = obj.height
                                                7
  this.width = obj.width
  this.height = obj.height
                                                disj sig Dimension3D extends Dimension {
class Dimension3D extends Dimension {
                                                  depth: Integer
                                                7
 depth: Integer
                                                fun Object::Dimension3D_equals(obj: Object) {
virtual fun Dimension3D::equals(obj: Object) {
                                                  obj..getClass() = this..getClass()
  obj..getClass() = this..getClass()
                                                  this..Dimension_equals(obj)
  super..equals(obj)
                                                  this.depth = obj.depth
  this.depth = obj.depth
                                                }
                                                assert equalsIsEquivalence {
                                                  all o: Object |
assert equalsIsEquivalence {
                                                                             // reflexivity
  all o: Object |
                             // reflexivity
                                                    o..equals(o)
                                                  all o1, o2: Object |
                                                                             // symmetry
   o..equals(o)
                                                    o1..equals(o2) => o2..equals(o1)
  all o1, o2: Object |
                             // symmetry
   o1..equals(o2) => o2..equals(o1)
                                                  all o1, o2, o3: Object |
                                                                            // transitivity
                                                    o1..equals(o2) && o2..equals(o3) =>
  all o1, o2, o3: Object | // transitivity
   o1..equals(o2) && o2..equals(o3) =>
                                                    o1..equals(o3)
                                                }
   o1..equals(o3)
3
                                                   Fig. 3. Translated Alloy specification
        Fig. 2. VAlloy specification
```

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declared subsets to contain exactly one atom, and the keyword **part** declares a partition—the subsets are disjoint and their union is the whole set.

For each atom o in Object, o.class gives the corresponding Class atom. This correspondence is set with fact ObjectClasses based on the VAlloy class hierarchy. (The '-' operator denotes set difference in Alloy.) This translation step also introduces the function getClass.

Step 3. Change class declarations into disj sig declarations, adding extends Object where required:

```
disj sig Dimension extends Object { ... }
disj sig Dimension3D extends Dimension { ... }
```

This step does not change field declarations.⁵

Step 4. Rename each virtual function so that all functions in the specification have unique names:

```
fun Object::Object_equals(obj: Object) { this = obj }
fun Object::Dimension_equals(obj: Object) { ... }
fun Object::Dimension3D_equals(obj: Object) { ... }
```

This step also removes the modifier virtual, translating dynamically dispatched VAlloy functions into statically dispatched Alloy functions.

Step 5. Add, for each overridden function name, a *dispatching* function, i.e., a new Alloy function that models dynamic dispatch:

```
fun Object::equals(obj: Object) {
  this.class = Object_Class =>
  this..Object_equals(obj)
    this.class = Dimension_Class =>
    this..Dimension_equals(obj)
    this.class = Dimension3D_Class =>
    this..Dimension3D_equals(obj)
}
```

This step is the crux of the translation. It allows function invocations in VAlloy to be written in the usual Alloy notation, but it models dynamic dispatch semantics—the actual function is selected based on the class of the receiver.

Step 6. Replace each invocation on **super** with an invocation to the corresponding, previously renamed, static function:

```
fun Object::Dimension3D_equals(obj: Object) {
   obj..getClass() = this..getClass()
   this..Dimension_equals(obj) && this.depth = obj.depth
}
```

This completes the translation. Figure 3 shows the full resulting Alloy specification. Note that the translation does not change the assertion; the invocations o..equals(o') remain written in the most intuitive manner, but they have dynamic dispatch semantics.

⁵ For simplicity, we do not present modeling null, which would require slightly changing field declarations.

3.2 General class hierarchy

To illustrate the general translation of **class** hierarchy, consider the following excerpt from a VAlloy specification:

```
class 0 {} virtual fun 0::hC() { /*0*/ }
class C extends 0 {} virtual fun C::hC() { /*0*/ }
class C1 extends C {} // C1 does not define fun hC
class C2 extends C {} virtual fun C2::hC() { /*C2*/ }
class D extends 0 {} // D does not define fun hC
class D1 extends D {} virtual fun D1::hC() { /*D1*/ }
```

For this hierarchy, the translation generates the following sig Class and sig Object:

