

# Analog-to-Digital Converter Circuit and System Design to Improve with CMOS Scaling

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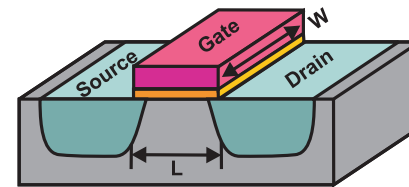
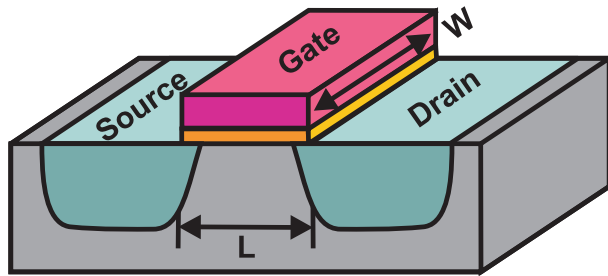
PHD DEFENSE

April 16, 2015

COMMITTEE MEMBERS

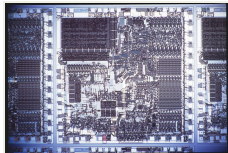
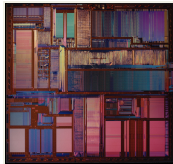
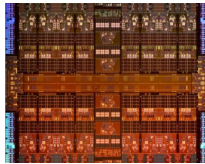
Brian L. Evans                      Arjang Hassibi  
Todd E. Humphreys    Earl E. Swartzlander, Jr.  
Ahmed H. Tewfik

# CMOS Scaling of Digital Integrated Circuits



Metal-Oxide-Semiconductor (MOS) Transistor

- Scaling CMOS transistor dimensions results in
  - exponential increase in number of transistors per chip [[Moore's law](#)]
  - lower capacitance, delay, active power dissipation, cost

Feature size	3 $\mu\text{m}$	0.8 $\mu\text{m}$	16 nm
# of Transistors	29K	3.1M	10B+
Die Photo/Year			
	Intel x86 (1978)	Intel Pentium (1993)	Oracle Sparc M7 (exp: 2015)

Source: [http://en.wikipedia.org/wiki/Transistor\\_count](http://en.wikipedia.org/wiki/Transistor_count)

# CMOS Scaling of Mixed-Signal/Analog Circuits

- Analog circuits generally don't scale like digital circuits
- State-of-the art CMOS processes are **digital-friendly**,  
**but analog-hostile**



## Good:

reduced: capacitance, active power  
increased: speed



## Bad:

reduced: supply voltage, voltage headroom

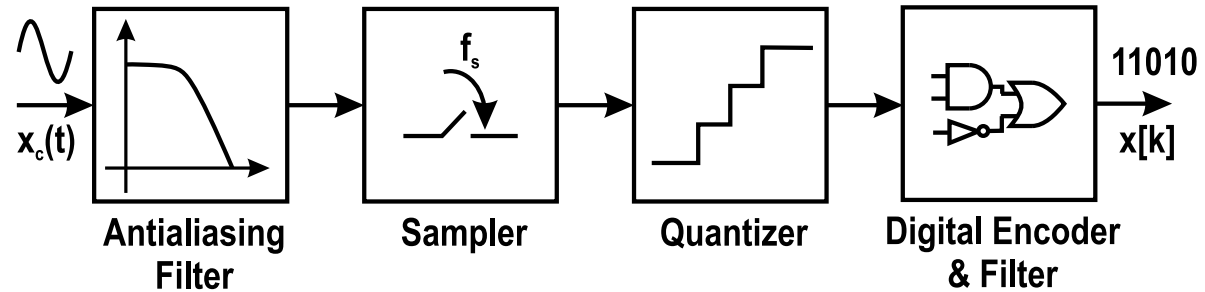


## Ugly:

increased: mismatch, noise, short-channel effects, nonlinearity  
reduced: intrinsic transistor gain, signal-to-noise ratio, dynamic range

