Name:________________________________________________________________________

Problem 1 (20 points):_____

Problem 2 (15 points):_____

Problem 3 (20 points):_____

Problem 4 (20 points):_____

Problem 5 (25 points):_____

Total (100 points):_____________

Note: Please be sure that your answers to all questions (and all supporting work that is required) are contained in the space provided.

Note: Please be sure your name is recorded on each sheet of the exam.

Please read the following sentence, and if you agree, sign where requested: I have not given nor received any unauthorized help on this exam.

Signature:_____________________________________________________________________

GOOD LUCK!
Problem 1 (20 points):

Part a (5 points): When discussing out-of-order execution, some have misconstrued the notion of hazard and talked about "hazards," and in particular, "WAR Hazards." I prefer Professor Kuck's term for this: "antidependencies." Why are they not a problem and create no latency when implementing out of order execution with the Tomasulo algorithm?

Part b (5 points): In a modern microarchitecture, where 4 instructions are fetched each cycle, performance is optimized if we can maximize instruction supply. That is, no instruction supply misses, 100% branch prediction, and no packet breaks. What causes a packet break? In ten words or fewer, please.

Part c (10 points): Little Computer Inc. has a CPU that takes 3 cycles to execute a \texttt{MUL} instruction, 5 cycles to execute a \texttt{DIV} instruction, and 1 cycle to execute all other instructions. There is no pipelining. The target workload has an instruction mix containing 10\% \texttt{MUL} instructions, 10\% \texttt{DIV} instructions, and 80\% others.

Part c.i (5 points): What is the Cycles Per Instruction (CPI) of this CPU running this target workload?

Part c.ii (5 points): An improvement in the multiplier makes the \texttt{MUL} instruction take 1 cycle to execute but causes the overall cycle time to increase by 20\%. Does this new design make the workload run faster than the original CPU? Explain.
Problem 2 (15 points):

We can add predicated execution to the LC-3b using the unused opcode 1011, much like the prefixes in the x86 ISA. That is, if we wish to predicate instruction X, we put the following prefix just before instruction X in our program:

\[ \begin{array}{c}
1 & 0 & 1 & 1 & N & Z & P & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
\end{array} \]

Instruction[11:9] act in a way similar to those bits in a conditional branch instruction. In the case of a conditional branch, the branch is taken only if the condition is satisfied. In this case, instruction X is executed only if the condition is satisfied.

Whether or not instruction X is executed, we wish to preserve the condition codes so we can predicate additional instructions based on the same condition. Therefore, if instruction X is executed, it must not set condition codes. To make this work, we need to augment the data path (next page) with a flip-flop \( A \), an AND gate, and two new control signals \( \text{SETA} \) and \( \text{CLRA} \). \( \text{SETA} \) sets \( A \) to 1; \( \text{CLRA} \) sets \( A \) to 0.

The state machine for this addition is shown below. Only relevant states are shown, and some information (state numbers, and activity in a state) is missing. **Your job:** Fill in the missing information.
We augment the datapath with a new flip-flop, \( A \), and AND gate, and the control signals \( \text{CLRA} \) and \( \text{SETA} \). The changes to the datapath are in bold.
Problem 3 (20 points):

An LC-3b system has a GAg two-level adaptive branch predictor, with one modification. We index into the PHT with a vector created (like g-share) by XOR-ing the four bits of the BHR with four bits taken from the address of the current branch instruction, as follows:

\[
\begin{align*}
\text{INDEX}[3] &= \text{BHR}[3] \text{ xor } \text{PC}[10] \\
\text{INDEX}[2] &= \text{BHR}[2] \text{ xor } \text{PC}[4] \\
\text{INDEX}[1] &= \text{BHR}[1] \text{ xor } \text{PC}[3] \\
\text{INDEX}[0] &= \text{BHR}[0] \text{ xor } \text{PC}[1]
\end{align*}
\]

The rightmost bit of the BHR comes from the most recent branch. When a branch instruction is encountered, the BHR is updated with the result of the branch predictor, i.e., the \textit{speculative} (predicted) result. That result is shifted into the BHR, and the BHR is shifted one bit to the left. Information about the oldest branch is shifted out. The PHT is updated with the actual result of the branch.

(We hasten to add that when the predicted branch is actually determined, that information should replace the predicted value in the BHR. Unfortunately, this branch predictor was designed by an Aggie, and he never understood that the branch prediction is better than no information, but better still is the actual direction of the branch. So, in this problem we are stuck with the Aggie’s design, i.e., values in the BHR are always predicted values.)

Part a (6 points):
Given the snapshot of the branch predictor shown above, what is the index into the PHT?

Is the branch predicted taken or not taken?

Assume the branch is actually taken. Show the BHR after this branch is processed. Show the updated PHT entry in the column labeled PHT after as a result of this branch. It is not necessary to copy the other 15 entries in the PHT after that are unchanged as a result of this branch.

PROBLEM CONTINUES ON NEXT PAGE
Part b (14 points): The branch predictor is initially in the state shown below executes five branch instructions at addresses 0x3004, 0x300a, 0x3012, 0x301c, and 0x3028.

