ROLLING SHUTTER CAMERA TRACKING AND VIDEO RECTIFICATION USING VISUAL AND INERTIAL MEASUREMENTS

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Overview

- Rolling shutter effects
- Previous work using IMUs
- Sensor fusion
 - Feature point correspondence in rolling shutter camera
 - EKF-based sensor fusion
 - Outlier detection using 1-point RANSAC
- Experiments and comparison

Rolling Shutter Effects

- Handheld cameras fast motion
- CMOS image sensors:



Rows in sensor array are exposed sequentially from top to bottom



Rolling shutter effects:



Rectify Rolling Shutter Effects

- Pose estimation for each row needed
- Pure rotational model
 - Main cause of pose difference between rows
 - Fast rectification

 $\mathbf{u} \sim \mathbf{KR}(t(\mathbf{u}, j))\mathbf{x}$ $\mathbf{u}' \sim \mathbf{KR}((t_j)\mathbf{R}^T(t(\mathbf{u}, j))\mathbf{K}^{-1}\mathbf{u}$

- Previous work on pose estimation
 - [Karpenko 2011]
 - Integrate gyro readings (100Hz on Nexus S)
 - Use SLERP for exposure time between samples
 - Unknown bias and noise; Fast changing motion
 - [Hanning 2011]
 - EKF-based estimation with accelerometer readings as measurements
 - acceleration = f (pose, gravity)
 - Good loop closing property
 - Gravity is not the only source of acceleration

Proposed Method

- Gyro readings integrated with visual measurements
- Feature point correspondences provide accurate geometric clue
 - Structure from Motion; Simultaneous Localization and Mapping (SLAM)
 - How to relate matched features with high-frequency camera poses in rolling shutter model
 - How to effectively detect outliers
- Research platform
 - Android smartphones (Google Nexus S)
 - Use app "data logger" to record video and gyro readings (with timestamp) at the same time
 - How to synchronize sensor measurements

Gyro and Feature Point Correspondence

• Gyro returns measurements with higher sampling rate



Compute the relative rotation between two exposure time

$$\mathbf{R}(t(\mathbf{u}', i+1))\mathbf{R}^{T}(t(\mathbf{u}, i)) = \prod_{n=k+1}^{k+4} \Delta \mathbf{R}(\omega_{n} \Delta t_{n})$$
$$\Delta \mathbf{R}(\omega_{n} \Delta t_{n}) = \exp(\operatorname{skew}(\omega_{n}) \Delta t_{n})$$

EKF-based Estimation

State vector: two groups of angular velocities

$$\mathbf{x}_i = [\omega(i-1,1),\ldots,\omega(i-1,N_{i-1}),\omega(i,1),\ldots,\omega(i,N_i)]^T$$

- Why two groups?
 - The visual measurements depend on both the group of the current frame and the group of the previous frame
- Why angular velocity instead of rotation representation (unit quaternion)
 - Equivalent for relative rotation estimation
 - No SLERP needed (simple Jacobian in EKF)
- Probabilistic Graphical Model



Dynamic Motion Model (State Prediction)

• Group cloning in prediction



$$\mathbf{x}_i = \left[egin{array}{c} \mathbf{x}_{i,1} \ \mathbf{x}_{i,2} \end{array}
ight] = \left[egin{array}{c} \mathbf{x}_{i-1,2} \ \mathbf{y}_i \end{array}
ight] + \left[egin{array}{c} \mathbf{0} \ \mathbf{w}_i \end{array}
ight]$$

Linear model

$$A_{i} = \left. \frac{\partial f}{\partial \mathbf{x}} \right|_{\mathbf{x}_{i-1}} = \left[\begin{array}{cc} \mathbf{0} & I \\ \mathbf{0} & \mathbf{0} \end{array} \right], W_{i} = \left. \frac{\partial f}{\partial \mathbf{w}} \right|_{\mathbf{w}_{i}} = \left[\begin{array}{c} \mathbf{0} \\ I \end{array} \right]$$

Measurement Model (State Update)