# Analog-to-Digital Converters

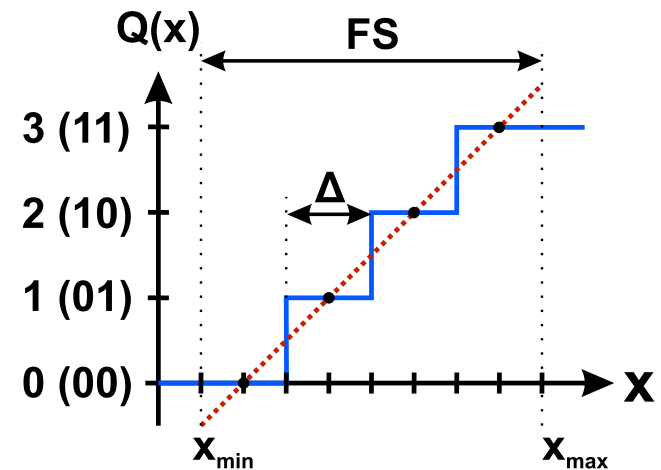
- Typical ADC:



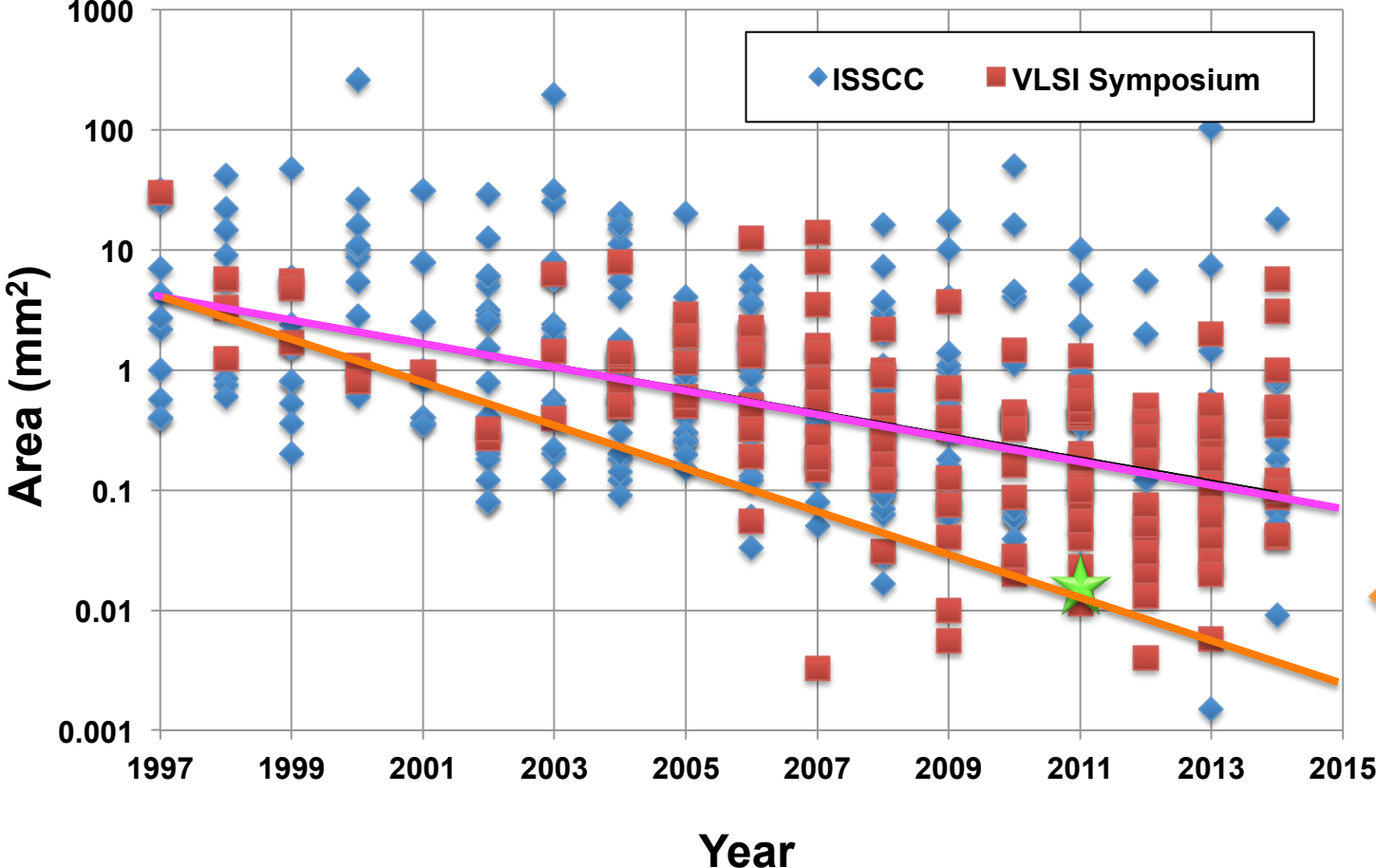
- Antialiasing filter (ideally) enforces band-limitedness to BW
- Sampling is lossless if  $f_s > 2$  BW (Nyquist rate)
- Quantization is lossy, *i.e.* it adds noise

