A Framework for Exploring Unifying Theories of Empirical Software Engineering

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Abstract

One of the reasons for the lack of rigor in software engineering compared to physical and behavioral sciences is that the theories that underpin our work, both as software engineers and as software engineering researchers, have not been given enough attention. To provide a step forward towards greater rigor, a framework has been created with which to explore theories of software engineering and software engineering research. This framework provides a simple theory modeling language and model calculus to explore informally described theories and to generate the results of composing modeled theories.

To illustrate and evaluate this framework, a general theory about software engineering is presented and then two simple theories, D and E, proposed as the basis for laying out a unified theoretical foundation for software engineering and software engineering research. Software Engineering consists of two logical parts: design, and empirical evaluation (both terms used in their broadest senses). Theory D is the theoretical basis for the design part, and theory E is the theoretical basis for empirical evaluation. These two theories are then composed in various ways to lay out a space (a taxonomy, or ontology if you will) for software engineering and software engineering research. Finally, it is claimed that software engineering and software engineering research (both fully integrated with empirical evaluations) are models (in the logical sense) for these atomic and composed theories. To further evaluate the framework, examples are provided of modeling (implicit) theories found in a number of software engineering (theory) papers.

The results of this research are 1) a scientific elegance in creating larger more complex theories out of simpler theories, 2) an elegant way of explaining the complexity of software engineering and software engineering research, and 3) a theory modeling language and model calculus for composing the resulting theoretical models.

1. Introduction

The motivation for this research is twofold: 1) to establish a unifying foundation for software engineering, and 2) to establish the same rigorous empirical foundations for software engineering that we find in natural and behavioral sciences. As engineering pursuits go, software engineering is still a very young discipline. Researchers and practitioners have not given sufficient attention to the theories that underpin our discipline, leaving those theories implicit rather than clearly delineated. Further, the empirical support for many of these (implicit) theories and decisions about research and practice are often anecdotal rather than rigorously and empirically evaluated. While our understanding of many critical issues in empirical studies has improved, there is still a significant amount of work needed to be done to reach the level of understanding to be found in behavioral and physical sciences. There are many useful empirical techniques and structures that can be borrowed and adapted from them but there are still aspects to be more fully developed that are unique to software engineering and software engineering research.

In pursuit of these goals, a framework has been created for modeling informally described theories and a model calculus [15] for composing these modeled theories to create more complex theories from simpler ones. This framework provides a scientific elegance in creating more complex theories out of simpler ones, and an elegant way of explaining the complexity of software engineering and software engineering research. Composition is as fundamental in the theoretical pursuits of software engineering as it is in the practical pursuits of constructing software systems.

In the context of a general theory of software engineering (GTSE), this paper addresses the technical part of software engineering: the design, construction, evaluation, and deployment of software systems. This technical part of software engineering is separated out from such aspects as project management, business economics, and strategic planning. While software engineers play multiple roles in the context of both project management and strategic planning, the concern here is about their role creating and evolving software systems. So with respect to a GTSE, the focus is on the technical side of a GTSE. With respect to how this technical focus fits into a GTSE, see Batory and Perry [17] for a proposed theory about the compositional and structural organization of a GTSE.

The basic theory presented here is that Software Engineering consists of two logical parts: design and empirical evaluation (both terms used in their broadest senses). There are two simple theories proposed, D and E, as the basis for laying out a unified theoretical foundation for software engineering and software engineering research [16]. Theory D is the theoretical basis for the design part, and theory E is the theoretical basis for the empirical evaluation part. Models for D and E are then defined, using the presented theory modeling language, and subsequently, the theories D and E are composed using the model calculus in various ways, and the composed models used to explore various ways of thinking about the underlying foundations for software engineering and software engineering research.

Theories D and E abstract away details that undoubtedly differ significantly in actual research and practice; but, as in practice, abstraction is one of our most important intellectual tools for managing complexity. As will be illustrated in what follows, even with the abstract and
simple theories D and E, the composition of theories results in significant increases in complexity, just as it does in the composition of software components into software systems. Brooks in his No Silver Bullet paper [5], states: “I believe the hard part of building software to be the specification, design, and testing [evaluating] of this conceptual construct, not the labor of representing it and testing the fidelity of the representation. . . . If this is true, building software will always be hard. There is inherently no silver bullet.” Further, he states that “Software entities are more complex for their size than perhaps any other human construct . . . .” A complete general theory of software engineering is at least as equally hard, and at least as equally complex. The envisioned use of the framework and the model calculus is to delineate and explicate the elements of design theories via models, and to clarify the implications of those design models with respect to their evaluations via the resulting taxonomies. The resulting explicitness of both will help us to understand more fully, and reason more carefully, about what is often hidden in their current implicitness.

The paper is organized as follows. The rest of the introduction 1) defines how the terms theory and model are used in this paper, 2) provides a general overview of theories, 3) summarizes important aspects of science in general, as well as 4) delineating specific differences among natural, behavioral, and artificial sciences. Section 2 provides a formal definition of models and presents the model calculus. Section 3 illustrates this paper’s approach with simple theories D and E and their models. Section 4 illustrates the issues in theory and model composition by composing the simple theories D and E in various ways to cover software engineering and software engineering research. Section 5 presents more complex versions of D and E, D’ and E’, introducing the notion of refining a model and exploring the implications for compositions of these more complex theories in the composition E’:E’ – the evaluations of evaluations. A variety of examples are used to illustrate various aspects in sections 4 and 5. Section 6 evaluates the utility of the presented approach by using the framework to explore three rather diverse theories and models. Finally, Section 7 summarizes the results of this research.

1.1 Theories and Models

The terms “theory” and “model” are used and misused in a variety of ways, often informally and interchangeably. They are used here in a very specific way: a theory (a more or less abstract entity) is reified, represented, satisfied, etc., by a model (a concrete entity).

This view of theories and models is derived in part from Turski and Maibaum [20] where they state “A specification is rather like a natural science theory of the application domain, but seen as a theory of the corresponding program it enjoys an unmatched status: it is truly a postulative theory, the program is nothing more than an exact embodiment of the specification”. In this paper, theory is considered to be broader than a specification and, more than likely, less formal.

Models are often used as a representation of a theory. In natural sciences, the model is often a set of mathematical formulas. In logic, a model is an interpretation of a theory and has certain logical properties. Here the purpose is to broaden the notion of a model to be a representation (indeed, a reification) of the theory. The model is of paramount importance in design disciplines as it is the visible manifestation of a theory. Of fundamental importance is the fact that a theory can have an arbitrary number of models.

1.2 More About Theories

The key to a unifying, rigorous, and systematic foundation for software engineering, software engineering research, and empirical studies in software engineering and software engineering research, is to be found in a focus on theory: 1) the source of the theories; 2) the structure of the theories; and 3) the use of the theories.

Source of Theories. In terms of sources of theories relevant to software engineering, three different types of theories are important:

1. Scientific theory – Scientific theory is based on observations of the world. They change on the basis of new observations, or new interpretations of observations.
2. Legal theory – Legal theory is quite different: it is based on decisions about the world, and is changed on the basis of new decisions or new interpretations of decisions.
3. Normative theory – Normative theory is different yet and is based on a system of philosophical tenets about what is good and bad, and judgments are changed on the basis of new tenets, new inferences from tenets, or new interpretations of them.

Theories in design disciplines are a combination of all three of the above. They are based on observations, decisions, and judgments about the world. They change on the basis of new observations, decisions, and judgments or on the basis of new interpretations of those observations, decisions, and judgments.

Structure of Theories. Markus and Robey [13] distinguish two different theory structures:

1. Variance – In the case of variance, the theoretical structure is a set of laws about interactions or relationships. For example, given a variation in theory A, what other units can be linked to A such that they account for the variance in A.
2. Process – In the case of process, the theoretical structure is a temporal ordering of activities, steps, or events.

We find both kinds of theoretical structures in design discipline theories depending on what kind, and at what level, we are theorizing about design and evaluation issues.

Use of Theories. The taxonomy of uses described here is derived from Gregor [9]. Five distinct uses of theories are distinguished that may be used also in combinations:
1. Description – A theory is used to describe phenomena in terms of its constructs, properties, and relationships, and the boundaries within which those properties and relationships hold. Descriptions are intended to be complete.

2. Prescription – A theory is used to provide a set of constraints on its constructs, properties, and relationships, and the boundaries within which those properties and relationships hold. Prescriptions are intended to emphasize the crucial aspects of the theory.

3. Explanation – A theory is used to explain how, why and when things happen based on causality and methods of demonstration (that is, argumentation). The intent is to provide deeper understanding and insight into the subject phenomena.

4. Prediction – A theory is used to predict what will happen on the basis of necessary and sufficient conditions for the theorized phenomena. The phenomena will not happen if the necessary conditions are withheld; nor will they happen if the sufficient conditions are withheld.

5. Action – A theory provides principles, techniques, and methods for enabling the desired phenomena (for example, achieving a desired goal, or designing, constructing, or evaluating an artifact).

Depending on the context in software engineering, theories are used in all these different ways. Software requirements, considered as theories, or mainly descriptive, but may also be prescriptive. Certainly requirements are used as explanations for various aspects of their models. And in requirements based testing (experimental evaluations), requirements are used for predicting the outcomes of the testing experiments. Theories in software engineering research do all of these things as well, and in addition also often included in the theoretical underpinnings are theories as actions – that is, principles, techniques and methods for enabling the desired phenomena.

Theories, of course, influence their models: the source of a theory will affect its model; the structure of a theory will influence the structure of its model; and, the use of a theory will also influence the structure of its model.

1.3 Experimental Science

A look at basic science is also instructive, even though one might argue that it is not necessary since everyone understands it thoroughly. The reason for doing this is to set the stage for the theories and models relevant for empirical software engineering.

Science is basically an iterative process consisting of the following steps:

- Observations and abstractions are used to create a theory T.
- Theory T is tested against reality W with an empirical evaluation E using one or more instruments I.
- Theory T is then reconciled with reality.
- When predictions don’t agree with reality, assuming a sound empirical evaluation, theory T is changed.

