

# **THE FSM DOMAIN**

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## **OUTLINE**

1. Motivations
2. Specification of FSMs
3. Embedding of FSMs:
  - into the SDF domain
  - into the DDF domain
  - into the SR domain
4. Adding hierarchy
5. Comparison with ARGOS

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## **MOTIVATIONS**

**Control:** clean control structure in PTOLEMY

**Heterogeneity:** keep the usual PTOLEMY philosophy: a new domain

## **DOMAIN of VALUES**

Each signal has 3 states: “unknown” ( $\perp$ ), “absent” ( $\varepsilon$ ) and “present with value  $v$ ” ( $v$ )

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## **SPECIFICATION**

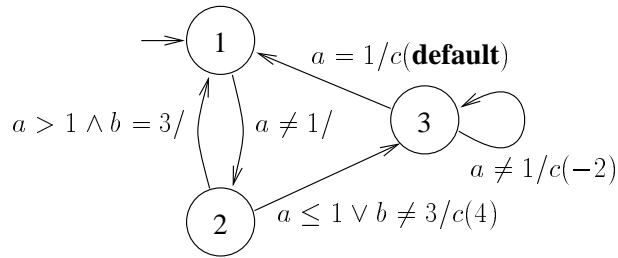
$$\langle I, O, Q, q_0, T \rangle$$

where:

- $I$  is a set of input signals,
- $O$  is a set of output signals,
- $Q$  is a set of states,
- $q_0 \in Q$  is the initial state, and
- $T$  is a set of transitions of the form *guard\_part/action\_part*

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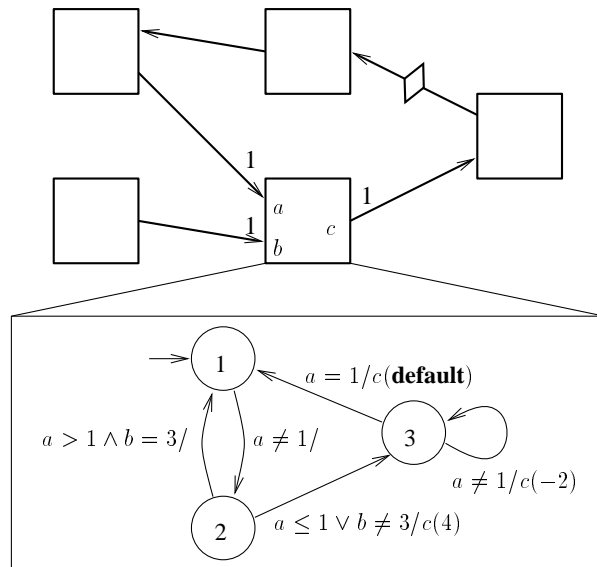
### EXAMPLE



current state	1	2	3	3	3	1	1	2	...
<i>a</i>	0	0	3	8	1	1	7	4	...
<i>b</i>	1	5	0	-4	5	4	1	2	...
next state	2	3	3	3	1	1	2	3	...
<i>c</i>	ε	4	-2	-2	0	ε	ε	4	...

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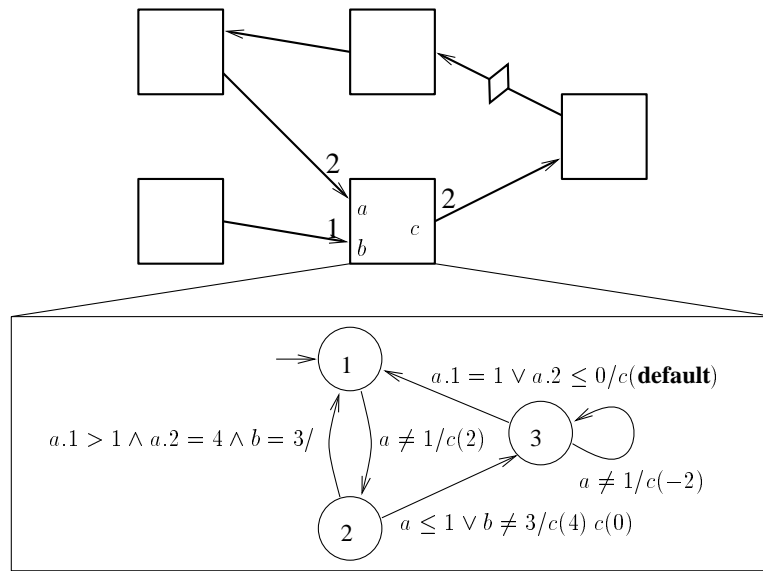
### EMBEDDING into SDF