$$\sigma_q^2 = \frac{\Delta}{12} \quad \Delta = \frac{FS}{2^N}$$

- Signal-to-quantization noise ratio:  
SQNR = 6.02 N + 1.76 (dB)



# Analog-to-Digital Converter Area Trend



B. Murmann, "ADC Performance Survey 1997-2015," [Online]. Available: <http://web.stanford.edu/~murmann/adcsurvey.html>.

# Contributions

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## Analog-to-Digital Converter Circuit and System Design to Improve with CMOS Scaling

### Time-Based Delta Sigma ADC Architecture & Modeling

- Novel architecture with loop delay calibration
- Combines time-based information processing & noise shaping

### Two Prototype ADC Chips

- Prototype chips demonstrate proof of concept
- Among smallest area in literature

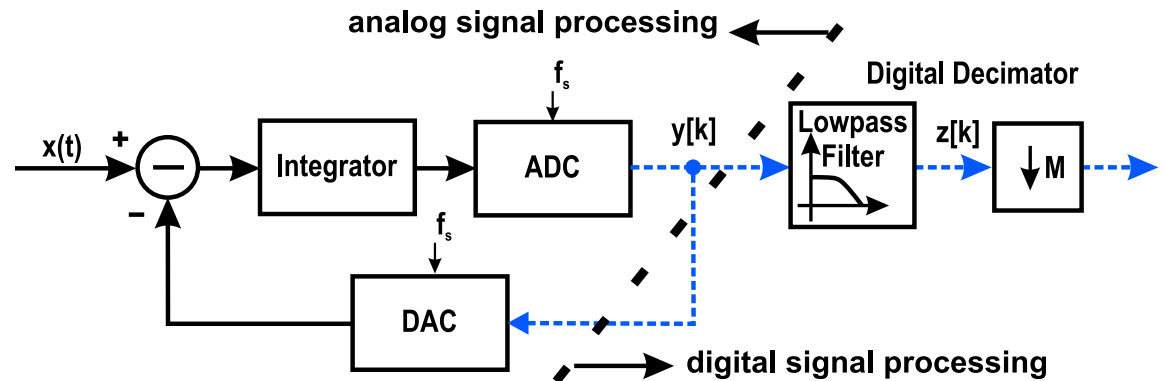
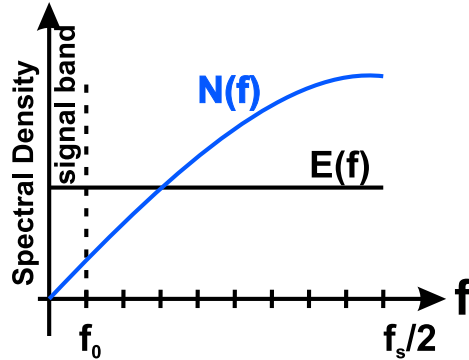
### Nonlinearity Estimation and Correction

