

***Fast Rehalftoning and  
Interpolated Halftoning with  
Flat Low-Frequency Response***

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## *Outline*

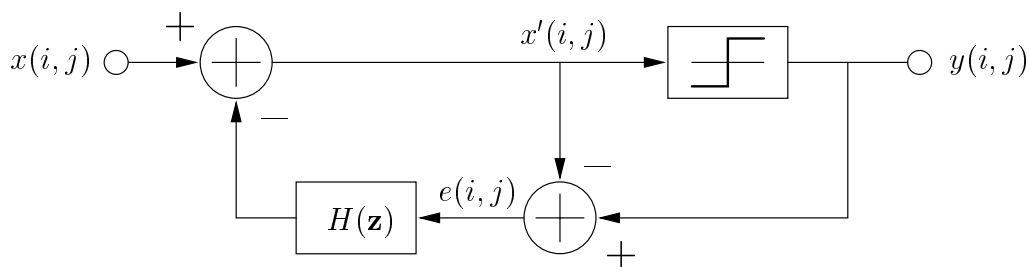
- Introduction to halftoning
- Halftoning by error diffusion
- Rehalftoning
  - ▶ Algorithm
  - ▶ Results
- Interpolated halftoning
  - ▶ Algorithm
  - ▶ Results
- Computational requirements
- Conclusion

# ***Introduction to Halftoning***

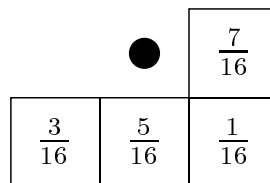
- **Word length reduction for images**
  - ▶ 8-bit to 1-bit for grayscale
  - ▶ 24-bit RGB to 8-bit for color displays
  - ▶ 24-bit RGB to CMYK for color printers
  
- **Applications**
  - ▶ Printers
  - ▶ Digital copiers
  - ▶ Liquid crystal displays
  - ▶ Video cards
  
- **Halftoning methods**
  - ▶ Screening
  - ▶ Error diffusion
  - ▶ Direct binary search
  - ▶ Hybrid schemes
  
- **Consider grayscale error diffusion**

# Halftoning by Error Diffusion

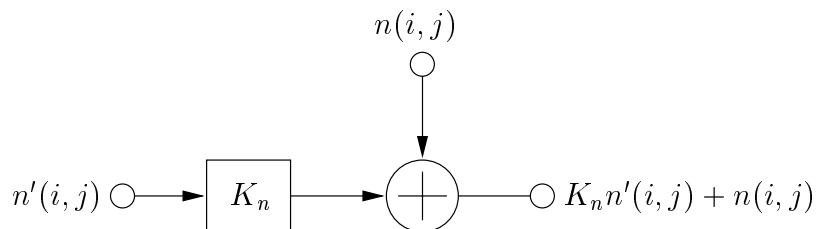
- 2-D delta-sigma modulator
- Noise shaping feedback coder



- Error filter



- Model by linearizing quantizer

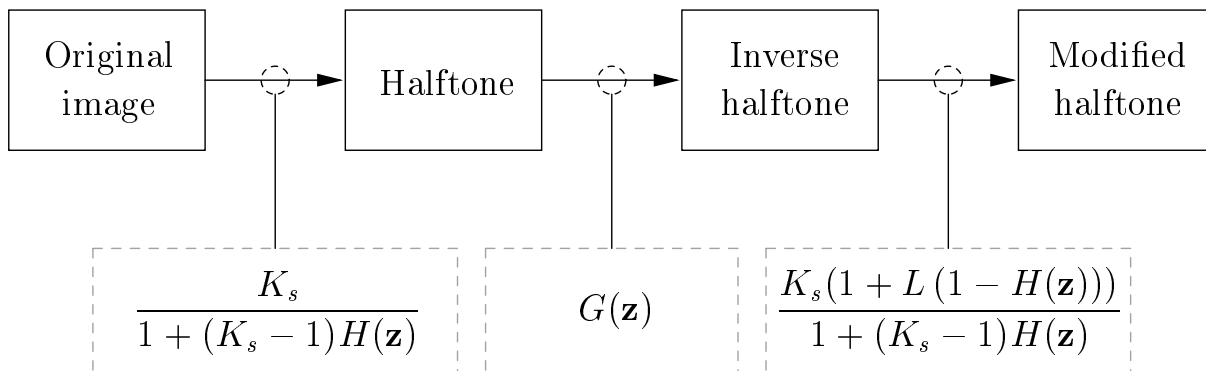


- $K_n = 1$  for error diffusion
- $K_s \approx 2$  for Floyd-Steinberg filter

# ***Rehalftoning***

- **Different halftoning methods in use**
  - ▶ Laser printer: ordered screening
  - ▶ Inkjet printer: error diffusion
- **Optimal rendering of halftone for a particular device**
  - ▶ Inverse halftone to grayscale image
  - ▶ Rehalftone grayscale image
- **Inverse halftoning is expensive**
  - ▶ Use simple inverse halftoning method
  - ▶ Artifacts concealed
  - ▶ Response errors corrected in halftoning
- **Use modified error diffusion**  
[Eschbach and Knox, 1991]
  - ▶ Sharpness control parameter  $L$
- **Assume input and output are error diffused halftones**

# Rehalftoning Algorithm



Block diagram of rehalftoning system

- Convert one error diffused halftone into another error diffused halftone
- Inverse halftone with  $4 \times 4$  filter
  - ▶ Symmetric FIR filter
  - ▶ Zeros at band edges
  - ▶ 6-bit output resolution
- Set sharpness control parameter  $L$  to flatten system response at low frequencies
  - ▶  $L \approx 0.188$  for Floyd-Steinberg filter