After executing these five branch instructions, the state of the branch predictor is as shown below. Entries 2, 5, 8, and 14 are the only ones that changed.
**Your job:** Using the before and after state of the branch predictor shown on the previous page, complete the table below with the predicted and actual branch direction values for the five branches.

<table>
<thead>
<tr>
<th>Branch PC</th>
<th>Prediction (Taken/Not Taken)</th>
<th>Actual (Taken/Not Taken)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0x3004</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x300a</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x3012</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x301c</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x3028</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Problem 4 (20 points):

Assume memory locations x1000 to x1009 contain values as shown:

<table>
<thead>
<tr>
<th>Address</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>x1000</td>
<td>A</td>
</tr>
<tr>
<td>x1001</td>
<td>B</td>
</tr>
<tr>
<td>x1002</td>
<td>C</td>
</tr>
<tr>
<td>x1003</td>
<td>D</td>
</tr>
<tr>
<td>x1004</td>
<td>E</td>
</tr>
<tr>
<td>x1005</td>
<td>F</td>
</tr>
<tr>
<td>x1006</td>
<td>G</td>
</tr>
<tr>
<td>x1007</td>
<td>H</td>
</tr>
<tr>
<td>x1008</td>
<td>I</td>
</tr>
<tr>
<td>x1009</td>
<td>J</td>
</tr>
</tbody>
</table>

Assume:

- Memory is byte-addressable, little endian
- Memory address and data buses are independent and 16-bits each
- It takes 2 cycles after an address is sent to memory to latch a row address
- It takes 4 cycles to open a new row
- It takes 1 cycle to read the row buffer
- Data is on the data bus in the next cycle after the row buffer is read
- A new address can be supplied on the address bus in the same cycle that data is returned on the data bus

If we access memory in sequence starting with location x1000, we observe the following behavior on the memory address and data buses.

<table>
<thead>
<tr>
<th>Time</th>
<th>Addr</th>
<th>Data</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0x1000</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>0x1002</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>0x1004</td>
<td>BA</td>
</tr>
<tr>
<td>9</td>
<td>0x1006</td>
<td>DC</td>
</tr>
<tr>
<td>10</td>
<td>0x1008</td>
<td>FE</td>
</tr>
<tr>
<td>11</td>
<td></td>
<td>HG</td>
</tr>
<tr>
<td>18</td>
<td></td>
<td>JI</td>
</tr>
</tbody>
</table>

Part a (5 points): Given the access latencies above, and restricting the number of banks and columns to their minimum size, how many bank bits (B), column bits (C), row bits (R) and byte-on-bus bits (E) make up the 16 bit address to memory.

Specify with the letters B, C, R, E which bits of the 16-bit address belong to each.
Part b (5 points): If instead of accessing successive memory locations, we access every 16th location, our address stream will look like the following: 0x1000, 0x1010, 0x1020, 0x1030, 0x1040.

How many cycles does it take to complete this access stream?

Number of cycles

Part c (5 points): How would you change the assignments of address bits to bank, row, and column to minimize latency? Note: we are not changing the memory architecture, i.e., we keep the same number of bank, row, and column bits.

Again, specify with the letters B, C, R, E which bits of the 16-bit address belong to each.

Part d (5 points): How many cycles does it take to complete the access stream from part b after making the change in part c?

Number of cycles
Problem 5 (25 points):

Consider an out-of-order processor which executes its instructions based on the Tomasulo algorithm. The ISA specifies 8 registers, R0 to R7. The execute stage of the pipeline contains one pipelined adder and one pipelined multiplier. Fetch and Decode take a single cycle each. The ADD instruction takes 4 cycles to execute; the MUL instruction takes 5 cycles to execute. Both ADD and MUL take an additional cycle to store the result into a register and/or any reservation stations waiting for it. There is no data forwarding/bypassing implemented in this system.

Only a single instruction can store its result at a time. If two attempt to store their results at the same time, the older instruction has priority. The newer instruction will stall in execute until it can store its result.

The adder and multiplier each have 2-entry reservation stations. The reservation stations are initially empty and are filled from top to bottom. Each instruction remains in the reservation station until the end of the cycle in which it writes its result to a register.

The state of the register file is shown before execution, after cycle 7, and after all five instructions have completed.

The reservation stations are shown after cycle 7:

PROBLEM CONTINUES ON NEXT PAGE
The table below shows the cycles in which each functional unit is executing an instruction. An asterisk (*) indicates a stall.

<table>
<thead>
<tr>
<th></th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
<th>11</th>
<th>12</th>
<th>13</th>
<th>14</th>
<th>15</th>
<th>16</th>
</tr>
</thead>
<tbody>
<tr>
<td>Adder</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E*</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
</tr>
<tr>
<td>Multiplier</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
<td>E</td>
</tr>
</tbody>
</table>

**Part a (12 points):** Determine the five instructions that were executed.

<table>
<thead>
<tr>
<th>Opcode</th>
<th>DR</th>
<th>SR1</th>
<th>SR2</th>
</tr>
</thead>
<tbody>
<tr>
<td>I1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>I2</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>I3</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>I4</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>I5</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Part b (5 points):** Complete the timing diagram for the execution of the five instructions. Indicate the stage each instruction is occupying during each cycle. If an instruction is storing a result, write the name of the register written in that cycle. If an instruction is stalled in a stage, add an asterisk (*) to that cycle.