- Up to 16 dB improvement in SNDR with digital calibration
- Diagnostic tool for identifying linearity bottleneck

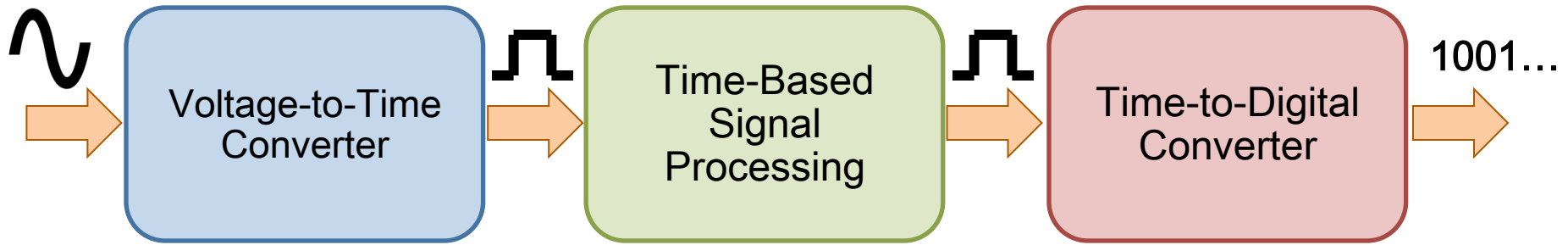
# Delta Sigma Modulation (DSM)

- Idea:
  - start with low-resolution quantizer (1 to few bits)
  - use feedback to shape noise spectrum as high-pass, and
  - use oversampling and digital lowpass filtering to reduce noise

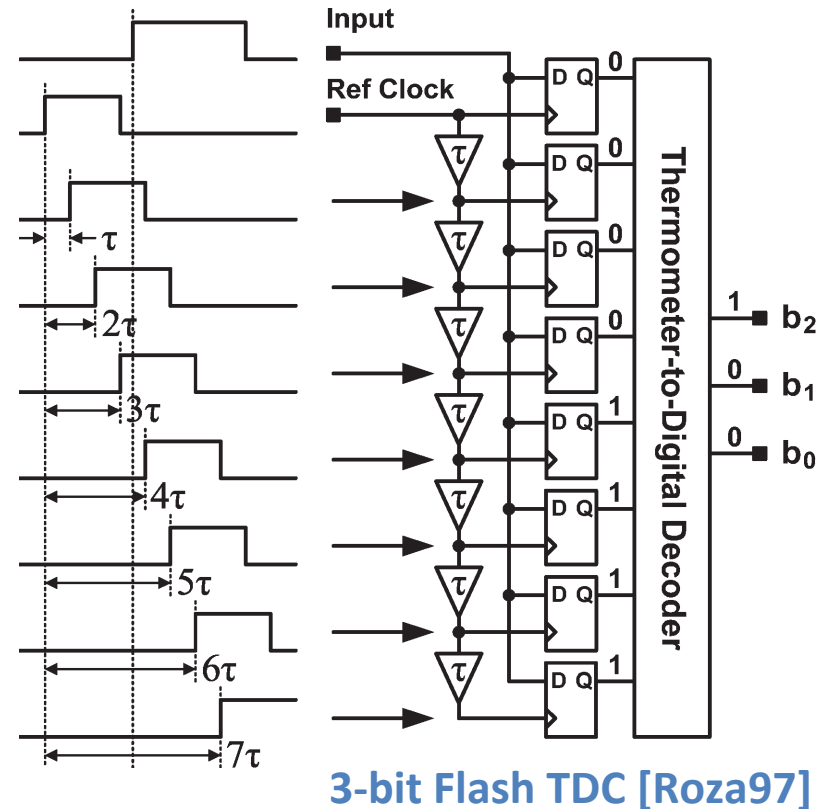
## 1st Order DSM



# Time-Based Signal Processing



- Benefits from scaling perspective:
  - Improved timing accuracy with CMOS scaling
  - Digital implementation
  - Not thermal noise limited, no need for large capacitances