Gooding et al. [7] argue for the critical importance of the instruments used in experimental work. They are the lens through which the world is observed. To paraphrase Wittgenstein [22], the limits of my instruments are the limits of my world. They enhance, limit, and color the way the world is viewed. In natural sciences, instruments are often physical creations; in behavioral sciences they are often intellectual creations. Humans are common instruments in both. Instruments may be active or passive. They may be theory-laden or transparent and neutral. They may be reliable and standardized or not. In any case, they are a critical part of the empirical apparatus and as such will play a critical part in any scientific endeavor.

1.4 Natural, Behavioral & Artificial Sciences

In remedying the current lack of rigor in software engineering, it is critical to understand how the sciences of the artificial (that is, the sciences of design 1) [19] differ from, and are similar to, behavioral and natural sciences. Obviously, all types of theories must be testable. The differences come in the context of testability and the constraints faced. The sciences of the artificial have some aspects in common with natural and behavioral sciences: testing is done in both physical and behavioral contexts. However, testing is also done in intellectual and technological worlds as well. For the physical and behavioral contexts there are hard and probabilistic constraints, respectively. For the technological context, there are selectable constraints – i.e., constraints that can be selected among, perhaps arbitrarily. For the intellectual context, there are malleable constraints – i.e., constraints that can be changed, also arbitrarily.

There are interesting differences between natural and behavioral sciences that are relevant to design disciplines. The general goals of natural sciences are to understand natural phenomena and create a theoretical basis for prediction. Further, natural sciences provide a basis for invention and engineering. The general goals of behavioral sciences are to understand human and societal phenomena and provide a theoretical basis for prediction and interventions. The inventions and interventions are important because of the need to change the world which is also one of the fundamental goals in sciences of the artificial: build systems of practical value in, and effect changes in, the world [10], not merely observe it (though, of course, we do need to observe our software systems and make predictions about them as well).

For those interested in delving more broadly into the issues of design, Simon’s book [19] referenced here is highly recommended. Other useful design references are: Suh’s The Axiomatic Theory of Design, Oxford University Press 1990; Gero’s various papers on his function-behavior-structure framework; Cross’s Designerly Ways of Knowing, Birkhäuser Architecture, 2007; and Petre and van der Hoek, Software Designers in Action: A Human-Centric Look at Design Work, CRC Press, (forthcoming). And of course, there have been a variety of design methods proposed specifically for software engineering.
2. A Model Calculus

Since theories as used here are informal entities, their composition is also informal and the resulting integration is done informally. This will become clear as theories are introduced and composed in the following sections.

The theory about models, however, has a more formal definition and a set of rules for the model operators. Models provide the means of understanding the implications of theories and compositions of theories by reifying them so as to illustrate the true breadth, depth and complexity of those models and compositions.

2.1 Models

A model is a tuple consisting of two sets: a set of objects O (or elements), and a set of mappings M (or more informally, transformations, processes, derivations, etc.) from an object in one set of objects to another object in a (usually, but not necessarily, different) set of objects.

\[
\text{Model} = < \{O\}, \{M\} >
\]

Models can be arbitrarily considered to be either atomic or open-structured. If viewed as atomic, then their structure is abstract – that is, the structure is hidden and the model is considered as a whole, indivisible entity. If viewed as open-structured, all the individual objects and mappings are visible in the model. It is a matter of choice whether a model is viewed as atomic or open-structured and may be one or the other depending on the context of its use.

2.2 Model Syntax

The following are the special symbols in the model calculus (in order of precedence):

- "+" a unary operator on objects that indicates 1 or more of the designated objects. For example, A+ represents one or more A elements.
- ":" a binary operator on models and model components that indicates composition of two such elements – i.e., the restriction of the left model element or model to the right model element or model. For example, B:C can represent the composition of models B and C, the composition of model B to element C, the composition of element B to model C, or the composition of elements B and C.
- "*" a binary operator on objects that delineates an object in the Cartesian space of two objects. This can be thought of as functional application of the first object to the second yielding a specific object as its value. For example, in model D below M*W is the application of a model M to a world W.
- "\rightarrow" a binary operator that maps one object onto another. For example, T \rightarrow M in model D below maps theory T into model M – that is, T \rightarrow M is a process or transformation by which model M is derived from theory T.

() parentheses may be used to clarify the use of these operators.

Generally alphabetic letters are used to denote objects, mappings, and models, though of course one may use descriptive names for clarity if needed. For clarity in distinguishing between models or model elements, lower case letters are sometimes used for one of the model’s elements. Further, a dot notation, Model.Element (for example D.T), is sometimes used to represent a specific element of a model (element T of model D), typically to distinguish it from another, possibly identical, element in a different model. Different font colors may be used for distinguishing models and/or elements of models. I have tried to provide distinct letters for the different elements in the various theories but T (theory) is used in both the design and empirical models D and E. They generally denote different theories.

2.3 Mappings

All possible mappings are possible in this model calculus:

- One to one mappings are indicated by A \rightarrow B.
- Many to one mappings are indicated in several different ways. For example, A * B \rightarrow C, and A+ \rightarrow B.
- One to many mappings are indicated by A \rightarrow B+ and A \rightarrow B * C.
- Many to many mappings are indicated by any combinations using "+", "*", together with "\rightarrow".

2.4 Calculus Rules

The following are the distribution rules among expressions about various operators.

- ":" is both left and right distributive over models.
- ":" is left distributive over "+", "*", and "\rightarrow".

Examples of the first distribution rule can be seen in the next section. Examples of the second are as follows with O representing objects (elements) and AM representing an abstract model:
There is one rule about the operator "+" (which implies that "+" is left distributive) over "*" and "+". For example,

\[(O_1 \rightarrow O_2) + = O_1 + \rightarrow O_2 +\]
\[(O_1 * O_2) + = O_1 + * O_2 +\]

2.5 Model Composition

Models (and theories) can be composed to yield further models (and theories). As mentioned above, model compositions are indicated by \( A : B \). Further, models can be arbitrarily considered to be atomic (that is, its structure is hidden) or open-structured (that is, the objects and mappings are visible).

For example, composing an open structured model (OSM) with an atomic model (AM) results in a single model via left distribution of the atomic model AM over the open-structure model OSM. This composition yields one model.

\[\text{OSM} : \text{AM} = \quad \langle \{O\}, \{M\} > : \text{AM} = \]
\[\langle \{O\}, \text{AM} : \{M\} > = \]
\[\langle \langle O^1 : \text{AM} \ldots O^n : \text{AM} \rangle, \{M^1 : \text{AM} \ldots M^m : \text{AM} \rangle \rangle =\]

Note that in this case, the above left distribution rules of composition over mappings can then be applied moving model AM into those mappings.

On the other hand, composing an atomic model with an open structure model yields a number of models (equal to the number of objects and mappings) via right distribution of the atomic model AM over the open-structured model OSM.

\[\text{AM} : \text{OSM} = \quad \langle \{O\}, \{M\} > = \]
\[\langle \text{AM} : \{O\}, \text{AM} : \{M\} > = \]
\[\langle \langle \text{AM} : O^1, \ldots, \text{AM} : O^n, \{\text{AM} : M^1, \ldots, \text{AM} : M^m \rangle > = \]
\[\text{AM} : O^1, \ldots, \text{AM} : O^n, \text{AM} : M^1, \ldots, \text{AM} : M^m =\]

Each of these compositions is a model restricted to that particular object or mapping. Note that because of the left distributive rule of composition over mapping operators, nothing further can be done if AM remains atomic. However, if AM is treated instead as an open-structure model, then the various objects and mappings can be left distributed over that now open model.

3. The Two Basic Theories \( D \) and \( E \)

For purposes of illustration, extremely simple (and very abstract) examples of Theories \( D \) and \( E \) are chosen deliberately. In this way, the utility of the formal model description format and the utility and implications of the composition rules in the context of both open structured models and abstract models can be evaluated. More realistic but still abstract theories and models for \( D \) and \( E \) are presented below. In either case, the examples are also used to make the case for covering software engineering and software engineering research.

3.1 Theory & Model \( D \)

Theory \( D \) is meant to capture the typical cycle of creating a theory that is then reified into a model where the model is then injected into the world – i.e., an initial, non-iterative, non-evolutionary development of a model from a theory. The injection of the model into the world results in a changed world\(^2\). \( D \) is summarized as follows:

- We observe and abstract some specific part of the world and create a theory.
- From that theory we create a usable model to reify or represent that theory.
- When satisfied that the model adequately represents the theory, we inject the model into the world.

The model of \( D \) consists of three elements (objects) and three transformations (mappings, or, if you will, processes). The elements are as follows:

- \( W \) the world, but more specifically, the part of the world relevant to the theory
- \( T \) the theory initiated by observations and abstractions
- \( M \) a model that reifies, represents or satisfies the theory \( T \)

The transformations involving these elements of the model are as follows:

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\(^2\) Note, however, the world can also change for a variety of other reasons. The discussion of those reasons is beyond the scope of this paper.
The following is an example of a system to manage samples of college textbooks for Harcourt, Brace & Jovanovich (HBJ).

Note that this is a very basic theory, but it still is sufficiently rich to cover the entire range of studies from exploratory through to rigorously controlled experiments (as will be indicated by a more complete model of E, model E' below).

Theory E is meant to capture the process of empirical evaluation. Again, for purposes of explanation and illustration a very simple theory for E is used. A more elaborate theory for is described below to illustrate more elaborate empirical evaluations. It is sufficient at this point to indicate that empirical evaluations can range from very informal evaluations (as indicated by this formulation of E) to formal and controlled experiments (as will be indicated by a more complete model of E, model E' below).

Not surprisingly, the theory E is essentially a simplification of basic empirical science described above.

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Not surprisingly, the theory E is essentially a simplification of basic empirical science described above.

- Given a world W, observe and abstract to create a theory
- Given a theory T, generate an hypothesis H to test some part of the theory
- From the hypothesis H, generate an evaluation regimen R.
- Apply the regimen R to the world W and revise theory T if necessary.

