# Real-Time 3D Rotation Smoothing for Video Stabilization 

Chao Jia, Zeina Sinno, and Brian L. Evans<br>Department of Electrical and Computer Engineering The University of Texas at Austin

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## Introduction

- Video recording by handheld cameras is growing exponentially due to:
- Compactness
- Everywhere \& Anytime
- Easy Sharing
- Good User Experience (touchscreen)

Common Problem: Unwanted inter-frame jitter ...

## Introduction

Why online video stabilization

- Real-time delivery: video conferencing, broadcasting, etc.
- Improved user experience: What You See is What You Get.
- More efficient compression



## Online Video Stabilization

- Removing unwanted jitter (inter-frame correction)



## Motion Model Selection

- 2D motion: apparent pixel displacements
Translation Similarity Euclidean Affine Projective
- 3D real camera motion

Rotation Full (Rotation + Translation)

| Motion <br> Model | Estimation <br> Complexity | Smoothing <br> Effectiveness <br> low | Correction <br> Complexity <br> low |
| :--- | :--- | :--- | :--- |
| 2D | high | high | high |
| 3D Full | high | high | low <br> (projective transform) |
| 3D Rotation | low <br> (using gyro) |  | ( |

- No approximation in 3D rotational stabilization (proposed method)
- We are not assuming pure camera rotation
- Translation is kept as is, and not smoothed


## Online 3D Rotation Smoothing

- Classical approaches for 2D motion models
- ( $1^{\text {st }}$ order low-pass) IIR filtering
- Kalman filtering with constant-velocity (CV) model
- Extension to 3D rotation smoothing
- Euclidean space $\rightarrow$ SO(3) manifold
- Ad-hoc projection for black-border constraint


## 3D Rotation Matrix

- Manifold of 3D Rotation Matrices
- Special Orthogonal Group $\quad \mathbf{S O}(\mathbf{3}) \mathbf{R R}^{\mathrm{T}}=\mathbf{I}$
- An embedded submanifold in $\mathbb{R}^{9}($ dimension $=3)$

Tangent Space $T_{x} M$

Tangent Vector

- Minimizing Geodesic \& Geodesic Distance

$$
d_{g}\left(\mathbf{R}, \mathbf{R}^{\prime}\right)=\left\|\operatorname{logm}\left(\mathbf{R}^{-1} \mathbf{R}^{\prime}\right)\right\|_{F}
$$

## Constrained Motion Smoothing

- Inevitably some pixels are not visible after view change


$$
\begin{aligned}
{\left[\begin{array}{c}
\tilde{u}_{i j} \\
\tilde{v}_{i j}
\end{array}\right]=g } & \left(\mathbf{K} \tilde{\mathbf{R}}_{i} \mathbf{R}_{i}{ }^{\mathrm{T}} \mathbf{K}^{-1}\left[\begin{array}{c}
u_{i j} \\
v_{i j} \\
1
\end{array}\right]\right) \\
& \begin{array}{l}
\text { Correction by } \\
\text { image warping }
\end{array}
\end{aligned}
$$

$$
\left\{\begin{array} { l } 
{ 0 \leq \tilde { u } _ { i j } \leq w } \\
{ 0 \leq \tilde { v } _ { i j } \leq h }
\end{array} \quad , \forall [ \begin{array} { l } 
{ u _ { i j } } \\
{ v _ { i j } }
\end{array} ] \text { s.t. } \left\{\begin{array}{l}
c_{1} \leq u_{i j} \leq c_{2} \\
d_{1} \leq v_{i j} \leq d_{2}
\end{array}\right.\right.
$$

Hard Constraint: All of the pixels in the cropped new frame should be visible in the original frame.

## IIR-like 3D Rotation Smoothing

- First-Order IIR filtering

$$
\hat{\boldsymbol{\theta}}_{k}=\alpha \hat{\boldsymbol{\theta}}_{k-1}+(1-\alpha) \boldsymbol{\theta}_{k} \quad \mathrm{SO}(3) x
$$

$$
\hat{\boldsymbol{\theta}}_{k}=\underset{\boldsymbol{\theta}}{\operatorname{argmin}} \alpha\left\|\boldsymbol{\theta}-\hat{\boldsymbol{\theta}}_{k-1}\right\|^{2}+(1-\alpha)\left\|\boldsymbol{\theta}-\boldsymbol{\theta}_{k}\right\|^{2}
$$

$$
\hat{\mathbf{R}}_{k}=\underset{\mathbf{R}}{\operatorname{argmin}} \alpha d_{g}\left(\mathbf{R}, \hat{\mathbf{R}}_{k-1}\right)^{2}+(1-\alpha) d_{g}\left(\mathbf{R}, \mathbf{R}_{k}\right)^{2} \underset{\text { linear }}{\text { spherical }}
$$

interpolation (SLERP)