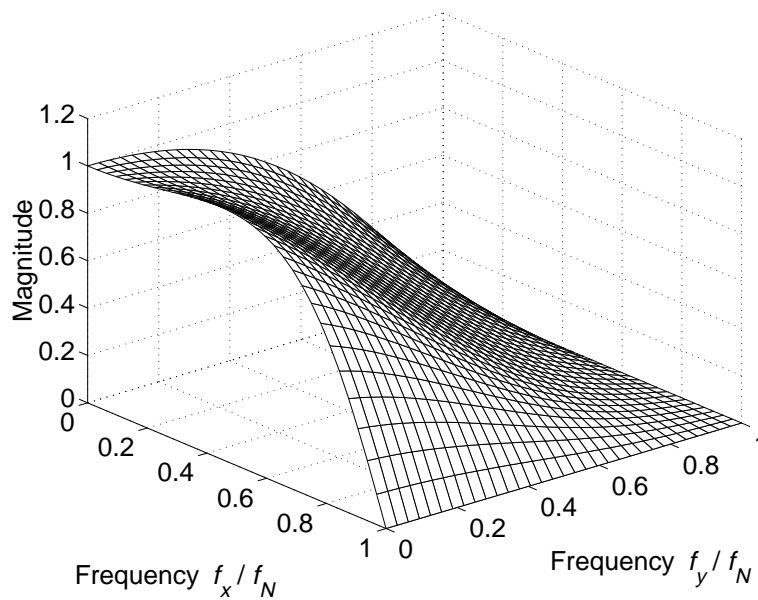
# Rehalftoning Results



Original image



Rehalftone



End-to-end signal transfer function

# *Interpolated Halftoning*

- Image resizing
- Methods in increasing complexity
  - ▶ Nearest neighbor
  - ▶ Bilinear
  - ▶ Bicubic, cubic splines, lowpass filtering
- Nearest neighbor, bilinear methods
  - ▶ Low computational cost
  - ▶ Artifacts masked by quantization noise in halftone
  - ▶ Blurring correctable by modified error diffusion
- Examine  $\times 2$  interpolation
  - ▶ Method applies to any scaling factor
  - ▶ Design  $L$  for flat transfer function using linear gain model of the quantizer
  - ▶  $L$  constant for an interpolation method



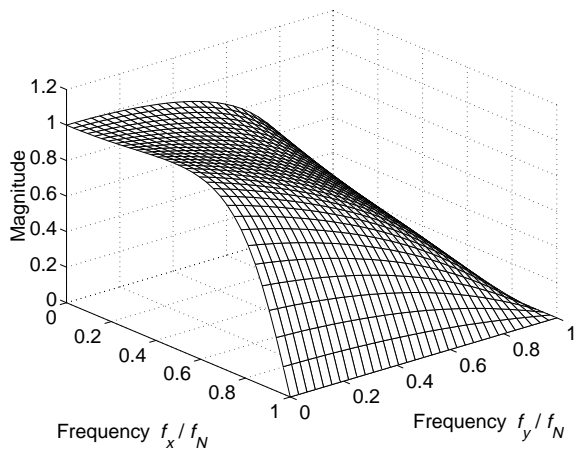
# Interpolation Results



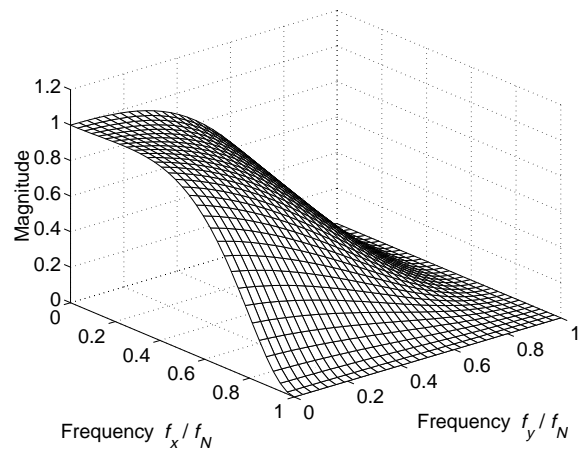
Nearest neighbor  $\times 2$



Bilinear  $\times 2$



Transfer function  
 $L = -0.0105$



Transfer function  
 $L = 0.340$

## ***Computational Requirements***

- **Rehalftoning per pixel**
  - ▶ 34 increments (++)
  - ▶ 12–28 integer additions
  - ▶ 4 integer multiplications
  - ▶ 2 bit shifts
  
- **Rehalftoning a  $512 \times 512$  image**
  - ▶ Computation: 16 million operations
  - ▶ Memory usage: 2060 bytes
  
- **$\times 2$  interpolation per pixel**
  - ▶ 2 increments (++)
  - ▶ 9.67 integer additions
  - ▶ 4 integer multiplications
  - ▶ 3 bit shifts
  
- **$\times 2$  interpolation on  $512 \times 512$  image**
  - ▶ Computation: 5 million operations
  - ▶ Memory usage: 1024 bytes

## ***Conclusion***

- Rehalftoning needed for scanning, processing, and reprinting
- Interpolation needed for resizing in printing and copying
- Developed algorithms for error diffused halftones
  - ▶ Rehalftoning & interpolated halftoning
  - ▶ Flat low-frequency end-to-end response
- Efficient implementation
  - ▶ Local memory
  - ▶ Integer arithmetic
  - ▶ Suitable for embedded implementation
- Web site for software and papers  
<http://www.ece.utexas.edu/~bevans/projects/inverseHalftoning.html>