Note that this is a very basic theory, but it still is sufficiently rich to cover the entire range of studies from exploratory through to rigorously explanatory studies. In practice, theory T may be vague and ill-formed (as it would be for exploratory work) or well-formed and mature (as it should be when doing explanatory work). Similarly the hypothesis may be generic and open-ended or focused and specific. Evaluations E may be opportunistic (for exploratory work) or specifically and well-designed. Further, the theory of E supports both theory generation (in the case of exploratory work) and focused theory evaluation.

The basic elements in the model are: world W, theory T, hypothesis H, and evaluation regimen R.

The following transformations represent the processes of conducting an empirical study.

- **W → T** generate a theory T by observing and abstracting from the world W
- **T → H** derive an hypothesis H from theory T

This model represents the informal theory of D above.

The design part of software engineering, at a suitable level of abstraction, is a reification of model D, and hence is a model of theory D. For example, W in theory D contains what Jackson [10] calls the problem space. It is that part of the world that represents the problem to be addressed with the software system. Observations and abstractions from this problem space are used to create a theory T (i.e., theory T in D) of the problem to be solved. T can be considered to be the requirements. T may also include a theory of one or more relevant domains of the world W. W also contains what Jackson calls the solution space. This solution space contains the elements that are put together to create the model M (the software system itself) that refines and represents those requirements T.

W→T is the process of deriving the requirements from the chosen problem space by observing and abstracting what is considered to be critical and central to the problem to be solved. It is also the process of understanding the effects of a changing world on the requirements that exist as the basis for an existing system M. T→M is the process of creating and evolving the model/system from the theory/requirements. And, finally, M*W→W releases/injects the model/system into the world to be used in solving the intended problem, and, in doing so, often radically changes the world. This injection is often referred to as *technology transfer*.

**An Example.**

The following is an example of a system to manage samples of college textbooks for Harcourt, Brace & Jovanovich (HBJ).

- **W** The part of the world W that was important in this example was the marketing of college textbooks.
- **T** Theory T was created about how to manage the distribution of samples of these textbooks to college teachers.
- **M** Model M is an implementation in COBOL of Theory T
- **W → T** The process of creating T, W → T, was done in conjunction with the editors and marketers of HBJ and focused on the input, handling, tracking, and distributing sample textbook requests. The result of this process was a written document describing T that was approved by HBJ.
- **T → M** The process of transforming theory/requirements T into a model/system M, T → M, was done in a top-down, incremental manner.
- **M*W → W** Once a completed model M satisfying theory T was created, model M was released into use, M*W → W, fundamentally changing how HBJ managed the distribution of their college textbook samples (i.e., introducing a new W where the marketing of college textbooks was changed significantly).

Clearly, this example is a reification of model D, and hence also a reification of the simple theory D. Theory T in this example required multiple pages to describe. The model D required about 66k lines of COBOL and was iteratively tested as it concurrently with the iterative transformation of T into M (one of the evaluations E discussed below). The injection of the system into the world was a simple release of the system into use.
An Example

Jani et al. [11] compared and evaluated two methods of deriving an architecture from a formal goal-oriented requirements specification of a power plant. As this was exploratory work, there was little theory that was available. This should be considered as more of a theory generation evaluation.

**The two architecture methods started from KAOS goal oriented requirements specifications, but the two methods used them in quite different ways. One generated a detailed architecture description whose structure was determined in good measure by the structure of the theory/requirements specification. The other generated a high level architecture prescription, keeping the focus on the goals as constraints on the architecture. There is an interesting difference in the two different processes T \(\rightarrow\) M that transform a theory into a model.**

### 4. Composing Theories

Two simple theories, D and E, have been introduced that represent the two different aspects of software engineering. The composition of the two theories is a critical part of software engineering: the evaluation E of the design D. These evaluations play a vital role in, among other things, the design process itself where one must make trade-offs between design decisions and also the evaluations of the model against the theory. Thus E:D plays a vital role throughout the entire process.

Other compositions lead us into the realm of software engineering research. For example, composing D with itself, D:D, leads to the topics of how to design the structure of artifacts and process to be used in the process of software engineering. Composition D and E in a different way leads to the problems of designing evaluations, while composing E with itself, E:E, leads to topics of how to evaluate the evaluations used in software engineering. It is possible to create more complex compositions, such as E:D:D, that cover the problem of evaluating our software engineering research. These compositions are explored below.

#### 4.1 Evaluating Design – E:D – i.e., E composed with D

It is here in the evaluation of the design that one finds the other half of the software engineering enterprise. It is here that the adequacy and utility of our theories and models, the efficacy of the processes used in deriving these theories and models are determined.

It should be noted that there is a theory T in D and a theory T in E. It is possible that the two theories may be identical, but most likely they are different. Theory T in D is a theory meant to be transformed into a model M. Theory T in E is a theory about some aspect of D (including D itself) and the properties of that aspect of D that can be confirmed or refuted by means of an evaluation E. It is more likely that E:T has a meta-theoretical relationship with those aspects of D. Examples below should help with this distinction.

To evaluate theory D, consider the composition of an atomic model of E (specifically E₂ but as it is clear the subscript is dropped) with an open structured model of D. This composition yields the following 6 models – that is, a model for evaluating each element of D.

- Three models about evaluating the elements of D:
  - evaluation of the world W of D: E:W;
  - evaluation of the theory T of D: E:T;
Three models about evaluating the processes of D:

- creating a theory \( T \) from the world \( W \): \( E(W \rightarrow T) \);
- creating a model \( M \) from theory \( T \): \( E(T \rightarrow M) \);
- changing the world as a result of injecting model \( M \) into it: \( E(M \rightarrow W) \).

Among the kinds of questions the evaluations might address are the following: the adequacy of \( D.T \) representing some part of \( D.W \); the adequacy of \( D.M \) representing \( D.T \); the utility of \( D.M \) in the world \( D.W \); the effectiveness of such transformations as creating \( D.M \) from \( D.T \), or of creating \( D.T \) from \( D.W \).

Alternatively, the evaluation of \( D \) as a whole by composing an open structured model of \( E \) (\( E_{\alpha} \)) with an atomic \( D \) (\( D_{\lambda} \)) yielding a single model \( E_{\alpha}D_{\lambda} \) that consists of the following.

- The elements of the model are:
  - the world \( W \) of evaluations of \( D \): \( W:D \);
  - the theory \( T \) of evaluations of \( D \): \( T:D \);
  - the hypotheses \( H \) about evaluations of \( D \): \( H:D \);
  - the regimens \( R \) for evaluations of \( D \): \( R:D \).

- The processes of the model \( E:D \):
  - creating a theory \( T:D \) from the world \( W:D \): \( (W \rightarrow T):D = W:D \rightarrow T:D \);
  - deriving an hypothesis \( H:D \) from the theory \( T:D \): \( (T \rightarrow H):D = T:D \rightarrow H:D \);
  - deriving a regimen \( R:D \) from the hypothesis \( H:D \): \( (H \rightarrow R):D = H:D \rightarrow R:D \);
  - applying regimen \( R:D \) to world \( W:D \), evolving theory \( T:D \): \( (R \ast W \rightarrow T):D = R:D \ast W:D \rightarrow T:D \).

Note that for the processes of \( E:D \) there is a left distribution of \( D \) over \( ":" \) into the processes that yields the elements of \( E:D \).

In the composition of two models, there are \( n \times m \) elements and processes – in this case, \( 6 \times 8 = 48 \). Thus given these two models of design and evaluation, a fully rigorous evaluation of \( E:D \) (where both models are open structured) would have 48 distinct elements and mappings for a full and rigorous evaluation. The fully expanded resulting matrix of \( E:D \) is found in Appendix 1.

Obviously, the more complex the models, the larger and more complex the taxonomy. For example the more complex alternative models present below will result in a much larger taxonomic space. Similarly if three models are composed together, the number of elements and processes would be: \( n \times m \times \alpha \). One use of the taxonomy the delineation of all the elements to be considered systematically in any composition. Another use of the taxonomy is e found in the example below where it is possible to locate explicitly what element in that composition is being addressed.

**An Example.**

In the example discussed above, the empirical study [11] could also be described as evaluations of the transformations of a theory (the goal-oriented requirements specification) to a model (in this case, an architecture), \( E(T \rightarrow M) \), for each method.

Thus, a model of the evaluation of \( T \rightarrow M \) would entail the following elements: \( W:(T \rightarrow M) \), \( T:(T \rightarrow M) \), \( H:(T \rightarrow M) \), \( R:(T \rightarrow M) \). These are the elements used in the transformations of \( E:T \rightarrow M \).

- \( W:(T \rightarrow M) \rightarrow T:(T \rightarrow M) \) – Create a theory about the process of creating models from theories from a world about processes of creating models from theories.
- \( T:(T \rightarrow M) \rightarrow H:(T \rightarrow M) \) – Create an hypothesis about the process of creating models from theories from a theory about process creating models from theories.
- \( H:(T \rightarrow M) \rightarrow R:(T \rightarrow M) \) – Create a regimen for evaluating the process of creating models from theories from the hypothesis.
- \( R:(T \rightarrow M) \ast W:(T \rightarrow M) \rightarrow T:(T \rightarrow M) \) – Reconcile the results of the regimen applied to the world to evolve the theory about the process of creating models from theories.

As mentioned above, there was little established theory, \( T:(T \rightarrow M) \), about the process of creating a (architectural) model from a theory. The hypothesis then was a simple one: the resulting models \( M \) would be the same or very similar. The regimen applied to each methods as the theory \( D.T \) – the KAOS goal oriented theory/requirements specification of the power plant. The results of the evaluation were as follows:

- Method A [12] began at a detailed level by constructing a dataflow architecture, applying architecture styles, and using patterns to achieve non-functional specifications, but did not have a specific criteria about when to stop applying styles and patterns.
- Method B [3,4] began at the most general level, goals, and required the user of the method to create an initial partitioning of the goals into the highest level components according to some architectural criteria (for example, non-functional characteristics, etc.). Once the initial structure was in place, the goals for each component were used to derive the sub-components to satisfy the various sub-goals. The architectural derivation was completed when all goals were completely covered.
The two methods resulted in very different architectures: in method A, it was very easy to start but difficult to determine when to stop, and resulted in a detailed network-style architectural description that mirrored the structure of the specification; in method B, it was difficult to know how to begin but simple to determine when it was done, and resulted in a high level, hierarchical architectural prescription that did not mirror the specifications to the extent of the other.