SDF semantics: a token **must** be produced on transition from state 1 to state 2  $\Rightarrow$  label  $a \neq 1/c(\mathbf{default})$

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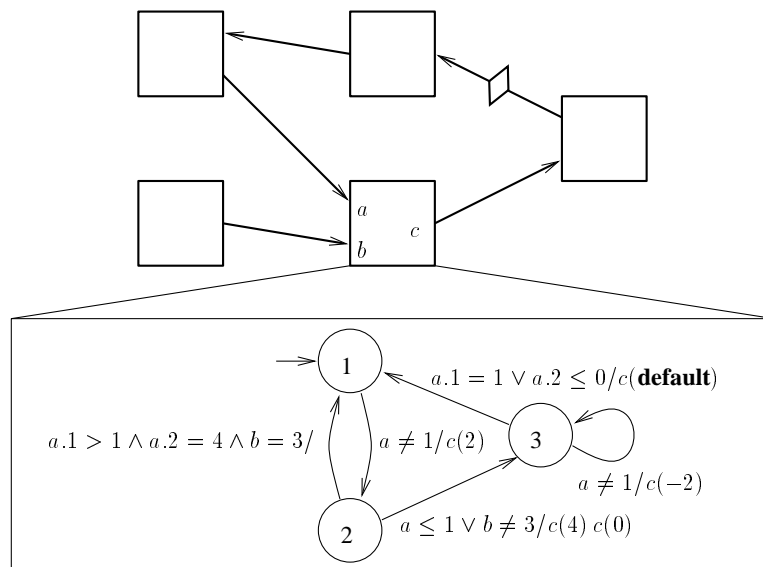
## NON HOMOGENEOUS CASE



SDF semantics: two tokens **must** be produced on transition from state 1 to state 2  $\Rightarrow$  label  $a \neq 1 / c(2) c(\mathbf{default})$

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## EMBEDDING into DDF



DDF semantics: additional tokens are **never** produced  
Need to consume a number of token sufficient to evaluate all the guards

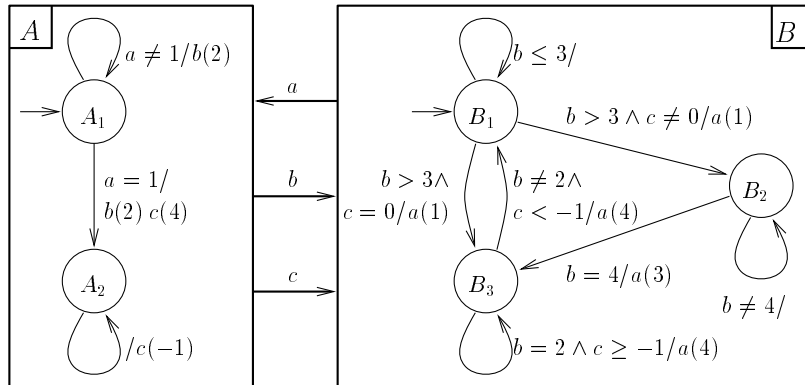
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## EMBEDDING into SR

Handling instantaneous loops:

1. partial order on the values of the wires
2. block functions must be monotonic w.r.t. this partial order

Partial evaluation algorithm for FSMs



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## PARTIAL EVALUATION

state 1: functions  $\mathcal{O}_b^1$  and  $\mathcal{O}_c^1$

$a$	$-\infty$	$1$	$+\infty$
$b$	$2$	$2$	$2$
$c$	$\varepsilon$	$4$	$\varepsilon$

For any state  $s$  and any output  $o$ :

$$\begin{cases} \text{if } \exists v : \forall x, \mathcal{O}_o^s(x) = v \text{ then } \mathcal{O}_o^s(\perp) = v \\ \text{else } \mathcal{O}_o^s(\perp) = \perp \end{cases}$$

state 1: extended functions  $\mathcal{O}_b^1$  and  $\mathcal{O}_c^1$

$a$	$-\infty$	$1$	$+\infty$	$\perp$
$b$	$2$	$2$	$2$	$2$
$c$	$\varepsilon$	$4$	$\varepsilon$	$\perp$