```
sig Class { ext: option Class }
static part sig O_Class, C_Class, C1_Class, C2_Class,
                 D_Class, D1_Class extends Class {}
fact Hierarchy {
 no O_Class.ext
    C_Class.ext = O_Class
      C1_Class.ext = C_Class
      C2_Class.ext = C_Class
    D_Class.ext = O_Class
      D1_Class.ext = D_Class
}
sig Object { class: Class }
fact ObjectClasses {
  (O - C - D).class = O_Class
(C - C1 - C2).class = C_Class
      C1.class = C1_Class
C2.class = C2_Class
    (D - D1).class = D_Class
      D1.class = D1 Class
}
```

For the function hC, the translation generates the following Alloy functions:

```
fun 0::0_hC() { /*0*/ }
fun 0::C_hC() { /*C*/ }
// there is no 0::C1_hC()
fun 0::C2_hC() { /*C2*/ }
// there is no 0::D_hC()
fun 0::D1_hC() { /*D1*/ }
fun 0::hC() {
    this.class = 0_Class => this..0_hC()
        this.class = C1_Class => this..C_hC()
        this.class = C2_Class => this..C_hC() /* not C1 */
        this.class = D_Class => this..0_hC()
        this.class = D_Class => this..0_hC()
        this.class = D_Class => this..0_hC()
        this.class = D_Class => this..0_hC() /* not D */
        this.class = D_1Class => this..D1_hC()
}
```

3.3 Summary

To summarize, the translation from VAlloy to Alloy proceeds in the following six steps:

- 1. Compute the hierarchy of class declarations.
- 2. Construct sig Class and sig Object.
- 3. Change class into disj sig declarations.
- 4. Rename uniquely each virtual function.
- 5. Add dispatching functions.
- 6. Replace super with an appropriate static invocation.

4 Collections

This section presents VAlloy models for some collection classes. Our main focus is comparison based on object values. We ignore the orthogonal issue of modeling state, i.e., sharing and object interactions. An approach for modeling state in Alloy is discussed in [4], and we can apply the same approach to VAlloy.

4.1 Sets

We develop a VAlloy specification for sets whose membership is based on object values, not object identities. As in Java, elements of the sets are objects of classes that (in)directly extend Object and potentially override equals.

We first declare a VAlloy class for sets:

```
class Set { s: set Object }
```

For each atom a in Set, a.s is the (Alloy) set of objects in the (modeled) set a. To constrain set membership to be based on object values, we introduce the following fact:

```
fact SetIsBasedOnEquals {
    all a: Set | all disj e1, e2: a.s | !e1..equals(e2)
}
```

This fact requires distinct elements in each set to be not equal with respect to equals. For example, this rules out the set a such that a.s={d1,d2}, where d1 and d2 are distinct atoms (i.e., d1!=d2) of Dimension, but d1.width=3, d1.height=8 and also d2.width=3, d2.height=8, which makes d1..equals(d2). Note that a.s is a valid Alloy set.

It is now easy to specify some set functions from the java.util.Set interface:

```
virtual fun Set::contains(o: Object) {
 some e: this.s | o..equals(e)
3
virtual fun Set::add(o: Object): Set {
 this.s..contains(o) =>
   result.s = this.s.
   result.s = this.s + o
3
virtual fun Set::remove(o: Object): Set {
 result.s = this.s - { e: this.s | e..equals(o) }
}
virtual fun Set::isEmpty() { no this.s }
virtual fun Set::clear(): Set { no result.s }
virtual fun Set::size(): Integer { result = #this.s }
virtual fun Set::subset(a: Set) {
 all e: this.s | a..contains(e)
3
virtual fun Set::equals(o: Object) {
 o in Set
  o..size() = this..size()
  o..subset(this)
3
```

The most interesting function is equals, which compares two sets for equality. It checks that both sets have the same number of elements and that o is a subset (based on equals) of this. The function remove uses set comprehension to specify an object's removal from a set.

The above VAlloy specification closely models java.util.Set. The main difference is that this specification is written in a functional style and does not model state modifications. As mentioned, state can be modeled using the approach from [4], which also presents a way to handle iterators. Therefore, we do not model "bulk operations" on sets, such as addAll, based on iterators. Instead, we present an analogous function for set union:

```
virtual fun Set::union(a: Set): Set {
   this..subset(result)
   a..subset(result)
   all e: result.s | this..contains(e) || a..contains(e)
}
```

Note that the use of contains (and subset based on contains), which is based on equals, enables specifying union in a direct way.

4.2 Maps

We next develop a partial VAlloy specification for maps, such as java.util.Map, that compare keys based on equals. In this specification, we reuse the class Set defined above to automatically constrain the set of keys:

```
class Map {
  keys: Set
  map: keys.s ->! Object
}
```

We model the mapping from keys to values using an Alloy relation map; the *multiplicity marking* '!' indicates that for each key, there is exactly one Object. For each atom a in class Map, a.map is the actual mapping. For a key k, a.map[k] gives the value that k is mapped to in map a.

We next model the essential map functions:

```
virtual fun Map::get(key: Object): Object {
   this.keys..contains(key) => result = this.map[key]
}
virtual fun Map::put(key: Object, value: Object): Map {
   result.keys = (this.key - { e: this.keys | e..equals(key) }) + key,
   result.map = (this.map - { e: this.keys | e..equals(key) }->Object) + key->value
}
```

The function get returns the value that key is mapped to, if such a key exists in the map; otherwise, the behavior of get is unspecified. (Since Alloy is a relational language, non-determinism comes for free.) We can constrain get to be deterministic, e.g., to return an explicit Null object, if the key is not in the map.

4.3 Trees

We next use a tree-based implementation of sets to illustrate how properties of abstract data types can be expressed in VAlloy. Consider the following declaration for binary trees:

```
class Tree { root: Node }
class Node {
    left: Node,
    right: Node,
    data: Object
}
```

Suppose that these VAlloy trees model a Java implementation of sets based on equals. We can state the *abstraction function* [19] for these trees in VAlloy:

```
fun Tree::abstractionFunction(): Set {
  result.s = this.root.*(left+right).data
}
```

The '*' operator is reflexive transitive closure, and root.*(left+right) denotes an (Alloy) set of all Nodes reachable from the root. The set of Objects from those nodes is obtained accessing data, and the abstraction function constrains this Alloy set to be a Set.

We also use VAlloy to state *representation invariant* [19] for these trees. Assume that they have the following structural constraints: root nodes are sentinels (and thus never null) and leaf nodes point to themselves. The following repOk predicate characterizes the representation invariants for a tree:

```
fun Tree::repOk() {
    // no node points to root
    no this.root.~(left+right)
    // acyclic (with self loops for leafs)
    all n: this.root.*(left+right) {
        n.left = n || n !in n.left.*(left+right)
        n.right = n || n !in n.right.*(left+right)
    }
    // no duplicates w.r.t equals()
    some a: Set | a = this..abstractionFunction()
}
```

(The '~' operator denotes transpose of a binary Alloy relation.) Beside the structural invariants, a valid tree is required to be a concrete representation of some Set. Note how the equals constraints from the abstract representation, Set, propagate to the concrete representation, Tree.

5 Related work

Recently, Jackson and Fekete [4] proposed an approach for modeling in Alloy object interactions, like those in Java. Their approach models heap using explicit references and captures properties of object sharing and aliasing. However, the approach does not handle inheritance in the presence of method overriding and dynamic dispatch. Their approach is orthogonal to our handling of virtual functions; we are planning to combine these two approaches.

Alloy has been used to check properties of programs that manipulate dynamic data structures. Jackson and Vaziri [7] developed a technique for analyzing bounded segments of procedures that manipulate linked lists. Their technique automatically builds an Alloy model of computation and checks it against a specification. They consider a small subset of Java, without dynamic dispatch.

We developed TestEra [12], a framework for automated testing of Java programs. In TestEra, specifications are written in Alloy and the Alloy Analyzer is used to provide automatic test case generation and correctness evaluation of programs. Writing specifications for Java collections, which use comparisons based on object values, requires modeling the equals method in Alloy. This led us to tackle modeling general Java-like inheritance in Alloy. VAlloy presents some ideas toward that goal.

The Java Modeling Language (JML) [10] is a popular specification language for Java. JML assertions use Java syntax and semantics, with some additional constructs, most notably for quantification. Leveraging on Java, JML specifications can obviously express dynamic dispatch. However, JML lacks static tools for automatic verification of such specifications.

The LOOP project [18] models inheritance in higher order logic to reason about Java classes. Java classes and their JML specifications are compiled into logical theories in higher order logic. A theorem prover is used to verify the desired properties. This framework has been used to verify that the methods of java.util.Vector maintain the safety property that the actual size of a vector is less than or equal to its capacity [3].

Object-oriented paradigm has been integrated into many existing languages, typically to make reuse easier. For example, Object-Z [15] extends the Z specification language [16], which enables building specifications in an object-oriented style. Object-Z retains the syntax and semantics of Z, adding new constructs. The major new construct is the class schema that captures the object-oriented notion of a class. Object-Z allows inheritance to be modeled, but it lacks tool support for automatically analyzing specifications.

Objects and inheritance have also been added to declarative languages. For example, Prolog++ [13] extends Prolog. OOLP+ [1] aims to integrate objectoriented paradigm with logic programming by translating OOLP+ code into Prolog without meta-interpretation.

Keidar et al. [8] add inheritance to the IOA language [11] for modeling state machines, which enables reusing simulation proofs between state machines. This approach allows only a limited form of inheritance, subclassing for extension: subclasses can add new methods and *specialize* inherited methods, but they cannot override those inherited methods, changing their behavior arbitrarily. VAlloy allows subclasses to arbitrarily change the behavior of inherited methods.

6 Future work

VAlloy presents our first step towards modeling in Alloy advanced constructs from object-oriented languages. The main focus has been on method overriding in Java. We have therefore designed VAlloy to support subclasses that can arbitrarily change behavior of inherited methods.

Our approach can easily be extended to support intuitive modeling of multiple inheritance, such as in C++, and multi-method dispatch, such as in Cecil. Support for method overloading can clearly be added through a simple syntactic manipulation. We omitted support for Java's interfaces, keeping in line with Alloy's "micromodularity" philosophy of being a lightweight language amenable to fully automatic analysis. Similarly, we do not consider encapsulation.

We would like to explore modeling in VAlloy other constructs of Java. Initially, we plan to add state to VAlloy, adapting the approach of [4], or maybe

TAlloy [9]. We also want to add support for exceptions to enable VAlloy specifications to directly model exceptional behavior of methods, as well as normal behavior. Further, having exceptions would allow modeling arrays with bound checking. We are also evaluating whether VAlloy specifications should include computation, such as control flow, recursion, and multi-threading.

To explore practical value of VAlloy, we intend to use it in connection with some existing frameworks. Daikon [2] is a tool for dynamically detecting likely program invariants; we are considering to use it to detect (partial) VAlloy specifications of Java classes. TestEra [12] is a framework for automated test generation and correctness evaluation of Java classes; we are considering to use VAlloy specifications for TestEra.

7 Conclusions

We described VAlloy, an extension to the first order, relational language Alloy. All function invocations in Alloy are static; Alloy has no direct support for dynamic dispatch. VAlloy introduces virtual functions in Alloy, which enables intuitive modeling of inheritance, such as that of Java. We illustrated the use of VAlloy by modeling a small part of the Java Collections Framework.

We defined a formal semantics for VAlloy through a translation to Alloy. VAlloy models can be automatically translated into Alloy. The translation is similar to building virtual function tables for object-oriented languages and can benefit from optimizations based on class hierarchy. The translated specifications can be automatically checked using the existing Alloy Analyzer. We believe that VAlloy can be effectively used for specification and checking of Java classes.

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