DG Tech Notes on reliability EE394JD It is often claimed that microgrids can provide a more reliable power supply than the goid. To study whether or not this statement is true we need to inderstand some basic concepts of reliability theory theory let's consider first that we are studying a particular device or component of a system Reliability is the probability that a item will operate without failure for a stated period of the Inder specified conditions Since relizedility is a probability it can only take values between 0 and 1. We identify the selicity of on item with R. The complement of the reliability is the unreliability F. F = 1 - RUnrelidoility ______ It's the probability that a coport/mpt intsval The use of the words "without failure" in the definition of reliability or the term " continuously" in the definition of

Unreliability is not arbitrary. They imply that the concept of reliability can only be applied directly to Systems of repairable items. The terms that consider a system's of a repairable item's behaviour innormal operation and after a failure are availability and un availability" and un evailability" The form "ovailability" conserved in different senses defending on the type of system or item 1) Availabil; to(A) is the probability that a system/item works on demand -> Definition appropriate for 2) Availzbility (AGH) is the probability that a system like is working at a specific the t -> Definition appropriate for continuous by operating systems 3) Availability (A) is the expected portion of the time that a system or item performs its required centron Depuision appropriate for repairable systems On avaliability - It is the probability that a system or ita." SVa does not operate at a the t A = 1 - Va

Simple model for system behavior State= working Repair Process Process · Reliability calculation: Fl+1= P(z given item fails in [0, t)) (1) (Locantinuous operation is implicit VIII is a probability distribution with random VERizsle t The probability density function is P(t)= d P(t) dt CHIdt= P[zgiven iten fails in (t, t+dt]) (2) then Flt) dt = Flt+dt) - Flt) os F642- [6616]d6 A hazard function hlt) is created to characterize the transition to the pailed state hit is the expected rate

Siven that"

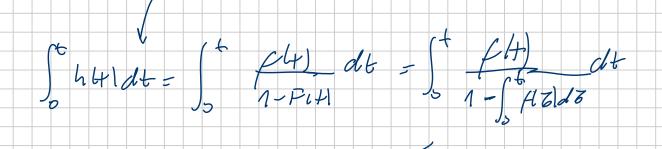
h CHIdt - P(an item pails betweent and totat / it has not pailed un til t) Since $P(\Delta/B) = P(\underline{A} \cap B)$ P(b)

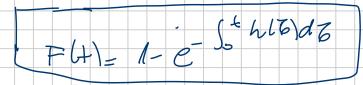
SUB) But any item that pails between t and t tot has not failed sepre so P(ANB) = P(A). Hence, but and the second second

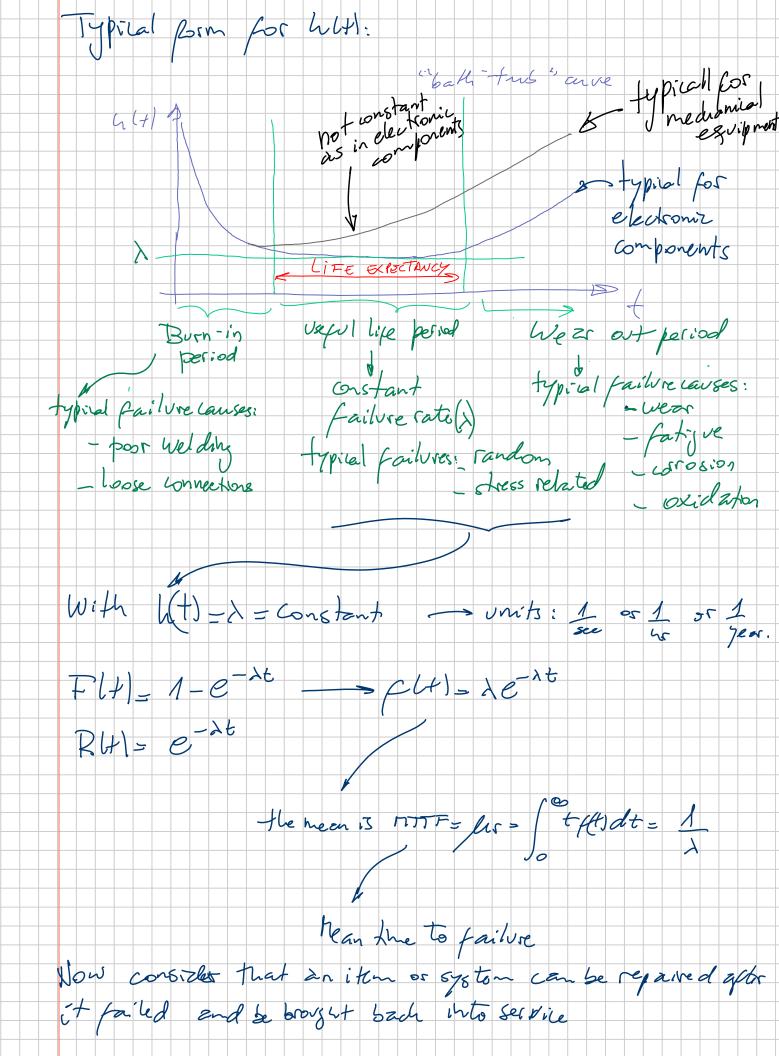
hilldt=PC component fails between t and ttdt) PC no failure in [0, t])