## **EXECUTION EXAMPLE**

1. start with  $(a, b, c) = (\perp, \perp, \perp)$
2. execute  $B$ :  $a = \mathcal{O}_a^1(\perp, \perp) = \perp$
3. execute  $A$ :  $b = \mathcal{O}_b^1(\perp) = 2$  and  $c = \mathcal{O}_c^1(\perp) = \perp$
4. execute  $B$ :  $a = \mathcal{O}_a^1(2, \perp) = 1$
5. execute  $A$ :  $b = \mathcal{O}_b^1(1) = 2$  and  $c = \mathcal{O}_c^1(1) = 4$

**Theorem:** The extended output functions are monotonic w.r.t. to the partial order

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## **ADDING HIERARCHY**

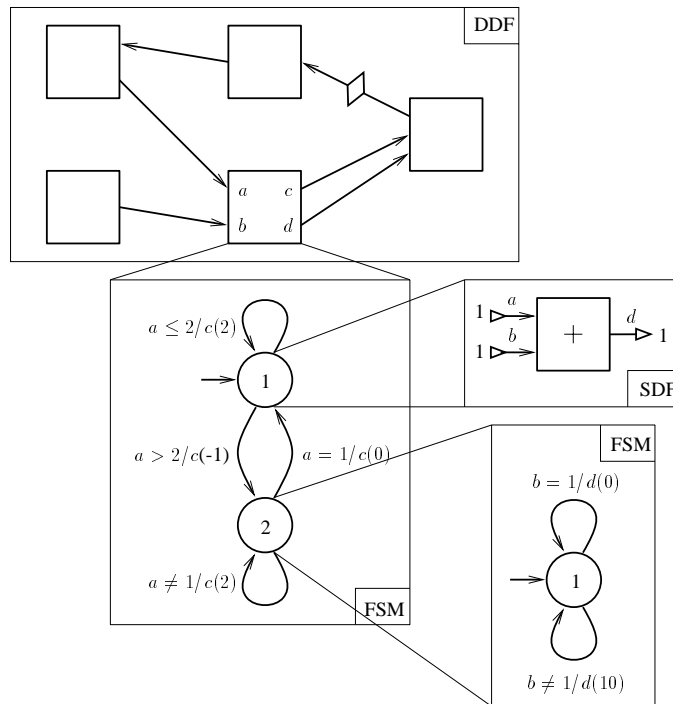
**Executing an FSM:** execute the current state & select and fire a transition (same set of inputs, distinct sets of outputs, internal events)

**Executing a data-flow network:** perform a complete execution cycle of the network (hierarchical blocks are executed according to their respective domain)

**Executing an SR network:** find the behavior (least fixed point) of the network (each block must compute a monotonic function)

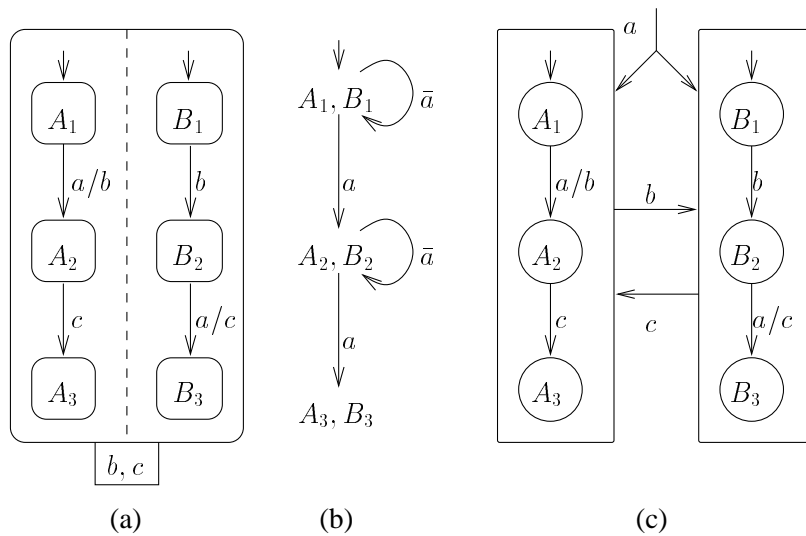
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## HIERARCHICAL EXAMPLE



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## COMPARISON with ARGOS



The SR scheduler will generate  $A.B.A$  or  $B.A.B$

In both cases, the network goes from state  $(A_1, B_1)$  to  $(A_2, B_2)$

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