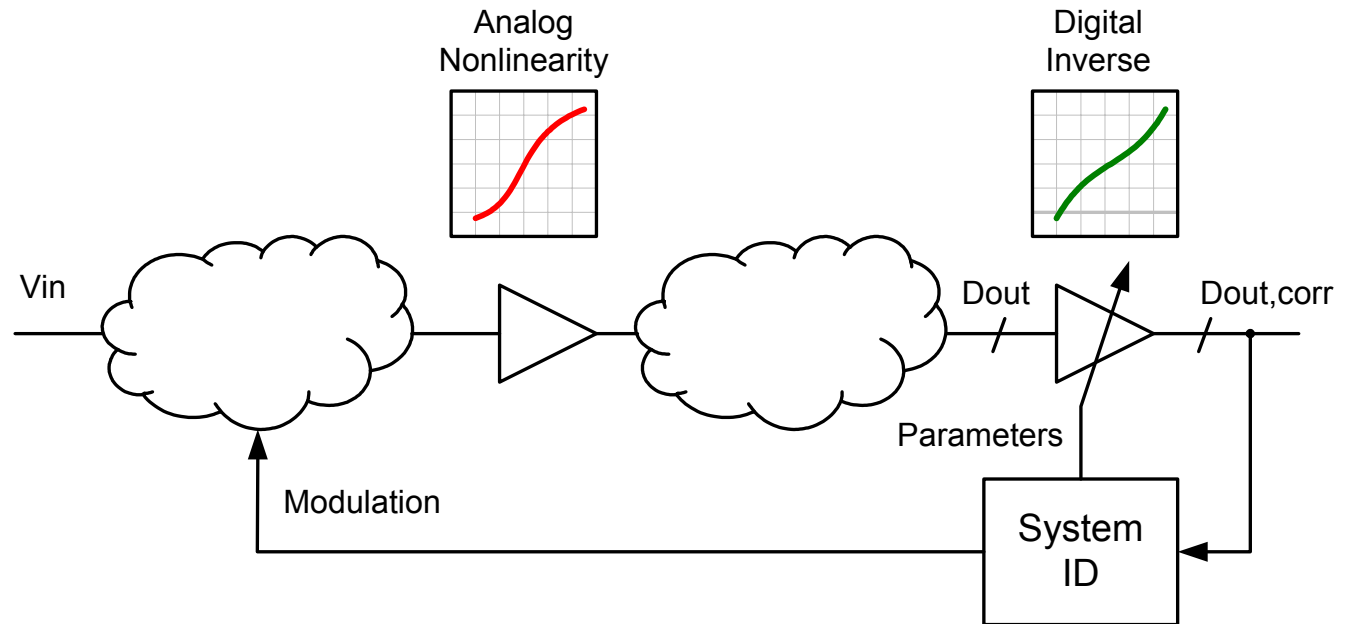




# Digitally-Assisted Analog Scheme

- A trend in the literature, to improve analog circuit performance through digital methods [Mурmann2010]
- The availability of cheap (power/area) digital circuits makes these methods more attractive as processes scale.