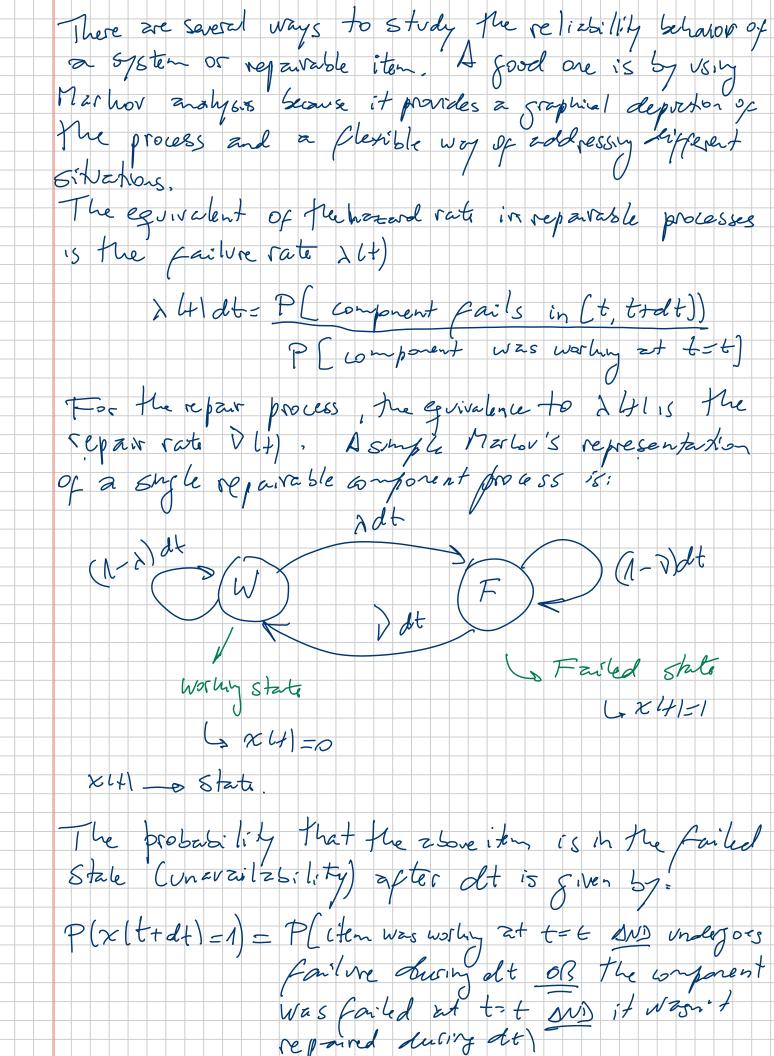
And, from (1) and (2)