<table>
<thead>
<tr>
<th>Instruction</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
<th>11</th>
<th>12</th>
<th>13</th>
<th>14</th>
<th>15</th>
<th>16</th>
</tr>
</thead>
<tbody>
<tr>
<td>I1</td>
<td>F</td>
<td>D</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>I2</td>
<td>F</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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<td></td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>I3</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>I4</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>I5</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Part c (8 points):** If an additional entry is added to the reservation station for both functional units, how many cycles would it take to execute the same five instructions? Explain.
Figure 1: LC-3b Instruction Encodings
### Table 1: Data path control signals

<table>
<thead>
<tr>
<th>Signal Name</th>
<th>Signal Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>LD.MAR/1</td>
<td>NO(0), LOAD(1)</td>
</tr>
<tr>
<td>LD.MDR/1</td>
<td>NO(0), LOAD(1)</td>
</tr>
<tr>
<td>LD.IR/1</td>
<td>NO(0), LOAD(1)</td>
</tr>
<tr>
<td>LD.BEN/1</td>
<td>NO(0), LOAD(1)</td>
</tr>
<tr>
<td>LD.REG/1</td>
<td>NO(0), LOAD(1)</td>
</tr>
<tr>
<td>LD.CC/1</td>
<td>NO(0), LOAD(1)</td>
</tr>
<tr>
<td>LD.PC/1</td>
<td>NO(0), LOAD(1)</td>
</tr>
<tr>
<td>GatePC/1</td>
<td>NO(0), YES(1)</td>
</tr>
<tr>
<td>GateMDR/1</td>
<td>NO(0), YES(1)</td>
</tr>
<tr>
<td>GateALU/1</td>
<td>NO(0), YES(1)</td>
</tr>
<tr>
<td>GateMARMUX/1</td>
<td>NO(0), YES(1)</td>
</tr>
<tr>
<td>GateSHF/1</td>
<td>NO(0), YES(1)</td>
</tr>
<tr>
<td>PCMUX/2</td>
<td>PC+2(0); select pc+2</td>
</tr>
<tr>
<td></td>
<td>BUS(1); select value from bus</td>
</tr>
<tr>
<td></td>
<td>ADDER(2); select output of address adder</td>
</tr>
<tr>
<td>DRMUX/1</td>
<td>11.9(0); destination IR[11:9]</td>
</tr>
<tr>
<td></td>
<td>R7(1); destination R7</td>
</tr>
<tr>
<td>SR1MUX/1</td>
<td>11.9(0); source IR[11:9]</td>
</tr>
<tr>
<td></td>
<td>8.6(1); source IR[8:6]</td>
</tr>
<tr>
<td>ADDR1MUX/1</td>
<td>PC(0), BaseR(1)</td>
</tr>
<tr>
<td>ADDR2MUX/2</td>
<td>ZERO(0); select the value zero</td>
</tr>
<tr>
<td></td>
<td>offset(1); select SEXT[IR[5:0]]</td>
</tr>
<tr>
<td></td>
<td>PCoffset9(2); select SEXT[IR[8:0]]</td>
</tr>
<tr>
<td></td>
<td>PCoffset11(3); select SEXT[IR[10:0]]</td>
</tr>
<tr>
<td>MARMUX/1</td>
<td>7.0(0); select LSHF(ZEXT[IR[7:0]],1)</td>
</tr>
<tr>
<td></td>
<td>ADDER(1); select output of address adder</td>
</tr>
<tr>
<td>ALUK/2</td>
<td>ADD(0), AND(1), XOR(2), PASSA(3)</td>
</tr>
<tr>
<td>MIO.EN/1</td>
<td>NO(0), YES(1)</td>
</tr>
<tr>
<td>R.W/1</td>
<td>RD(0), WR(1)</td>
</tr>
<tr>
<td>DATA.SIZE/1</td>
<td>BYTE(0), WORD(1)</td>
</tr>
<tr>
<td>LSHF1/1</td>
<td>NO(0), YES(1)</td>
</tr>
</tbody>
</table>

### Table 2: Microsequencer control signals

<table>
<thead>
<tr>
<th>Signal Name</th>
<th>Signal Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>J/6:</td>
<td></td>
</tr>
<tr>
<td>COND/2:</td>
<td>COND₀; Unconditional</td>
</tr>
<tr>
<td></td>
<td>COND₁; Memory Ready</td>
</tr>
<tr>
<td></td>
<td>COND₂; Branch</td>
</tr>
<tr>
<td></td>
<td>COND₃; Addressing Mode</td>
</tr>
<tr>
<td>IRD/1:</td>
<td>NO, YES</td>
</tr>
</tbody>
</table>
Figure 2: A state machine for the LC-3b
Figure 3: The LC-3b data path
Figure 4: The microsequencer of the LC-3b base machine