Obviously, there is a significant amount of work needed to create a theory about methods of creating architectures from requirements, given the significant differences in the resulting architectures from the same specification. This is not surprising given that there was very little theory to begin with. For example, if $E:T \rightarrow M$ is to be used predictively, what is needed in $T:(T \rightarrow M)$ to enable useful predictions?

### 4.2 Designing Design – Theory $D:D$

Theory $D:D$ (the composition of $D$ with itself) is meant to capture the typical cycle of designing $D$ (i.e., a theory of producing a design product) that is then reified into a model of $D$ and the model is injected into the world of $D$. I summarize it as follows:

- We observe and abstract some specific part of the world and create a theory of
  - What the world of $D$ is like
  - What form a theory in $D$ should take
  - What form a model in $D$ should take
  - What form the processes of creating the theory and its model of $D$ should take
  - How the resulting model of $D$ should be injected into the world

- From that theory we create a usable model to reify or represent that theory of
  - What the world of $D$ is like
  - What form the theory in $D$ should take
  - What form the model in $D$ should take
  - What form the processes of creating the theory and model $D$ should take
  - How the resulting model of $D$ should be injected into the world..

- When satisfied that the model adequately represents the theory we inject the model into the world.

The composition of model $D$ (as an open structured model) with itself (as an atomic model) – $D:D_A$ – results in a new model with the following elements and represents the theory $D:D$ above.

- $W:D$ the world of $D$
- $T:D$ the theory of $D$
- $M:D$ the model of $D$

The transformations involving these elements of the model generate the following:

- $W:D \rightarrow T:D$ generate a theory: observe and abstract from the world of $D$ to create a theory $D$
- $T:D \rightarrow M:D$ from the theory of $D$ create a model of $D$
- $M:D * W:D \rightarrow W:D$ inject model of $D$ into the world of $D$ thereby changing it (which depends on both the model and the world before the injection of the model into it).

The composition of model $D$ (as an atomic model) with itself (as an open structured model) yields nine models: $D:W$, $D:T$, $D:M$, $D:(W \rightarrow T)$, $D:(T \rightarrow M)$, $D:(T \rightarrow T)$, $D:(M \rightarrow M)$, $D:(M \rightarrow T)$, $D:(M x W \rightarrow W)$ – i.e., the design of each of the elements in the design model $D$, and the various transformations that take place in the design model $D$.

To illustrate the richness of compositional results, consider $D:T$ where $D$ is viewed as an open structured model. The objects are $W:T$, $T:T$ and $M:T$ (the world of $T$, the theory of $T$, and the model of $T$ respectively). The transformations: are $W:T \rightarrow T:T$, $T:T \rightarrow M:T$, $T:T \rightarrow T:T$, $M:T \rightarrow M:T$, $MT \rightarrow T:T$, and $M:T \rightarrow W:T$, exactly analogous to the transformations of $D$. The same follows for each of the remaining composed models above (see Appendix 2 for a complete delineation of the composition matrix).

Analogous to the claim that the design aspect of software engineering is a reification of the model of $D$, the design aspect of software engineering research is a reification of the model of $D:D$, and it is here that things get very interesting.

#### Discussion of Examples.

The elements found in the this discussion can be found in Appendix 2 and are the elements when both models in $D:D$ are consider to be open structured.

$T:W$, $M:W$ – world of software development. The world of software systems is a varied and multi-faceted world. It is a world of problems and solutions [10]. It is a world that changes for a variety of reasons. It is a world where some problems are not solvable at all by automation as well as a world where some problems are just too hard to solve at all [6]. For the problems that are solvable, there are those that are solvable by what Vincenti [21] calls normal design and those that are solvable only by radical design. Solving problems that require radical design may or may not be successful. When it is successful it is almost always the result of several iterations.
It is a world of rapid technological change where software-intensive systems are increasingly invading our lives, where computation is constantly getting faster and cheaper, and where electronic storage is getting larger, faster and cheaper as well. It is a world where the bases for design decisions are constantly changing, where the tradeoffs previously made must be re-examined in the light of the current state of the world.

**T:T, M:T – theories/models of requirements.** Frustratingly, there is little theory that is explicit in D:D:T:T or D:D:T:M; it is by-and-large implicit. Or, more specifically it is often stated normatively rather than descriptively (as one would find in natural sciences, for example). In one way, this is not surprising as our theories in D are largely normative: the system ought to do ...; it ought to respond within ...; it must provide ... Indeed, this normative approach is a feature of the sciences of the artificial [19]. And, of course, it is seen all too easily in every new *salvation du jour*.

However, since the goal in this paper is to lay a foundation for empirical software engineering, to make progress towards the kind of rigor found in natural and behavioral sciences, the level of discourse must be more descriptive — that is, theories must be more explicit so to be easily testable. Note also that theories are critical in empirical evaluations and there too theories have not been explicit enough to become a rigorous discipline.

**T:M, M:M – theories/models of software systems.** Common theories in D:D about the form that a model D:M (or parts of the model) should take include structured programming, object oriented programming, aspect-oriented programming, etc. Looking at this in a different way, there are the theories about creating systems bottom up, or top down, or about structuring them for future change, or about organizing them hierarchically, or as networks of cooperating processes, or to reflect the shape of the problem. There are those who theorize that the components in software systems should be orthogonal and each component do one thing well, while others such as Jackson indicate that designers should be mindful of the fact that the world (the problem space) has been implemented with the full exploitation of the Shanley Principle [10] of efficient design where each element serves multiple purposes.

There are a variety of theories in D:D about the transformation from requirements to the system D:D:T:D. The more or less standard ones include waterfall development, Boehm’s spiral development, refinement, etc. A more radical departure from these standard approaches is that of Extreme Programming. An interesting variation of refinement can be found in Batory’s algebraic compositional approach [2] that is considered below.

### 4.3 Evaluating the Theory D:D → E:D:D

One way to evaluate the design theory of D:D is to compose an atomic model of E with an open structured model D1 and atomic D2 in D1:D2. This composition yields the following model:

- The evaluation of
  - E:(W:D) the world of D;
  - E:(T:D) the theory of D;
  - E:(M:D) the model of D.

- The evaluation of the processes of
  - E:(W:D → T:D) creating a theory T:D from the world W:D;
  - E:(T:D → M:D) creating a model M:D from theory T:D;
  - E:(M:D*W:D → W:D) injecting model M:D into the world W:D.

As D:D was significantly more complex than D, so E:D:D is significantly more complex than E:D. Despite this increased complexity, the aims are still the same as with E:D. It’s just that there are many more elements and processes to evaluate. The space is much larger — in this case 8 * 6 * 6 = 288 objects and mappings. But of course that is to be expected when the concern is with theories and models about theories and models as in software engineering research.

However, just as the software engineering of software systems is composed of design and evaluation, so too is research about the design and evaluation of software systems composed of both design and evaluation. For example, evaluating

- the theory T in T:D might represent evaluating theory completeness, theory representativeness of the user’s needs or problems, or theory adequacy (how good is the theory for this domain);
- the world W in W:D might represent evaluating the user’s needs and desires about D, or the using of D, or the problem domain of D;
- the model M in M:D might represent evaluating the adequacy of model M of D – that is, how well does M:D represent T:D (black box testing) – or how good is M:D relative to the intent of the modeler (white box testing) – or the usefulness of M:D in W:D;
- the transformation W:D → T:D might represent evaluating the quality of the theory of D formation process;
- the transformation T:D → M:D might represent evaluating the quality of the model formation process; and
- the transformation M:D*W:D → W:D might represent evaluating the quality of the model deployment process.

Alternatively, consider E:D:D where D:D is atomic and E is open structured. E:(D:D) creates a new model of empirical evaluation focused specifically on D:D – i.e., evaluating D:D as a whole. That is, there are theories about D:D (derived from the world W:(D:D)) from which
hypotheses are created, and from those hypotheses regimens are created (i.e., evaluations) – and there are processes for doing just that with respect to D:D.

The elements of this model are as follows:

- \( W:(D:D) \) the world W of designing designs (D:D)
- \( T:(D:D) \) the theory T of designing designs (D:D)
- \( H:(D:D) \) the hypothesis about designing designs (D:D)
- \( R:(D:D) \) The regimen for evaluating the designing of designs (D:D)

The processes of evaluating the designing of designs D:D (left propagating D:D)

- \( (W \rightarrow T):(D:D) = W:(D:D) \rightarrow T:(D:D) \)
- \( (T \rightarrow H):(D:D) = T:(D:D) \rightarrow H:(D:D) \)
- \( (H \rightarrow R):(D:D) = H:(D:D) \rightarrow R:(D:D) \)
- \( (R \ast W \rightarrow T):(D:D) = R:(D:D) \ast W:(D:D) \rightarrow T:(D:D) \)

Consider the first model D in D:D, the design of software engineering research, and make it open structured, leaving the second D atomic, an even more complex set of models is exposed. Consider the evaluation \( E:(T:D) \), the evaluation of a theory of design (i.e., D):

- \( W:(T:D) \) the world of theories about D
- \( T:(T:D) \) a theory of the theories about D
- \( H:(T:D) \) an hypothesis derived from the theory about theories about D
- \( R:(T:D) \) a regimen to test the hypothesis about the theory about theories about D
- \( W:(T:D) \rightarrow T:(T:D) \) deriving a theory about the theories about D from the world of theories about D
- \( T:(T:D) \rightarrow H:(T:D) \) deriving an hypothesis about theories about D from the above theory
- \( H:(T:D) \rightarrow R:(T:D) \) deriving a regimen to test the hypothesis about theories about D
- \( R:(T:D) \ast W:(T:D) \rightarrow T:(T:D) \) applying the regimen in the world of theories about D, evolving the theory if needed

Clearly, a full and rigorous evaluation of software engineering research designs is a large and complex process. However, just as research is seldom done on the entirety of the domain of software engineering, so there is seldom a need for a full and complete evaluation of software engineering research design of the entire domain of software engineering. However, there is a need to do a full and rigorous evaluation of that part of the domain of software engineering on which research is conducted.