 $hl+1d+ = \frac{Cl+1dt}{1-F(t)} \qquad hl+1 = \frac{F(t)}{1-F(t)}$

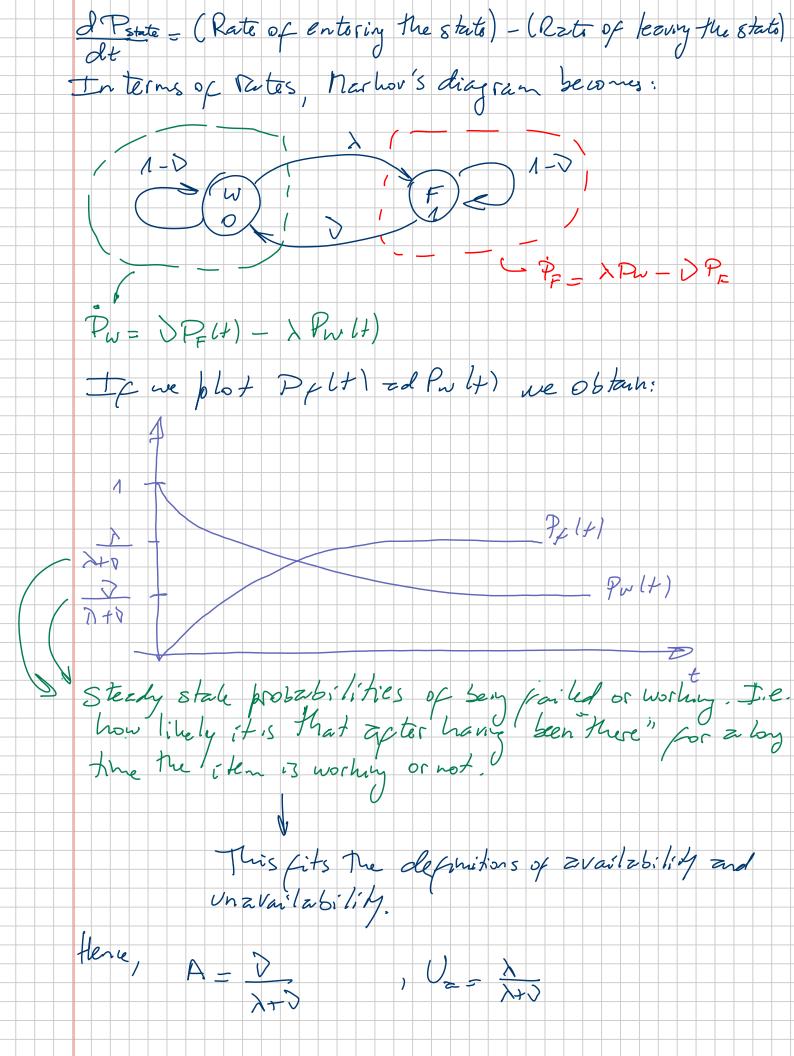


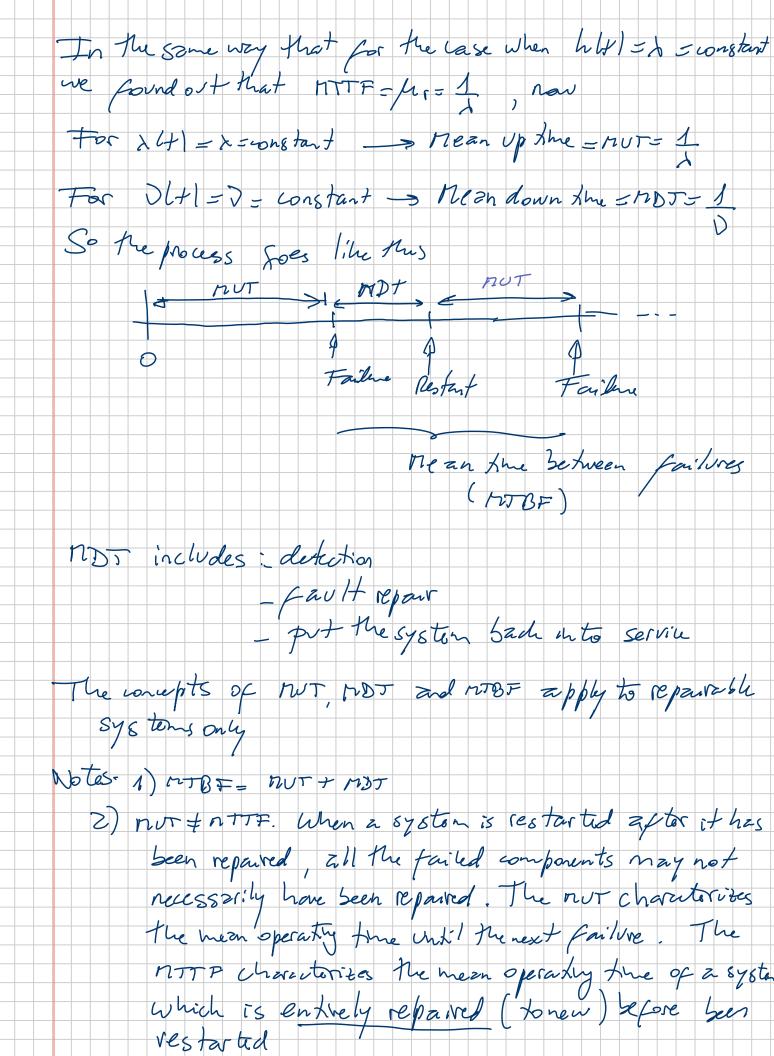


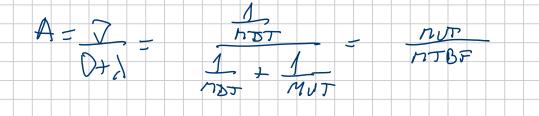




 $P(xl+rel+)=1) = P(x(+)=0) \wedge (+)dt + P(x(+)=1)(1-0)h)dt$ P(x(+)) = P(x(+)) + P(x(+)=1)(1-0)h)dt P(x(+)) + P(x(+) $P_{\mathcal{F}}(\mathcal{F}(\mathcal{A}) = \mathcal{P}_{\mathcal{N}}(\mathcal{A}) \times \mathcal{F}(\mathcal{A}) + \mathcal{P}_{\mathcal{N}}(\mathcal{A}) + \mathcal{P}_{\mathcal{N$ $\frac{P_{p}(t+dt)-P_{p}(t)}{dt}=P_{w}(t+\lambda-P_{p}(t))$ $\frac{dP_{F}(t)}{dt} = \hat{P}_{F}(t)$ $\frac{dP_{f}(t)}{dt} = \lambda P_{w}(t) - \nabla P_{f}(t)$ $\frac{dP_{f}(t)}{dt} = \lambda P_{w}(t) - \nabla P_{f}(t)$ $\frac{dP_{f}(t)}{dt} = \lambda P_{w}(t) - \nabla P_{f}(t)$ $\frac{dP_{f}(t)}{dt} = \lambda P_{w}(t) - \nabla P_{f}(t)$ $\begin{cases} d \mathcal{P}_{\mathcal{F}} = \lambda - (\lambda + \sqrt{2}) \mathcal{P}_{\mathcal{F}}(\mathcal{F}) \\ d\mathcal{F} \end{cases} \longrightarrow 1^{s+} order dif.eq.$ I 2850 me that > initial cond: Pelo =0 itwas initially nothing Assuming constant $\left| \begin{array}{c} P_{\mathcal{E}} \left(\mathcal{L} \right) = \lambda \\ \overline{\lambda \mathcal{L} \mathcal{D}} \left(\mathcal{L} - \mathcal{E} - (\overline{\lambda \mathcal{L} \mathcal{D}}) \mathcal{L} \right) \\ \end{array} \right|$ Failure and And Since Pw (+1= 1- Pe (+1) ~> repair rates $\left(\begin{array}{c}
P_{w}\left(+\right) = \Lambda \\
\lambda \neq \partial
\end{array} \left(\begin{array}{c}
0 + \lambda e^{-(\lambda \neq 0) \neq}
\end{array}\right)$ We could have reached the dif. quarters is from the pollowing property of the dizgram: 7