- Example:



# Thesis Statement

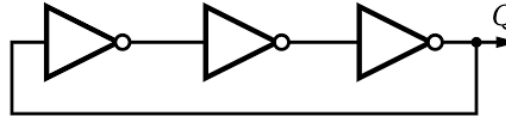
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*Architect low-area delta-sigma data converters that scale with CMOS technology by replacing voltage-domain with time-domain processing.*

# Prior Art

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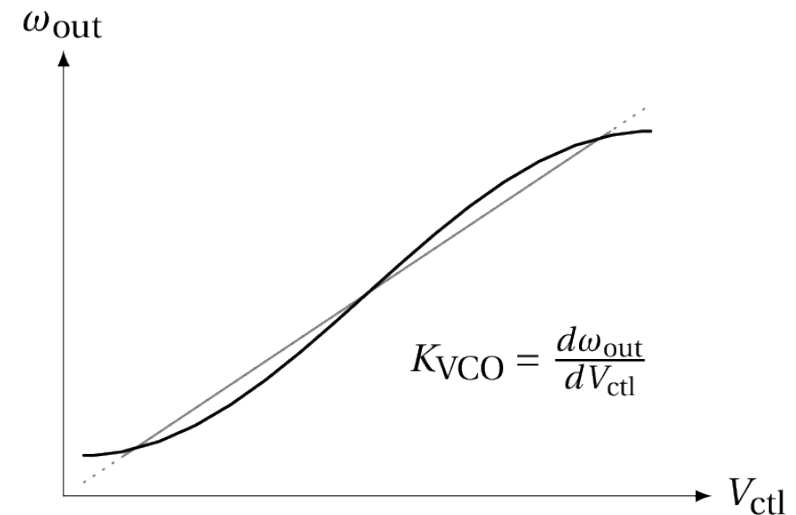
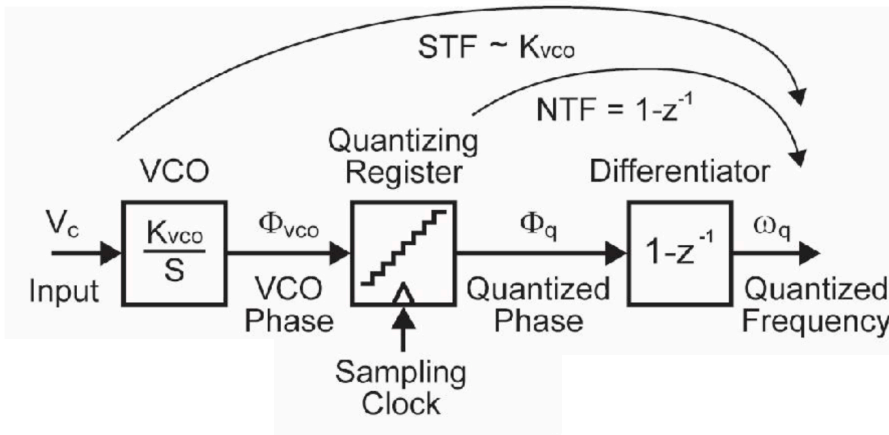
- Voltage Controlled Oscillator (VCO)-Based Delta Sigma ADC



- Time-Based Delta Sigma ADCs
  - Using asynchronous delta sigma modulator
  - Time-to-Digital Converters (TDCs)

# VCO-Based Delta Sigma ADC

- Continuous-time integration ( $1/s$ ) is inherent.
- Sampling VCO phase at periodic intervals gives quantized phase.
- VCO nonlinearity ( $K_{VCO}$ ) is an important limitation.
  - [Rao2011] proposes two-level PWM modulator to avoid the problem
  - [Taylor2013] uses digital calibration and post-correction to mitigate the problem