**Discussion of Examples.**

In the context of \( E:(D:D) \), there are several interesting examples. One is an instantiation of \( E:(T:D \rightarrow M:D) \). There is a common sub-theory of T:D that van Lamsweerde [12] and Brandozzi and Perry [3, 4] agree on: namely, that an architecture can be generated effectively from a formal goal-oriented requirements specification – that is, a structural model of a system can be generated from a goal-based theory. Not surprisingly, the two models are significantly different, as van Lamsweerde’s is based on using the structure of the theory to generate the structure of the model, where Brandozzi and Perry’s is based on the goals described in the theory to generate the structure of the model.

The evaluation of \( E:(T:D \rightarrow M:D) \) is provided in Jani et al. [11] (as discussed above) in which the strengths and weakness of each generation process and model are evaluated and described using a common goal-based theory.

Another example is found in Shao et al. [18] where there is a theory about software engineering, T:D, specifically a theory about models, T:D:M, such that changes to model D.M made under certain conditions are at increased risk of inserting faults with those changes. Basically, the theory T:D:M is that parallel changes to the same component are likely to cause semantic conflicts (text on text conflicts being seldom encountered). Further, it is more likely that these semantic conflicts occur in new features, less so in improvements, and least likely in bug fixes. A model was created for this theory, M:D.M, referred to as the Semantic Conflict Analyzer, that detects faults in D.M under the conditions described in the T:D:M. The specific evaluation \( E:(M:D) \) was performed in which it was determined that the model M was effective in detecting the predicted faults under the described theoretical conditions. In addition the evaluation determined what kinds of faults it would not detect. One way to view M:D.M, is as the regimen R in the evaluation that is applied two successive versions of D.M that expose semantic conflicts if they exist. Note that a different view is take in the different theory and model of E’ below.

**4.4 Evaluating Evaluations – E:E, E:E:D, and E:E:D:D**

In addition to evaluating designs, there is also a need to evaluate evaluations as well as evaluate evaluations of designs and evaluations of designing design, especially relative to issues of construct, internal, conclusion, and external validity. To evaluate the empirical theory E, we compose an atomic model of E with an open structured model of E giving the following eight models:  See Appendix 3 for the complete matrix of E:E with both E’s as open structured models.

- the evaluation of the elements of \( E_A:E_O \)
  - \( E:E \) evaluating the world of W of E
  - \( E:T \) evaluating the theory of T of E
  - \( E:H \) evaluating the hypothesis H of E
  - \( E:R \) evaluating the evaluation regimen R of E
The issues that need to be considered here are those concerning the adequacy of the evaluations and the effectiveness of the evaluation processes. Among the critical issues are those such as the appropriateness of the world \( W \) of possible Es, the completeness and consistency of the theory as well as its appropriateness and adequacy, the relevance of the hypothesis to the theory, the relevance of the empirical regimen to the hypothesis and theory, and the standard problems of construct, internal and external validity. Further there is the need to evaluate the quality of the theory derivation, hypothesis derivation, regimen generation, and the application and reconciliation processes.

In addition to evaluating our different forms of empirical evaluations themselves (\( E:E \)), there is also a need to evaluate specific evaluations of design in its various incarnations (for example, \( E:E:D \), evaluating evaluations of design, and \( E:E:D:D \) evaluating evaluations of designing design).

### 4.5 Designing Evaluations – \( D:E \) and \( D:E:E \)

The composition \( D:E \) represents the design of an empirical evaluation which is, again, a practical part of everyday software engineering. The composition \( D:E:E \) represents the design of an empirical evaluation of an empirical evaluation – that is, designing the evaluation to determine how good an evaluation is, which is more in the realm of software engineering research, but also a matter for practical software engineering as well. Further, given the composition discussed in the previous section – namely \( E:E:D \) and \( E:E:D:D \) – there is clearly a need for two further compositions: \( D:E:E:D \) to design the evaluation \( E:E:D \), and \( D:E:E:D:D \) to design the evaluation \( E:E:D:D \). It is easy to see how theoretical models increase significantly in multiple compositions. \( D:E:E:D \), for example has \( 6 \times 8 \times 8 \times 6 = 24,768 \) elements and mappings. Given this level of complexity it is extremely easy to see the utility of treating models as abstract rather than open structured. This use of atomicity provides a useful means of separating concerns – an extremely useful principle in software engineering, and clearly similarly useful in the exploration of theories and models about software engineering.

To design the empirical evaluation theory \( E \), compose an atomic model of \( D \) with an open structured model of \( E \), and an atomic model of \( D \) and \( E \) with an open structured models of the second \( E \), giving the following:

- the design
  - \( D:W \) & \( D:(E;W) \) of the world \( W \) of \( E \) and its evaluation
  - \( D:T \) & \( D:(E:T) \) of the theory \( T \) of \( E \) and its evaluation
  - \( D:H \) & \( D:(E:H) \) of the hypothesis \( H \) of \( E \) and its evaluation
  - \( D:R \) & \( D:(E:R) \) of the regimen of \( E \) and its evaluation
- the design of the processes, and their evaluations, of
  - \( D:(W \rightarrow T) \) & \( D:(E:(W \rightarrow T)) \) creating a theory \( T \) from world \( W \)
  - \( D:(T \rightarrow H) \) & \( D:(E:(T \rightarrow H)) \) creating an hypothesis \( H \) from theory \( T \)
  - \( D:(H \rightarrow R) \) & \( D:(E:(H \rightarrow R)) \) creating an evaluation regimen from hypothesis \( H \)
  - \( D:(R \times W \rightarrow T) \) & \( D:(E:(R \times W \rightarrow T)) \) evolving theory \( T \) as a result of the evaluation \( R \)

The design of empirical evaluations and the design of evaluating empirical evaluations (\( D:E \) and \( D:E:E \)) is analogous to \( D:D \): it is part of the software engineering research enterprise.

### 5. Alternative and More Complex Theories for \( D \) and \( E \)

In the discussions and examples above of the theories \( D \) and \( E \) and their various compositions, an extremely simpler version of these two base theories was deliberately used. In the case of the theory of design \( D \), the fact that design is both iterative and evolutionary was omitted. Similarly, in the case of \( E \), the theory of evaluation was deliberately simplified to make it easier to illustrate the issues of composition. In this section, both \( D \) and \( E \) are expanded to be more realistic, though in the case of \( D' \), still at a rather high level of abstraction. Evaluation theory \( E' \) represents classic experimental or quasi-experimental structures.

#### 5.1 An Iterative and Evolutionary Theory of Design – \( D' \)

The model of \( D' \) consists of three elements (objects) and six transformations (mappings, or processes). The elements are the same as the original formulation of \( D \):

- \( W \) the world, but more specifically, the part of the world relevant to the theory
- \( T \) the theory initiated by observations and abstractions
- \( M \) a model that reifies, represents or satisfies the theory \( T \)

The mappings involving these elements of the model are as follows:
generate a theory: observe and abstract from the world W to create a theory T
- T → M from the theory T create/evolve a model M
- T → T evolve theory T until satisfied
- M → M evolve the model M until satisfied
- M → T change the theory T to better conform to model M
- M * W → W inject model M into the world W thereby changing it (which depends on both the model and the world before the injection of the model into it).

The process of iteration includes T → T (refining and changing the theory until it is satisfactory), M → M (refining and changing the model until it is satisfactory), and M → T (providing feedback from the model M to evolve the theory T to bring it more in line with what is possible in the model M). The injection changes the world, M * W → W, induces a cycle of evolution for both the theory and its model. Obviously, other changes in the world induce the same cycle.

5.2 Refining the Model

The model M in D is a monolithic entity where in reality we typically consider the model to be comprised of three components: architecture, design, and code. The iterative theory can be extended from model D’ to R by replacing the various uses of M in D’ with elements A, D, and C (architecture, design, and code) and introduce a new element S (system) that is the result of “building” the code into a system.

- Replace M with A, D, and C
- Add a new object S and a mapping C → S
- T → M is replaced with T → A, T → D, and T → C
- M → T is replaced with A → T, D → T, and C → T
- M → M is replaced with
  - A → D, D → C
  - A → A, D → D, C → C
  - C → A, D → A, C → D
- Replace M * W → W with S * W → W

The new design theory and model R has 6 objects and 21 mappings. Obviously much more complex and the compositions considered above as basic are even more so. Small wonder that Brooks [2] considers complexity to be the most significant of the essential characteristics. Using the simple model E, the evaluation of R, E:R, has 8 * 27 = 216 elements and evaluations of E:R, E:E:R has 1728 elements. E’:R (the more complete evaluation theory in the next subsection) explodes even more.

5.3 A More Complete Evaluation Theory – E’

What is missing in E is the centrality of instruments as a critically important [8] element in empirical science. They are the lens through which we observe the world. To paraphrase Wittgenstein [22], the limits of my instruments are the limits of my world. They enhance, limit, and color our view of the world. In natural sciences, instruments are often physical creations; in behavioral sciences they are often intellectual creations. Humans are common instruments in both. Instruments may be active or passive. They may be theory-laden or transparent and neutral. They may be reliable and standardized or not. In any case, they are a critical part of the empirical apparatus and as such will play a critical part in any empirical evaluation endeavor.

Theory E’ then is described as follows:

- Given a theory, generate an hypothesis to test some part of the theory
- From the hypothesis, generate a regimen (that is, a treatment), and select or generate one or more instruments.
- The regimen is a treatment mechanism to generate desired data in the designated context.
- The instruments are used to provide observations about the generated data resulting from the manipulations of the independent variables.
- On the basis of the instrumented observations, generate a set of result analyses to use to reconcile the observations with the theory, revising the theory if needed.

Iteration is inherent in E’ as it is in both E and D. Revising T and generating new hypotheses, regimens and instruments to refine theory T. Theory E’ then provides a more realistic view of empirical evaluation ventures.

