**Tune-Up Tuesday for September 7, 2021**

% (a) Copy, paste and run the Matlab code from lecture slide 1-16 to generate  
% the cosine signal *x*(*t*) = cos(2 *f*0 *t*) with *f*0 = 440 Hz and play it as an audio  
% signal for 3s at a sampling rate of *f*s = 8000 Hz. (Using a higher standard  
% audio sampling rate such as 96000 Hz would give a smoother plot in part (d)).

**% (a) ‘A’ note on** [**Western scale**](https://en.wikipedia.org/wiki/Piano_key_frequencies) **in 4th octave (A4) @ 440 Hz**

**f0 = 440; % note ‘A4’**

**fs = 8000; % sampling rate**

**Ts = 1/fs; % sampling time**

**t = 0 : Ts : 3; % 3 seconds**

**x = cos(2\*pi\*f0\*t);**

**sound(x, fs);  
pause(3);**

% (b) Add to the code in (a) to generate a new signal *y*(*t*) = cos(2 *f*0 *t*) cos(2 *f*1 *t*)  
% with *f*1 = 110 Hz by using the same sampling rate of *f*s = 8000 Hz.

**% (b) Multiply cosine @ 440 Hz and cosine @ 110 Hz**

**% Modified code from left side of lecture slide 3-3.**

**f1 = 110;**

**x1 = cos(2\*pi\*f1\*t);**

**y = x .\* x1;**

% (c) Add to the code in (b) to playing *y*(*t*) as an audio signal.  
% Describe what you hear.  
% Express y(t) as a sum of two sinusoids.

**% (c) Play y(t) at a sampling (playback) rate 8000 Hz.**

**% I hear two notes/tones at a lower pitch than 440 Hz.**

**% The product can be written as a sum of two cosines.**

**% Using the result from lecture slide 3-2,**

**% y(t) = 0.5 cos(2 pi 330 t) + 0.5 cos(2 pi 550 t)**

**% Tones at 330 Hz (E4) and 550 Hz (C#5) are**

**% harmonics of 110 Hz. See** [**Piano frequencies**](https://en.wikipedia.org/wiki/Piano_key_frequencies)**.**

**sound(y, fs);**

% (d) Plot one period of y(t). We'll need to find the periodicity of y(t).  
% The product of two sinusoids at frequencies f0 and f1 produces  
% frequencies at f0+f1 and f0-f1. You could modify the code from the  
% bottom right side of lecture slide 3-3.

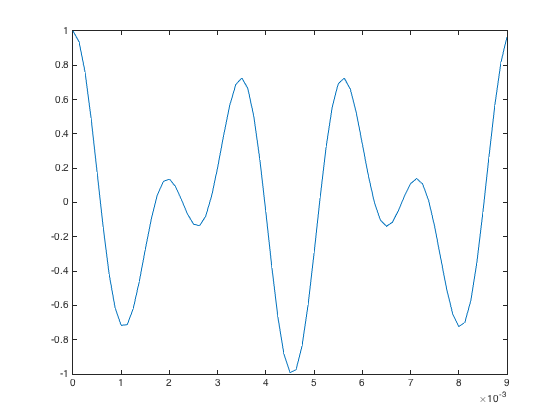
**ffund = gcd(f0+f1, f0-f1); % 110 Hz which is note ‘A2’**

**Tfund = 1/ffund;**

**n = round(Tfund / Ts); % Tfund / Ts isn’t an integer.**

**plot( t(1:n), y(1:n) );**

% See the next page for the plot.



Non-smooth troughs