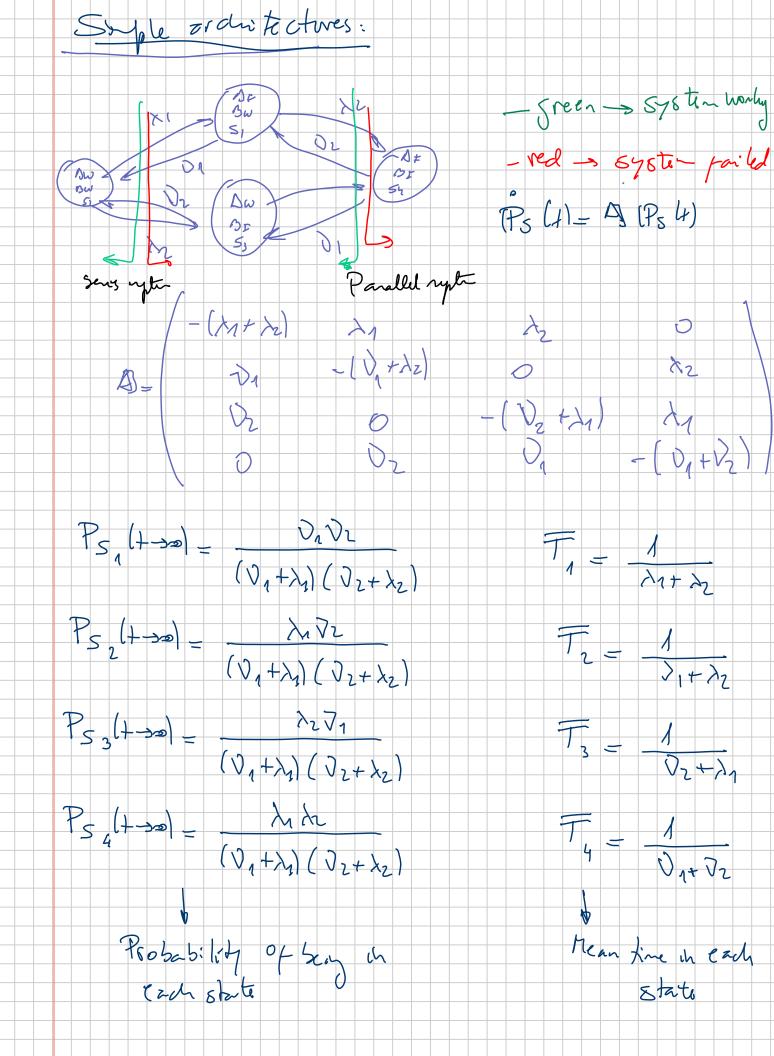


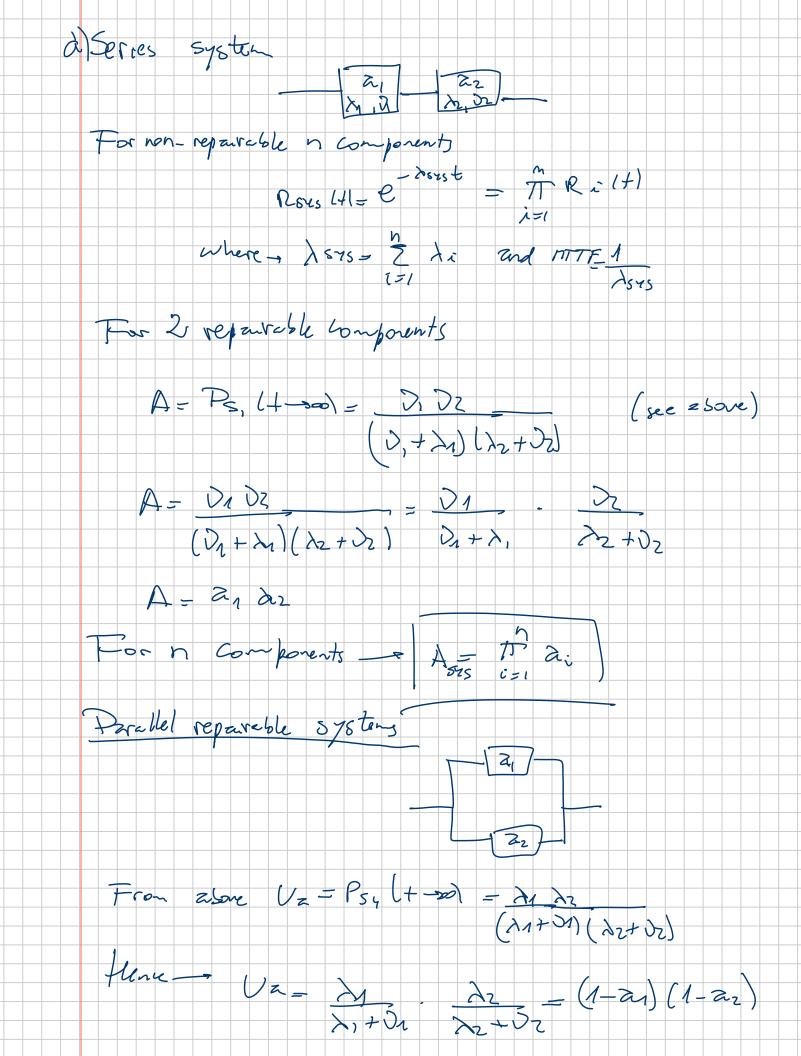
Va-MDI-

Relicbility networks is another technique to calculate availability of systems with multiple comparents.

A reliability network is a representation of the reliability dependencies between components of a system

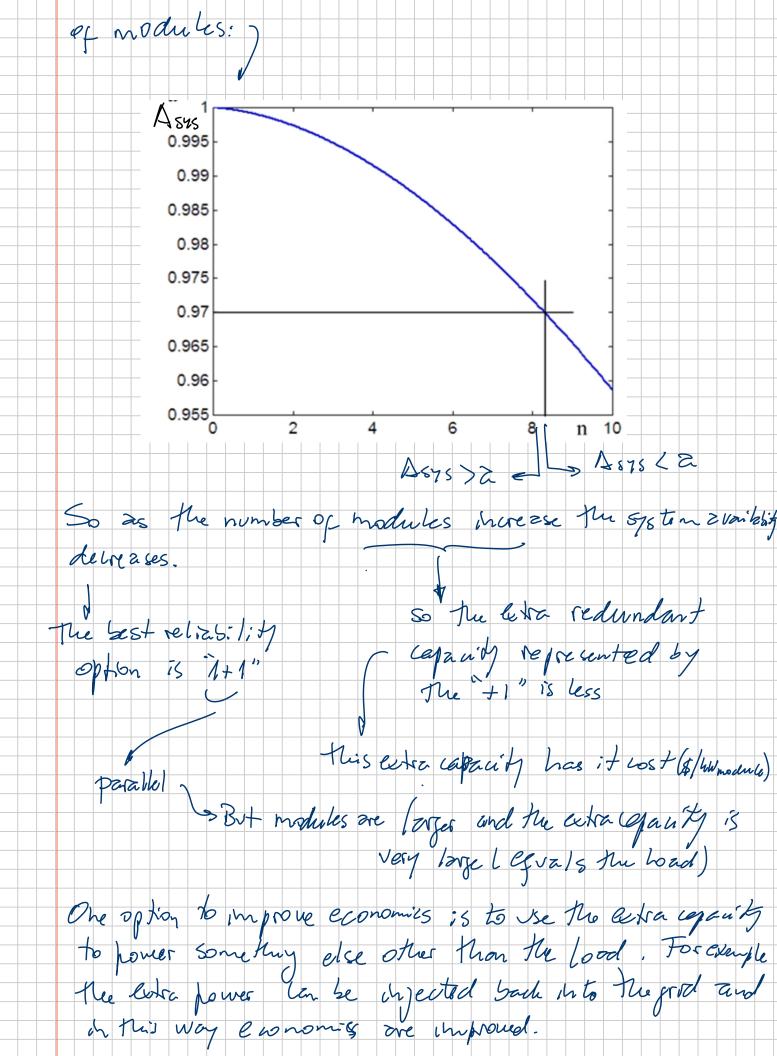
The network has always the following leatures: a) A starting node b) On Cading node c) A set of nodes d) A sot of edges O Dr miderie finition that associates each edge with an ordered pair of nodes The edges represent the components - The nodes represent system architecture The expected operating condition of the system is represented by paths though the network. As If there is at least one path from the starty node to the Endry node then the system is working > If not the syster has pailed