- Ad-hoc projection $\hat{\mathbf{R}}=\mathbb{P}\left(\hat{\mathbf{R}}^{*}\right)=\mathbf{R e x p m}\left(\beta^{*} \operatorname{logm}\left(\mathbf{R}^{-1} \hat{\mathbf{R}}^{*}\right)\right)$


Move closer to the original rotation if necessary for black-border constraint

## UKF-based 3D Rotation Smoothing

- Constant-Velocity Model (widely used in target tracking)

- Hard to solve on SO(3)
- Nonlinear on Euclidean space
- Solved approximately by unscented Kalman filter (UKF)


## Proposed Algorithms

```
Algorithm . IIR-like 3D Rotation Smoothing
    Input: \(\mathrm{q}_{1}, \cdots, \mathrm{q}_{K}\) (original rotations)
    Output: \(\hat{\mathbf{q}}_{1}, \cdots, \hat{\mathbf{q}}_{K}\) (smoothed rotations)
    \(\hat{\mathbf{q}}_{1}=\mathbf{q}_{1}\)
    for \(k=2\) to \(K\) do
        \(\hat{\mathbf{q}}_{k}=\operatorname{slerp}\left(\mathbf{q}_{k}, \hat{\mathbf{q}}_{k-1}, \alpha\right)\)
        \(\hat{\mathbf{q}}_{k} \leftarrow \mathbb{P}\left(\hat{\mathbf{q}}_{k}\right)\)
    end for
```

$1.54 \mathrm{~ms} /$ frame

```
Algorithm _ UKF-based 3D Rotation Smoothing
    : Input: \(\mathrm{q}_{1}, \cdots, \mathrm{q}_{K}\) (original rotations)
    2: Output: \(\hat{\mathbf{q}}_{1}, \cdots, \hat{\mathbf{q}}_{K}\) (smoothed rotations)
    3: Parameters: \(\mathbf{Q}, \mathbf{R}\) (process and measurement noise vari-
    ance)
    for \(k=1\) to \(K\) do
    : Obtain unconstrained UKF estimate \(\hat{\mathbf{q}}_{k}^{*}, \hat{\boldsymbol{\omega}}_{k}^{*}, \mathbf{P}_{k}\)
    6: \(\quad \hat{\mathbf{q}}_{k}^{*}=\hat{\mathbf{q}}_{k}^{*} /\left\|\hat{\mathbf{q}}_{k}^{*}\right\|_{2}\) (normalization)
    7: \(\quad \hat{\mathbf{q}}_{k} \leftarrow \mathbb{P}\left(\hat{\mathbf{q}}_{k}\right)\)
    8: (Mean and covariance estimate to pass to the next stage
    are \(\hat{\mathbf{q}}_{k}, \hat{\boldsymbol{\omega}}_{k}, \mathbf{P}_{k}\) )
    9: end for
```

$6.97 \mathrm{~ms} /$ frame

## Experimental Results - 2D vs. 3D KF



2D Affine KF


3D Rotational UKF


## Experimental Results- 2D vs. 3D KF




## Experimental Results- 2D vs. 3D IIR




## Experimental Results - 2D vs. 3D IIR



3D Rotational IIR


## Thanks!

## Backup - Pure Rotation

Camera Projection


## Backup - Pinhole Camera Model



## Backup - Camera Model \& Camera Motion



World Coordinates $\rightarrow$ Camera Coordinates

$$
\left[\begin{array}{c}
x_{s} \\
y_{s} \\
1
\end{array}\right] \sim\left[\begin{array}{llc}
f & 0 & c_{x} \\
0 & f & c_{y} \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{l}
x_{c} \\
y_{c} \\
z_{c}
\end{array}\right] \longmapsto\left[\begin{array}{c}
x_{c} \\
y_{c} \\
z_{c}
\end{array}\right]=\mathbf{R}\left(\left[\begin{array}{c}
x \\
y \\
z
\end{array}\right]+\left[\begin{array}{c}
t_{x} \\
t_{y} \\
t_{z}
\end{array}\right]\right)
$$