Of course, with the richer theory E’, the richer model needed to represent E’. The model of E’ has 8 objects and 7 mappings. The objects are as follows:

- T a theory
- H an hypothesis
- R a regimen (treatment) manipulates independent variables in context C
- C a context (where the independent and dependent variables are found) in which R is applied and observed by I
- D the data resulting from application of the regimen
• I  the instrument(s)
• O  the observations of the data D seen through instrument(s) I
• A  the analyses based on the observations

The mappings are as follows:

• T  H  deriving a hypothesis H from theory T
• H  I  creating appropriate instruments/mechanisms for observing the dependent variables
• H  R  creating appropriate regimen with manipulations of independent variables
• R*C  D  performing the experiment: apply regimen to context yielding resulting data
• I*D  O  using instrument I to provide observations of data D
• O  A  generating analyses from the observations O – i.e., drawing conclusions from the experiment
• A*T  T'  reconciling theory and reality (that is, the results of the analysis): evaluating T possibly revising T

An Example.

It is usually the case that D.T is a different theory from E.T. In the retrospective study [18], the two are indeed different but significantly related: E.T is a theory about the effects of changes in D.M; D.T is the theory about D.M itself – that is, a theory about detecting some of the effects of such changes.

Given the more detailed theory of E’, the Semantic Conflict Analyzer (SCA) is viewed as an instrument. The theory E.T is basically that software engineers need a reasonable amount of time to digest changes and to understand their implications. As a result of this, changes made concurrently, or at least within a reasonably short amount of time, are more likely to introduce faults. SCA (D.M) was designed and implemented to efficiently detect these interfering changes that result from semantic conflicts.

The null hypothesis H is that time intervals among changes have nothing to do with the likelihood of introducing faults. The regimen is to use SCA as the instrument I to analyze three populations of changes where the time intervals between changes are 1) a month or more, 2) a week or more but less than a month, and 3) less than a week. Also factored in is whether the changes represented bug fixes, improvements, or new features. The context C was change and version control databases in a large real-time project. Because the regimen is the application of SCA to these various programs the data D and observations O are the same: a set of semantic conflicts. The analysis A compared the set of semantic conflicts with the known sets of faults for the programs and determined which were relevant conflicts and which were false positives (conflicts where there were not faults – semantic interference often results from changing code intentionally) and which were were any false negatives (faults where there were no conflicts).

The null hypothesis was disproved and the study provided support for E.T:M that time is an important factor in the likelihood of faults. The results confirmed the theory that concurrency was a critical factor and that there were few unintentional conflicts in fixing bugs, a few more in making improvements, but semantic conflicts were very likely when introducing new features.

5.4 Evaluating the Alternative Evaluation Theory E’ – E’:E’

With the more complex theory and model of E’ comes a larger number of models as a results of the composition E’:E’ – 16 for E’:E’ instead of 9 for E:E. The taxonomic space is significantly larger as well – 225 elements instead of 64.almost a factor of 4 larger. The usefulness of the more complete theory and model is the exposure of what in many cases are critically important issues.

1) Using an Atomic E’ To Evaluate an Open-Structured e’. In this and the following sections we use E’ and e’ to distinguish the two uses of E’. In this and the next section, we also illustrate the usefulness in the atomic versus open-structured. In this case we consider E’ to be atomic, and used as a whole to evaluate the individual objects and mappings of e’.

• E’:t  evaluate the theory of e’
• E’:h  evaluate the hypothesis of e’
• E’:i  evaluate the instrument of e’
• E’:r  evaluate the regimen of e’
• E’:c  evaluate the context of e’
• E’:d  evaluate the data of e’
• E’:o  evaluate the observations of e’
• E’:a  evaluate the analyses used in e’
• E’:(t  h)  evaluate the derivation of the hypothesis of e’ from the theory of e’
• E’:(h  l)  evaluate the determination of the instrument for e’ from the hypothesis of e’
• E’:(l  r)  evaluate the design of the regimen derived from the hypothesis for e’
• E’:(r*e*d)  evaluate generation of data by means of the application of the regimen for evaluating e’ to its context
E':(t→d→u) evaluate the generation of observations from the data using the instruments of e'
E':(t→a) evaluate the derivations of the analysis from the observations for e'
E':(a→t→t) evaluate the reconciliation of the analysis and the theory and possibly revising the theory for e'

The interpretation of elements of the model E':e' may be as follows. E':t may evaluate theory completeness and consistency, or theory appropriateness and adequacy. E':h may evaluate the appropriateness of the hypothesis h relative to the theory t, or evaluate the construct validity of hypothesis h. E':r may consider the appropriateness of regimen r relative to hypothesis h and theory t, or consider the construct and/or internal validity of regimen r. E':c may evaluate the appropriateness of context c relative to theory t and hypothesis h. E':(t→h) may evaluate the quality of the hypothesis generation process, or evaluate construct validity. E':(h→r) may address the problems of construct and internal validity.

2) Using an Open-Structured E' To Evaluate Atomic e'. In this case, we consider E' to be open-structured and e' to be atomic, thus evaluating e' as a whole in terms of the individual elements of E'
The set of objects then in the composition of E':e' are as follows.
- T:e' a theory about evaluating e'
- H:e' an hypothesis about evaluating e'
- R:e' a regimen for evaluating e'
- C:e' a context for evaluating e'
- D:e' the data for e' resulting from the application of the regimen for evaluating e'
- I:e' the instrument(s) for evaluating e'
- O:e' the observations of the data seen through the instruments for evaluating e'
- A:e' the analyses based on the observations in evaluating e'

The set of mappings in the composition of E':e' are as follows:
- (T→H):e' = T:e' → H:e' Deriving an hypothesis for evaluating e' from the theory about evaluating e'
- (H→I):e' = H:e' → I:e' Determining an instrument to be used in the evaluation of e' from the hypothesis for evaluating e'
- (H→R):e' = H:e' → R:e' Deriving a regimen for evaluating e' from the hypothesis for evaluating e'
- (R*C→D):e' = R:e' * C:e' → D:e' Performing the evaluation of e' in the context for evaluating e' yielding the evaluation data for e'
- (I*D→O):e' = I:e' * D:e' → O:e' Applying the instrument for evaluating e' to the evaluation data for e', yielding evaluation observations about e'
- (O→A):e' = O:e' → A:e' Deriving an analysis of the evaluation of e' from the evaluation observations
- (A*T→T):e' = A:e' * T:e' → T:e' Reconciling the evaluation of e' with the theory about evaluating e' and possibly revising that theory.

3) Expanding the Details – Both Models Open-Structured. To understand fully the implication of what is hidden by keeping one of the models atomic (which does provide a useful abstraction in reducing the inherent complexity of model composition), consider an example from each of the preceding compositions to illustrate that complexity.

Consider a simple example from using E' to evaluate an object of e', E':t. The set of objects in this model is as follows:
- T:t a theory T about the theory t of e'
- H:t an hypotheses H about the theory t of e'
- I:t an instrument I used for theory t of e'
- R:t a regimen R used for the theory t of e'
- C:t a context C appropriate for theory t of e'
- D:t the data for the theory t of e'
- O:t the observations for the theory t of e'
- A:t the analysis relevant to the theory t of e'

These objects in the mappings of E' are then used for the evaluation of t.
- (T→H):t = T:t → H:t Generating an hypothesis H about t from the theory T about t
- (H→I):t = H:t → I:t Deriving an instrument I for t from the hypothesis H about t
- (H→R):t = H:t → R:t Deriving a regimen R about t from the hypothesis H about t
- (R*C→D):t = R:t * C:t → D:t Applying the regimen for t to the context of t to generate the data about t
- (I*D→O):t = I:t * D:t → O:t Using the instruments for t to yield observations about t from the data of t
- (O→A):t = O:t → A:t Deriving analyses about t from the observations on t
- (A*T→T):t = A:t * T:t → T:t Reconciling the analyses of t with the theory of t, possibly modifying the theory about t

In the second example where individual objects and mappings are applied to e' as a whole (that is, as atomic), to fully understand the implications, the structure of e' must be opened. Consider the example, (T→H):e' = T:e' → H:e'.

The set of objects then in the composition of E':e' are as follows.
- T:e' a theory about evaluating e'
- H:e' an hypothesis about evaluating e'
- R:e' a regimen for evaluating e'
- C:e' a context for evaluating e'
- D:e' the data for e' resulting from the application of the regimen for evaluating e'
- I:e' the instrument(s) for evaluating e'
- O:e' the observations of the data seen through the instruments for evaluating e'
- A:e' the analyses based on the observations in evaluating e'

The set of mappings in the composition of E':e' are as follows:
- (T→H):e' = T:e' → H:e' Deriving an hypothesis for evaluating e' from the theory about evaluating e'
- (H→I):e' = H:e' → I:e' Determining an instrument to be used in the evaluation of e' from the hypothesis for evaluating e'
- (H→R):e' = H:e' → R:e' Deriving a regimen for evaluating e' from the hypothesis for evaluating e'
- (R*C→D):e' = R:e' * C:e' → D:e' Performing the evaluation of e' in the context for evaluating e' yielding the evaluation data for e'
- (I*D→O):e' = I:e' * D:e' → O:e' Applying the instrument for evaluating e' to the evaluation data for e', yielding evaluation observations about e'
- (O→A):e' = O:e' → A:e' Deriving an analysis of the evaluation of e' from the evaluation observations
- (A*T→T):e' = A:e' * T:e' → T:e' Reconciling the evaluation of e' with the theory about evaluating e' and possibly revising that theory.
The instruments I and regimens R (i.e., treatments) may be human and opportunistic when doing exploratory work, or a predictive one. The hypothesis H may be generic and open-ended when doing exploratory work, or focused and specific when doing explanatory work (typically using a null hypothesis or a well-formed and mature when doing explanatory work (typically using a null hypothesis or a well-designed in both cases when doing explanatory work). Reconciliation of theory and reality may result in theory generation when doing exploratory work, or adding support for the theory or revising it when doing explanatory work.