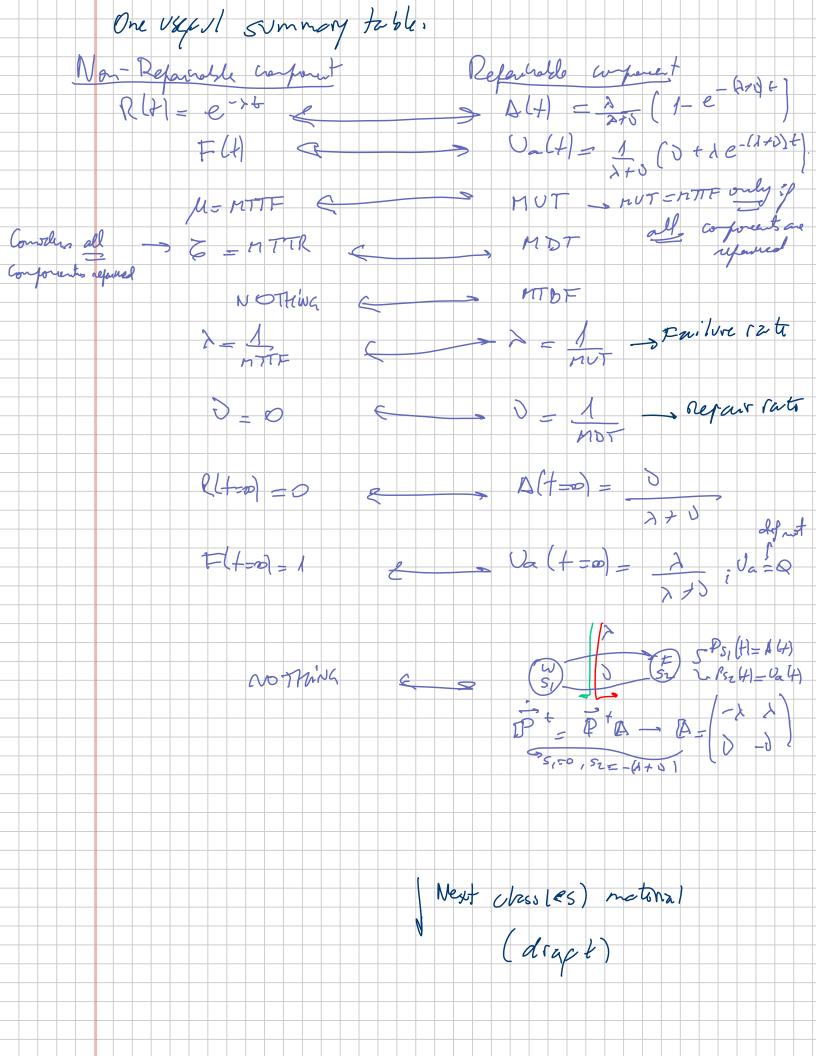


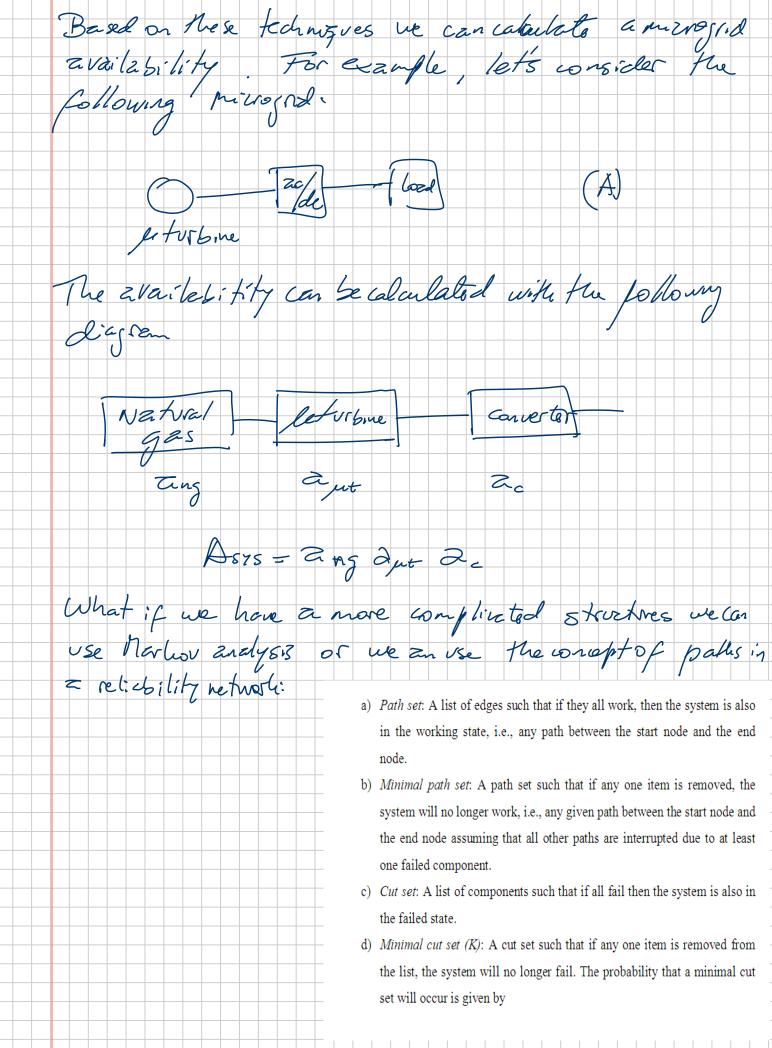


For n components in 11 $\left[\begin{array}{c} Uz_{szs} = TT \left(1 - Z_{i}\right) \right]$ n+1 redundary Suppose now that me have a mahular system with a to tat power to and each module has are rated pr Pm. Then without redundancy we need $h = \frac{P_0}{P_h}$ s The upper integer value of the point $e.s. \quad Po = 7 leW \left\{ \begin{array}{c} n & 54 \end{array} \right\}$ $Pm = 2 leW \left\{ \begin{array}{c} n & 54 \end{array} \right\}$ The problem with Ich of redundary is that if one module fails then there is not enough capacity to bruces the local power the load. With n+1 redundary we provide 1 extra module gra Those needed. Then $h = \left(\begin{array}{c} P_{-} \\ P_{-} \end{array} \right) + l$ So with not redundancy it is required that nog th not modules work for full system operation Then,