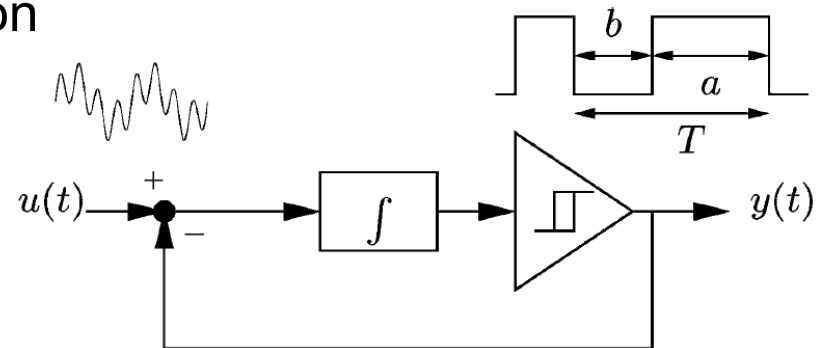


# Prior Art

- Time-Based Delta Sigma ADCs

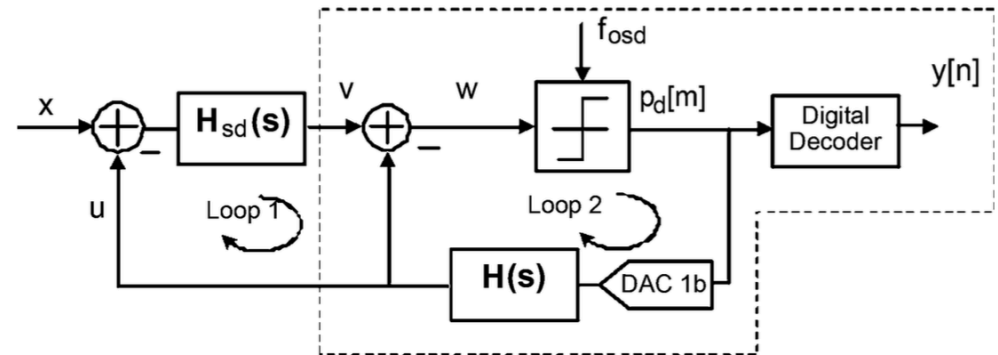
- Asynchronous delta-sigma modulation

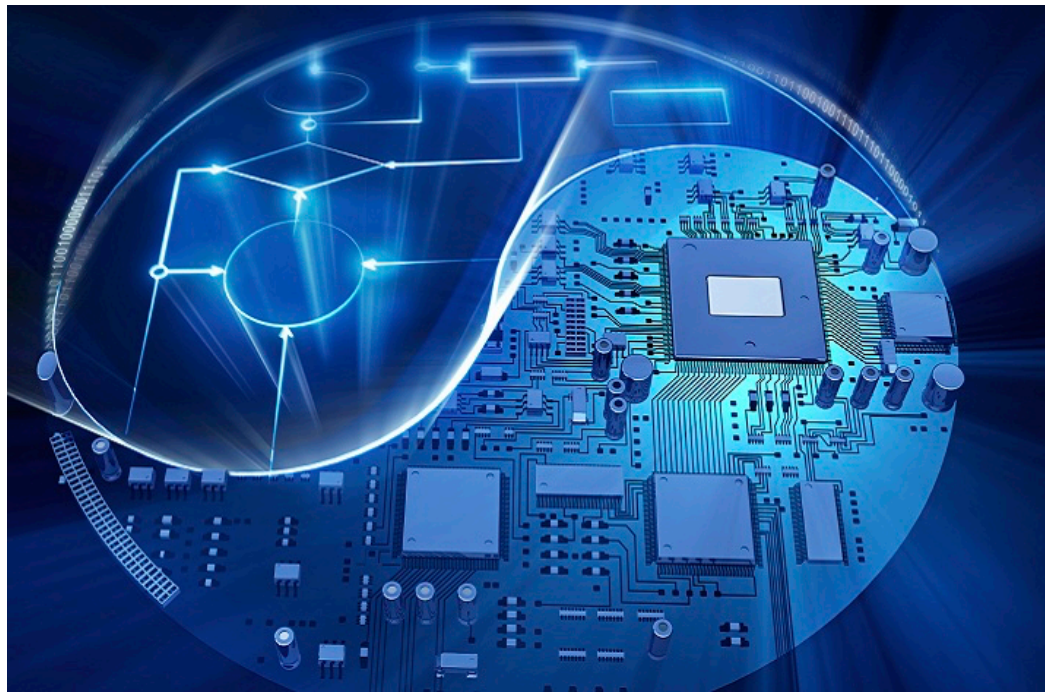
[Dhanasekaran2009,  
Taillefer2009,  
Daniels2010]



