Fall 2024 EE 313 Linear Systems and Signals Prof. Evans

Homework #8

# Continuous-Time Frequency Response and Intro to Fourier Transform

Assigned on Sunday, November 17, 2024

Due on Friday, November 22, 2024, by 11:59 pm via Gradescope submission

*Late homework is subject to a penalty of two points per minute late*.

***Reading***: McClellan, Schafer & Yoder, *Signal Processing First*, 2003, Sections 10.1-11.4.

Companion Web site with demos and other supplemental information: <http://dspfirst.gatech.edu/>

Web site contains solutions to selected homework problems from *DSP First*.

Office hours for Prof. Evans follow. Prof. Evans is also available immediately after lecture.

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| ***Time Slot*** | ***Monday*** | ***Tuesday*** | ***Wednesday*** | ***Thursday*** | ***Friday*** |
| 11:00am – 12:30pm |  | Evans (ECJ 1.204) |  | Evans (ECJ 1.204) |  |
| 12:30pm – 2:00pm |  |  |  |  |  |
| 2:00pm – 3:30pm |  |  | Evans (EER 6.882; [Zoom](https://utexas.zoom.us/j/92416635120)) |  |  |
| 3:30pm – 5:00pm | Evans (EER 6.882; [Zoom](https://utexas.zoom.us/j/93660425176)) |  | Evans (EER 6.882; [Zoom](https://utexas.zoom.us/j/92416635120)) |  |  |
| 5:00pm-6:30pm |  |  |  |  |  |
|  |  |  |  |  |  |
| 7:00pm-8:30pm | [Tutoring](http://www.ece.utexas.edu/academics/tutoring) in EER 0.814 |  |  | [Tutoring](http://www.ece.utexas.edu/academics/tutoring) in EER 0.814 |  |
| 8:30pm-10:00pm | [Tutoring](http://www.ece.utexas.edu/academics/tutoring) in EER 0.814 |  |  | [Tutoring](http://www.ece.utexas.edu/academics/tutoring) in EER 0.814 |  |

Th homework assignment is the first two problems from homework #8 in Fall 2023.

1. **Continuous-Time System Properties. *48 points.***

*Signal Processing First*, problem P-9.2, page 279.

1. **Continuous-Time Averaging Filters. *52 points.***

For a continuous-time LTI system with input signal and impulse response , the output signal is the convolution of and :

1. Compute the output when the input is a rectangular pulse of amplitude 1 for and amplitude 0 otherwise and is filtered by an LTI unnormalized averaging filter whose impulse response is a rectangular pulse of amplitude 1 for and amplitude 0 otherwise. Assume .
   1. Write an equation relating output and input . *6 points*
   2. What is(are) the initial condition(s) and what value should it(they) be set to? *5 points*
   3. Develop a formula for using the convolution definition in terms of . Show the intermediate steps in computing the convolution. *9 points*
   4. Validate the formula for to compute the convolution for *6 points*
2. When an input signal has an average value of zero, i.e. the DC component is zero, an LTI integrator can be used as an averaging filter. The differential equation governing the input-output relationship is
   1. What is(are) the initial condition(s) and what value should it(they) be set to? *5 points*
   2. What is the impulse response? *6 points*
   3. Develop a formula for using the convolution definition when the input signal is . Note that has bounded amplitude. *9 points*
   4. Is the LTI integrator bounded-input bounded-output (BIBO) stable? Your work in part iii might be helpful. *6 points*

As stated on the course descriptor, “Discussion of homework questions is encouraged. Please be sure to submit your own independent homework solution.”

NOTE: In your solutions, please put all work for problem 1 together, then all work for problem 2 together, etc. Please see additional homework guidelines on the homework page.

Please read the [homework guidelines](http://users.ece.utexas.edu/~bevans/courses/signals/homework/index.html).