With respect to the issues of validity, the various elements of E’ constitute the following:

- **Construct validity** – (the most critical issue for design decisions) is addressed by at least E':h, E':i, and E':(h→i)
- **Internal validity** – is addressed by at least E':h, E':i, E':r, E':(h→r), E':(r→c→d), and E':(c→d→o)
- **Statistical validity** – is addressed by at least E':a, E':(o→a), and E':(a→t→t')
- **External validity** – is addressed at least E':c

An interesting question is whether the E’ should be used to evaluate itself or whether some other theory and model, perhaps simpler, should be used instead – for example, E, or perhaps a theory and model that focuses directly on validity issues. As seen above, the taxonomic space is large using E’ to evaluate itself. This is not necessarily a bad thing as it does have the utility of illustrating just how large and complex the problem is of evaluating our evaluations. The simpler theory E hides a large amount of that complexity. Further exploration of this issue is needed to understand the utility, strengths and weaknesses of alternative approaches.

### 6. Applying the Framework to Other Theories

So far the validation of this framework and approach to a theory for software engineering and software engineering research has been basically an existence proof with some illustrative examples or discussions. – that is, showing that it it is useful in exploring a theory of software engineering and software engineering research as a set of compositions of two simple theories. In this section, the framework is applied to a variety of other theories about various aspects of software engineering to illustrate its validity and utility with respect to these theories.

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3 The same question can be asked with respect to designing design: is D an appropriate theory and model for the software engineering research? Since much of what is produced in software engineering research are software techniques, software methods, software process, and software systems, it does seem to be an appropriate theory and model. Still it is something to be given further consideration.
6.1 Multiple Viewpoints Requirements Engineering based Software Engineering

An example of such a more detailed theory and model is that of Nuseibeh, Kramer and Finkelstein’s multiple viewpoints [14] approach in which there are different stakeholders with respect to the problem to be solved; these stakeholders have different views on what is important in the theory – i.e., requirements that need to be captured; and eventually any and all apparent and real conflicts need to be resolved to provide a consistent theory (i.e., a consistent set of requirements). One of the interesting facets of this work is the emphasis on the tolerance of inconsistency. While it was not mention, there is the implicit recognition of the existence of inconsistency in D’ between D’.T and D’.M in the mutual interaction between them. While inconsistency is tolerated, eventually inconsistencies have to be addressed and resolved, here by a set of rules: “In-Viewpoint check actions are those actions that can be performed to check that a specification is syntactically consistent. Inter-Viewpoint check actions, are those actions that can be performed to check the consistency between (overlapping or interacting) specifications residing in different Viewpoints.” [14] Their approach is basically that of lazy consistency evaluation on an as-needed basis. Ultimately, however, all inconsistencies need to be resolved.

1) Theory V (Viewpoints)

The added details to theory V are primarily in the generation of a theory that is then the basis for creating the corresponding model.

- Multiple stakeholders observe and abstract some specific part of the world and create a part of a theory that is relevant to them.
- These stakeholders’ partial theories eventually must be merged into a consistent single theory using consistency rules (and their supporting tools).
- From that theory a usable model is created to reify or represent that theory.
- The theory is iteratively adjusted (and sometimes the stakeholders’ partial theories) and the model is also adjusted as the understanding of the theory and its model evolves, both iteratively and interactively.
- When satisfied that the model adequately represents the theory, the model is injected into the world.
- Injecting the model into the world changes the world.
- The changes brought about by the model’s injection into the world as well as other changes in the world often lead to adjustments and extensions to the stakeholders partial theories and the eventually merged theory.
- Changes to the theory in turn lead to further changes in the model and the world.

So, theory iteration becomes more complex and in turn makes the iteration between the theory and model more complex as well.

2) Model V

For the most part, the theory of D is carried over into V. Similar to the architecture, design, code refinement of D’ discussed above, V is a refinement on the structure of deriving the theory T that is changed and provided in more detail

- W the world, but more specifically, the part of the world relevant to the theory
- S the stakeholders who create partial theories
- P partial theories
- R rules (and their supporting tools) for detecting and resolving inconsistencies
- T the theory resulting from merging partial theories
- M a model that reifies, represents or satisfies the theory T

The mappings involving these elements of the model are as follows:

- S+ * W P+ stakeholders generate partial theories: observe and abstract from the W to create partial theories P+
- P+ * R T the partial theories are merged into a consistent theory
- T * R P+ the partial theories are adjusted due to consistency issues in theory T
- T M evolve theory T until satisfied
- T M from the theory T create/evolve a model M
- M M evolve the model M until satisfied
- M T change the theory T to better conform to model M
- M W W inject model M into the world W thereby changing it (which depends on both the model and the world before the injection of the model into it).

A possible alternative to T P+ to capture the process of theory consistency issues resulting from either inconsistencies in the partial theories P+ or changes in the theory T to better to conform to the model M is to use instead a much more complex mapping: T R (S+ * W P+). This mapping would represent the process of the theory T generating a new set of partial theories by the various stakeholders. In T R P+, the need for the stakeholders themselves to modify their partial theories is implicit rather than explicit.

As always, then, how models reify their theories is a creative process often with various alternatives of perhaps differing utility and clarity. And, there is usually a tradeoff between simplicity and expressiveness.

3) Compositions with V

...
6.2 People-Centered Software Engineering

Adolph and Kruchten, in their GTSE workshop paper [1], argue that people are central, even dominant, in the software engineering enterprise: “the main concern of people involved in the process of software development is getting the job done and that different points of view and expectations create impediments – a perspective mismatch”. When a perspective mismatch is discovered, people converge their mismatched perspectives by negotiating a consensual perspective (similar to theory V above – the primarily difference is there is a logical calculus to determine inconsistency in the specifications of the viewpoints – here people detect and then negotiate the resolution of differences). These consensual perspectives are viewed as forming a set of “integrated hypotheses” that are used to produce a grounded theory [7] to explain the behavior of various participants.

In what follows, the term “observations” is used (for the sake of simplicity) for Adolph’s and Kruchten’s “consensual perspectives” or grounded theory’s “hypotheses” in the discussion of their approach. Their theory P includes E and extends D and E:D. At an abstract level, theory P adds four new elements and three extended theory mappings (based on D and E) for P:

- P: person, typically a software engineer
- O: observations (negotiated perspectives, hypothesis)
- R: researcher (a special subset of P)
- T: theory of software engineering
- P+ * D \rightarrow O+: one or more people derive one or more observations about creating/evolving design
- P+ * (E:D) \rightarrow O+: one or more people derive one or more observations about evaluating design
- R+ * O+ * T \rightarrow T: one or more researchers create or modify a theory of SE using the derived observations

To make these abstractions more concrete, D is expanded to make it clearer what P entails. People P are also involved in the evaluation E (using the simplified E for sake of clarity) of the expanded D.

- P+ * W \rightarrow O+: P+ * E:W \rightarrow O+  
- P+ * T \rightarrow O+: P+ * E:T \rightarrow O+  
- P+ * M \rightarrow O+: P+ * E:M \rightarrow O+  
- P+ * (W \rightarrow T) \rightarrow O+: P+ * E:(W \rightarrow T) \rightarrow O+  
- P+ * (T \rightarrow M) \rightarrow O+: P+ * E:(T \rightarrow M) \rightarrow O+  
- P+ * (M \rightarrow W \rightarrow T) \rightarrow O+: P+ * E:(M \rightarrow W \rightarrow T) \rightarrow O+  
- R+ * O+ * T \rightarrow T

I add to further mappings to represent people providing observations about people and observations as part of creating/evolving T.

- P+ * P \rightarrow O+  
- P+ * O \rightarrow O+

Further, E needs to be expanded as well to indicate the full range of observations that need to be provided to fully ground the resulting theory of software engineering – This is left as an exercise for the reader. At this point a full model of P has been defined.

P itself now needs to be evaluated, just as the theory of design D needed to be evaluated as represented by E:D. The following is the list of elements in evaluating P, E:P:

- E:(P+ * W \rightarrow O+): E:(P+ * E:W \rightarrow O+)  
- E:(P+ * T \rightarrow O+): E:(P+ * E:T \rightarrow O+)  
- E:(P+ * M \rightarrow O+): E:(P+ * E:M \rightarrow O+)
The evaluations of the mappings appear to be, and, indeed are, complicated. To get the evaluation half of software engineering, we compose E with F:

- \( E:(P^+ * P \rightarrow O^+) \)
- \( E:(P^+ * O \rightarrow O^+) \)
- \( E:(P^+ * (W \rightarrow T) \rightarrow O^+) \) \( E:(P^+ * E:(W \rightarrow T) \rightarrow O^+) \)
- \( E:(P^+ * (T \rightarrow M) \rightarrow O^+) \) \( E:(P^+ * E:(T \rightarrow M) \rightarrow O^+) \)
- \( E:(P^+ * (M^*W \rightarrow T) \rightarrow O^+) \) \( E:(P^+ * E:(M^*W \rightarrow T) \rightarrow O^+) \)
- \( E:(R^+ * O^+ * T_\omega \rightarrow T_\omega) \)

To illustrate what E:P implies, take a look at the one of these mappings and expand E it to an open structure. One of the more interesting of the elements is \( E:(P^+ * (T \rightarrow M) \rightarrow O^+) \) – that is, evaluating the generation of peoples’ observations about the process of producing a model from a theory. Considering E as an open structured model provides objects as follows (using a bold italics to represent the open-structured E). For ease of differentiation E from P, red is used for the objects and mappings of E.

- \( W:(P^+ * (T \rightarrow M) \rightarrow O^+) \) A world of people’s observations about deriving a model from a theory
- \( T:(P^+ * (T \rightarrow M) \rightarrow O^+) \) A theory about evaluating people’s observations about deriving a model from a theory
- \( H:(P^+ * (T \rightarrow M) \rightarrow O^+) \) An hypothesis to test about people’s observation about deriving a model from a theory
- \( R:(P^+ * (T \rightarrow M) \rightarrow O^+) \) A regimen for evaluating people’s observations about deriving a model from a theory

The evaluations of the mappings appear to be, and, indeed are, complicated.