Asys = PC Systen working)= = P (n modules working) + P(n+1 modules working) = ntlon a Ma + ntlontl a ntl All possible Errangement JC AJ elements taken in Svalps of n where the order Binoniai doesh't nather to distryvish among znangements dists , buto a _ zvailability of each module Ma -> Unzurilability of Cach module > I can think of the process 25 hours on trials and requiring h or more successes for the System to work Recall that $n_{n+1} = (n+1)! = (n+1)! = n+1$ (n+1-n)!n! = n! $S_{0} A_{sys} = \left((n+1) M_{z} + a \right) a^{n} = \left((n+1) (1-a) + a \right) a^{n}$ Is (n+1) redundancy always better than other options? Consider a fuel cell with a = 0,97 and variable number







$$\mathbf{P}(K) = \prod_{i=1}^{N_k} u_i$$

where u_i is the unavailability of the *i*-th edge of the N_k components in the minimal cut set *K*.

For a system with repairable components, the unavailability can be calculated from [277]

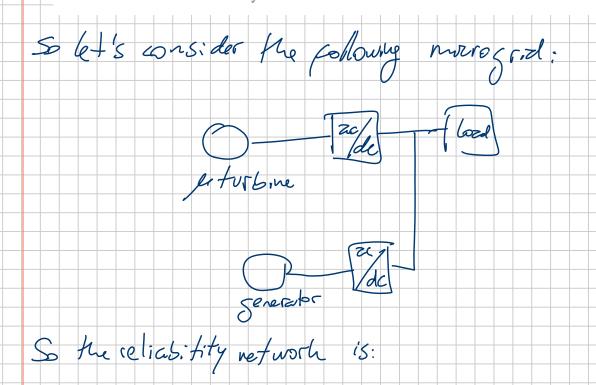
$$U = \mathbb{P}\left(\bigcup_{j=1}^{M_c} K_j\right)$$