 Use only feature points in current frame as the measurements; their matching points in previous frame are used as parameters

$$\mathbf{u}_{i,j} = g\left(K\Delta RK^{-1} \begin{bmatrix} \mathbf{u}_{i-1,j} & -\mathbf{v}_{i-1,j} \\ 1 & 1 \end{bmatrix} + \mathbf{v}_{i,j}\right)$$

state vector determines the relative rotation
$$\prod_{k=1}^{N_{i-1}} \Delta R(\omega(i-1,k)\Delta t_{i-1,j,k}) \prod_{k=1}^{N_i} \Delta R(\omega(i,k)\Delta t_{i,j,k})$$

measurement noise

- Final measurement equation for state update
 - Closed form Jacobian matrix using chain rule

$$\mathbf{z}_{i} = \begin{bmatrix} \mathbf{u}_{i,1} \\ \mathbf{u}_{i,2} \\ \vdots \\ \mathbf{u}_{i,M} \end{bmatrix} = \begin{bmatrix} h_{1}(\mathbf{x}_{i}, \mathbf{u}_{i-1,1} - \mathbf{v}_{i-1,1}) + \mathbf{v}_{i,1} \\ h_{2}(\mathbf{x}_{i}, \mathbf{u}_{i-1,2} - \mathbf{v}_{i-1,2}) + \mathbf{v}_{i,2} \\ \vdots \\ h_{M}(\mathbf{x}_{i}, \mathbf{u}_{i-1,M} - \mathbf{v}_{i-1,M}) + \mathbf{v}_{i,M} \end{bmatrix}$$



- State prediction of current stage is correlated with the noise of the observation (measurements) in previous stage
- Solution: augment the state vector with the measurement noise

Outliers Removal

- For global shutter model
 - Epipolar constraint / Homography fitting
- 1-point RANSAC in EKF
 - In standard RANSAC, each hypothesis need the minimum number of points necessary to estimate the parameters
 - For EKF, we have got a prior distribution of the parameters (state vector) by prediction
 - The minimum number of points to estimate the parameters can be reduced to one (in the rolling shutter case we choose three)

Outlier Removal

- Track features using the state prediction result, refine by KLT
- inliers = []
- for i = 1 to N_hyp
 - randomly choose 3 matches
 - update the states through EKF filtering
 - computer the re-projection error (innovation) and choose current_inliers
 - if num_current_inliers > max_num
 - inliers = current_inliers
 - max_num = num_current_inliers

end

Use inliers to compute the EKF update

75ms/frame in Matlab implementation on 2.3GHz Intel i5 processor 20 features tracked

Sensor Synchronization and Calibration

Parameters

 $J = \sum_{i=1}^{n}$

- Rolling shutter speed (actual exposure time)
- Intrinsic parameters of the camera
- Delay between timestamps of IMUs and video
- Batch optimization [Karpenko 2011]
 - Camera intrinsic parameters initialized by Zhang's self-calibration
 - Get relative rotation from gyro readings
 - Optimize over all matching points, minimize the average re-projection error
 - Solve by Levenberg-Marquardt algorithm

$$\mathbf{u} - \mathbf{K}\mathbf{R}(t(\mathbf{u}, i+1))\mathbf{R}^{T}(t(\mathbf{v}, i))\mathbf{K}^{-1}\mathbf{v}||^{2}$$



convergence of synchronization & calibration

Average Re-projection Error per Point

RANSAC EKF vs. Integrating gyro readings



- Zero-angle test
 - Start with cell phone on a plat surface
 - Rotate cell phone at will, then put it back on the surface and stay still for several seconds
 - Repeat for ten times
 - Ground truth available naturally for pitch and roll















Using unbiased gyro readings



Roll angle estimation error (rad)



Using unbiased gyro readings

Using unbiased gyro readings



Pitch angle estimation error (rad)







gyro



gyro + cam



gyro + cam



gyro + cam

• Complete failure using gyro + accel



Numerical Comparison

- No ground truth \rightarrow no-reference method
- Vanishing point check
 - Lines detected manually
 - Find vanishing point by least-square

Average Euclidean distance from the lines to the vanishing point (in pixel)