- \( (W \rightarrow T) : (P^+ * (T \rightarrow M) \rightarrow O^+) = W:(P^+ * (T \rightarrow M) \rightarrow O^+) \rightarrow T:(P^+ * (T \rightarrow M) \rightarrow O^+) \) Deriving a theory about peoples observations about deriving a model from a theory from the world of peoples observations about deriving a model from a theory
- \( (H \rightarrow R) : (P^+ * (T \rightarrow M) \rightarrow O^+) = H:(P^+ * (T \rightarrow M) \rightarrow O^+) \rightarrow R:(P^+ * (T \rightarrow M) \rightarrow O^+) \) Deriving an hypothesis about peoples observations about deriving a model from a theory from a theory of peoples observations about deriving a model from a theory
- \( (R^*W \rightarrow T) : (P^+ * (T \rightarrow M) \rightarrow O^+) = R:(P^+ * (T \rightarrow M) \rightarrow O^+) \rightarrow W:(P^+ * (T \rightarrow M) \rightarrow O^+) \rightarrow T:(P^+ * (T \rightarrow M) \rightarrow O^+) \) Reconciling the results of a regimen evaluating peoples observations about deriving a model from a theory, with the world of peoples observations about deriving a model from a theory, possibly modifying the evaluated theory

The rest of the evaluations follow the same pattern. The composition delineates the full taxonomy of what it means to evaluate the theory P via the composition of its model with the model of E. The notion of an evaluation represented with E is very broad where that of E’ is much more narrow and the composition E’:P much more complex.

### 6.3 Algebraic Refinement

Having taken a very traditional approach to design and evaluation in D and E, it is worthwhile to consider a very non-traditional approach such as that of Batory’s Feature Oriented Programming [2].

“Feature Oriented Programming (FOP) is a design methodology and tools for program synthesis. The goal is to specify a target program in terms of the features that it offers, and to synthesize an efficient program that meets these specifications”

Batory has created an algebra used to describe how features are composed together to create a system. Design rules define what comprises a legal composition by delineating the semantic constraints that need to be met for a proper composition. Compositions are expressed as algebraic equations that are then used, with the design rules and the supporting tools, to synthesize the system composition from the individual feature components. Evolution of the system is then a matter of synthesizing a new system by evolving the algebraic equations to incorporate new features or to eliminate no longer desired features. The algebraic approach and the design rules are innovative but the lynchpin are the underlying tools that enable the use of the equations and rules to synthesize a system from the set of features.

As done earlier, a simplified version of his approach is presented (leaving out iteration – that can be done by the reader as an intellectual exercise). The elements in Batory’s design theory F, which extends and modifies D, are as follows:

- \( W \) world
- \( T \) theory
- \( F \) feature
- \( A \) algebra
- \( R \) design rule
- \( M \) model
- \( W \rightarrow T \) derive a theory from the world
- \( T \rightarrow F+ \) derive features from the theory
- \( (A * R^+ * F^+ \rightarrow M) \) derive a model from the features via the algebra and design rules
- \( M * W \rightarrow W \) inject the model into the world

To get the evaluation half of software engineering, we compose E with F:

- \( E:W \) evaluate the relevant world
- \( E:T \) evaluate the theory
In making this distinction, it is important to emphasize the centrality and criticality of theory in both software engineering and software evaluation, both of which are critical parts of software engineering and research.

There are two important points: 1) the usefulness of theories and models, and 2) the important distinction between design and evaluation. The motivation for this research is to create a unifying theoretical basis for software engineering and research. It is necessary to make these underpinning theories more explicit and central, especially in research.

Based on the number of elements in F, D, and E (10, 6, and 8 respectively) the taxonomic spaces for these four compositions are as follows:

<table>
<thead>
<tr>
<th>Composition</th>
<th>Number of Elements</th>
</tr>
</thead>
<tbody>
<tr>
<td>D:F</td>
<td>60</td>
</tr>
<tr>
<td>D:E:F</td>
<td>480</td>
</tr>
<tr>
<td>E:D:F</td>
<td>480</td>
</tr>
<tr>
<td>E:D:E:F</td>
<td>3840</td>
</tr>
</tbody>
</table>

Obviously things get much more complicated if we instead used D’ and E’ in the compositions with their respective element counts of 9 and 15. The main point is that the taxonomic space grows significantly the more complex the theories and their models. The likelihood that one would cover, or perhaps even need to cover, all of these elements is small, especially in the richer compositions. However, the taxonomies do provide a space where once can locate precisely where one’s research focus lies and which of the taxonomic elements one’s research and evaluation cover.

7. Conclusions

The motivation for this research is to create a unifying theoretical basis for software engineering and research. In particular there are two important points: 1) the usefulness of theories and models, and 2) the important distinction between design and evaluation, both of which are critical parts of software engineering and research.

In making this distinction, it is important to emphasize the centrality and criticality of theory in both software engineering and software engineering research. Too often, little is explicit in the underlying theoretical basis of the work in software engineering and research. It is necessary to make these underpinning theories more explicit and central, especially in research.
Similarly, it is important to emphasize the centrality and criticality of empirical evaluations in both enterprises as well. Too little attention is paid to the evaluation part of software engineering and software engineering research with the primary, and sometimes sole, emphasis put on design (obviously critically important in its own right). There is an important need for a more explicit, systematic, and deeper approach to empirical evaluations in both software engineering and software engineering research.

D is proposed as the theoretical basis for the design part of software engineering, and theory E as the theoretical basis for the empirical evaluation part (which is the composition E:D). These two theories and the composed theories then lay out a rich space (a taxonomy, or ontology if you will) for all of software engineering and software engineering research.

From these two theories there is a set of various composed theories that focus on various aspects of design and evaluation. The first composition is that of E:D representing the empirical evaluation part of software engineering. The composition of D with itself, D:D, yields the design portion of software engineering research, while E:D:D provides the empirical evaluation of the design of research. The empirical evaluations themselves need to be empirically evaluated and E composed with itself, E:E, provides that. Of course, there is then the design of the empirical evaluations that are represented with the compositions D:E and D:E:E.

The goal of this research has been to illustrate the very rich space that can be define using small and relatively simple theories – especially in this case making D’ and E’ slightly richer than D and E. The beauty of this approach is that the composition of these theories and their models extend our understanding and illuminate the taxonomic space for the resulting theories and their models. The ability to designate models as atomic or open structured enables the control of level of complexity in compositions, enabling also the separation of various concerns.

Moreover, this approach is even more general than that. Such design disciplines as project management, instrument creation and evolution, empirical studies themselves are also models of these atomic and composed theories – that is, they are design disciplines and hence models for the theories of design disciplines that have been presented and alluded to.

Finally, there are a number of useful properties in this approach: 1) a theory modeling language and calculus for composing the resulting theoretical models; 2) the utility of the two levels of abstraction (atomic and open-structured) that are used to provide an intuitive high level abstraction, and the explicit low level details; 3) regularity among the various theories; 4) a scientific elegance in creating larger more complex theories out of simpler theories; and 5) an elegant way of explaining the complexity of software systems, software engineering and software engineering research.

8. Acknowledgements

This research was sponsored in part by NSF CISE SRS Grant CCF-0820251. My thanks also to Don Batory for a willingness to listen and comment.

9. References


Appendix 1 – E:D Matrix with both E and D as open structured models

The first row (in italics) is E as atomic model and D as a open structure model; the first column (in italics) is E as an open structure model and D as an atomic model. The remaining columns and rows show the results of both models as open structured.

<table>
<thead>
<tr>
<th>E:D</th>
<th>E:W</th>
<th>E:T</th>
<th>E:M</th>
</tr>
</thead>
<tbody>
<tr>
<td>W:D</td>
<td>W:W</td>
<td>W:T</td>
<td>W:M</td>
</tr>
<tr>
<td>T:D</td>
<td>T:W</td>
<td>T:T</td>
<td>T:M</td>
</tr>
<tr>
<td>H:D</td>
<td>H:W</td>
<td>H:T</td>
<td>H:M</td>
</tr>
<tr>
<td>R:D</td>
<td>R:W</td>
<td>R:T</td>
<td>R:M</td>
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</tbody>
</table>

<table>
<thead>
<tr>
<th>E:(W → T)</th>
<th>E:(T → M)</th>
<th>E:(M → W)</th>
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<tr>
<td>H:(W→T)</td>
<td>H:(T→M)</td>
<td>H:(M→W)</td>
</tr>
<tr>
<td>R:(W→T)</td>
<td>R:(T→M)</td>
<td>R:(M→W)</td>
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</tbody>
</table>
Appendix 2 – D₁:D₂ Matrix with both Ds as open structured models

The first row (in italics) is D₁ as atomic model and D₂ as a open structure model; the first column (in italics) is D₁ as an open structure model and D₂ as an atomic model. The remaining columns and rows show the results of both models as open structured.

<table>
<thead>
<tr>
<th>D₁:D₂</th>
<th>D₁:D</th>
<th>D₁:T</th>
<th>D₁:M</th>
</tr>
</thead>
<tbody>
<tr>
<td>W:D</td>
<td>W:W</td>
<td>W:T</td>
<td>W:M</td>
</tr>
<tr>
<td>T:D</td>
<td>T:W</td>
<td>T:T</td>
<td>T:M</td>
</tr>
<tr>
<td>M:D</td>
<td>M:W</td>
<td>M:T</td>
<td>M:M</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>D₁:(W → T)</th>
<th>D₁:(T → M)</th>
<th>D₁:(M*W → W)</th>
</tr>
</thead>
<tbody>
<tr>
<td>T:(W → T)</td>
<td>T:(T → M)</td>
<td>T:(M*W → W)</td>
</tr>
<tr>
<td>M:(W → T)</td>
<td>M:(T → M)</td>
<td>M:(M*W → W)</td>
</tr>
</tbody>
</table>
Appendix 3 - E₁:E₂ Matrix with both Es as open structured models

The first row (in italics) is E₁ as atomic model and E₂ as a open structure model; the first column (in italics) is E₁ as an open structure model and E₂ as an atomic model. The remaining columns and rows show the results of both models as open structured.