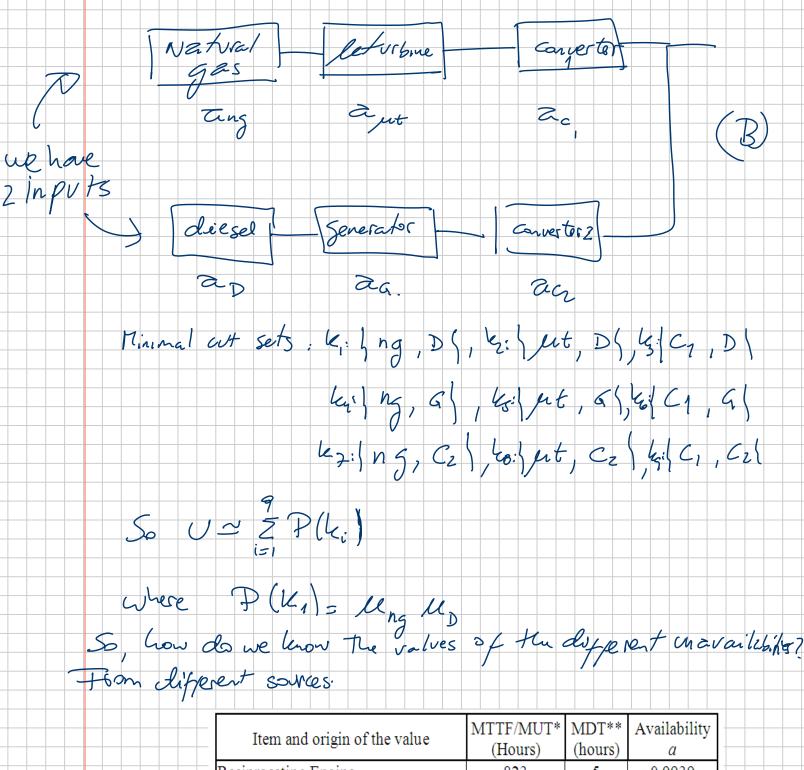
where Mc is the number of minimal cut sets in the system. Calculation of (B.6) is usually extremely tedious. However, the calculation can be simplified by recognizing that U is bounded by

$$\sum_{i=1}^{M_{e}} \mathbf{P}(K_{i}) - \sum_{i=2}^{M_{e}} \sum_{j=1}^{i-1} \mathbf{P}(K_{i} \bigcup K_{j}) \le U \le 1 - \prod_{i=1}^{M_{e}} [1 - \mathbf{P}(K_{i})] \le \sum_{i=1}^{M_{e}} \mathbf{P}(K_{i})$$

Thus, if the components are highly available, i.e., $q_i \ll 1$, then U can be approximated to

$$U \cong \sum_{j=1}^{M_c} \mathbb{P}(K_j)$$





| | (nours) | (nours) | u |
|-------------------------------------|---------|---------|----------|
| Reciprocating Engine | 823 | 5 | 0.9939 |
| PV arrays **** | 3636 | 14 | 0.996 |
| Fuel Cell (performance degradation) | 5000 | 166.6 | 0.967742 |
| Microturbine | 8000 | 50 | 0.993789 |
| Wind turbine **** | 1900 | 80 | 0.9595 |
| ac mains | 2440 | 2.08 | 0.999150 |
| Diesel / Gas | 2 M | 50 | 0.999975 |
| | | | |

*MUT: Mean up-time (used for repairable system components) **MDT: Mean down-time (only applicable to repairable components) ***NR: Not repairable

****Operational MUT and MDT depend on the actual energy availability

For the convertors we can calculate the Evailability by estimating the MDJ and by calculating the MUT-MITE $\frac{f(on)}{nTTF} = \frac{1}{2}$ where A can be calculated by considering that from a reliability perspective all components are in series. Here, The values of λ_i can be obtained from the normhal values Part Description λ_{iG} (FIT) - Fron relizbility Resistor 0.5 Information from: 1.0 Capacitor Ceramic prediction handbody Capacitor Tantalum 5.0 6.0 Diode such as klosdia J. Kippen. "Evaluating the 6.0 Transistor Reliability of DC/DC 19.0 Coil SR-237 = d Converters." Sept. 2003, 20.0 (Unfort notely no longer zvailable in Internet) MOSFET MIL-HOBU=217 IC (20 Transistors) 19.0 affected by temperative and electrical stress (e.g. white (Lvely) X = In The The The Comp Production quality ~ Usually=1 nominal value IT - temperative factor TTE _ electrical stress

-> Arrhenius rate model IT -> Temperature actor TTT = C) (Reference temporture (le - Boltzman constant 8.167.10⁻⁵ eV/4 Ea > failure activation energy > defeds on Gailure mechanin Seg. 0.6 ov Calculation of TTE: Stress Level Part Description 25% 70% 80% 0.72 1.30 1.48 Resistor 0.36 2.27 3.42 Capacitor Ceramic 0.23 3.25 5.87 Capacitor Tantalum 0.48 2.01 2.85 Diode Transistor 0.30 2.61 4.22 Coil 1.00 1.00 1.00 MOSFET 0.55 1.62 2.05 IC (25 Transistors) 1.00 1.00 1.00 1.00 1.00 1.00 IC (70 Transistors) IC (150 Transistors) 1.00 1.00 1.00 1.00 1.00 1.00 Optocoupler Final note: Fault tolerant stratogies (to avoid Single point of failines): - Redundarcy: Henry more of the minimum number of the same system components _ Diversity: Havy multiple paths Distributed systems: Spread 2 critical junction