- Time Encoding Quantizer (TEQ)-based ADCs

[Prefasi2009]



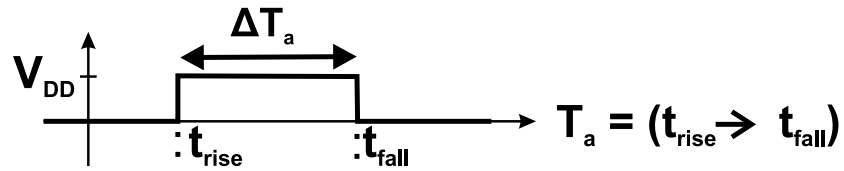


First Contribution

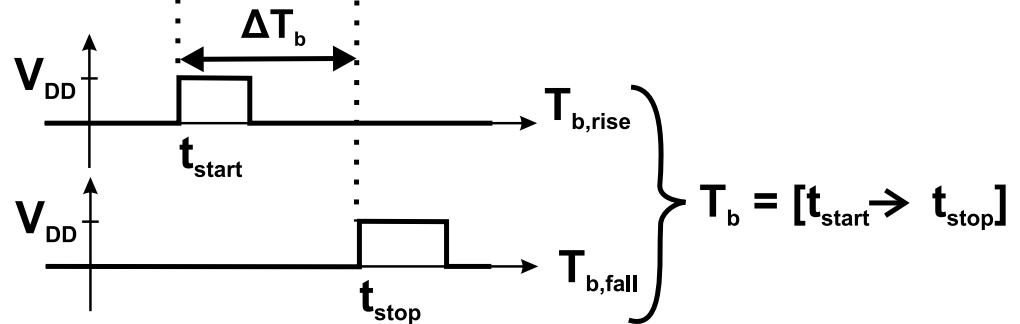
# Time-Based Delta Sigma ADC Architecture & Modeling

# Time-Based Processing Encoding/Operands

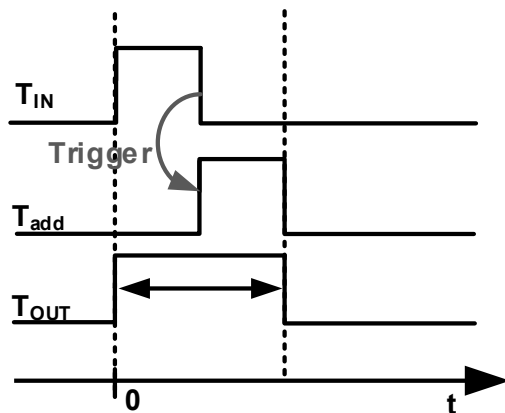
Conventional Pulse



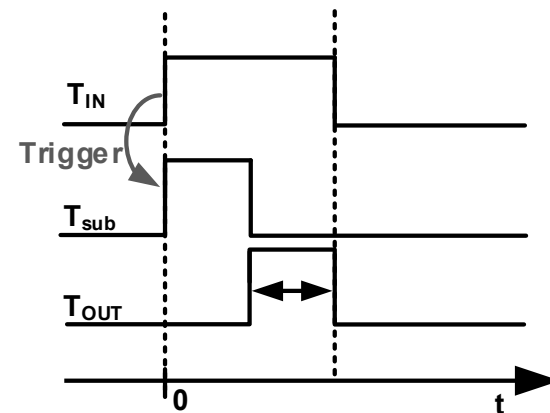
Pseudo-Differential Pulses



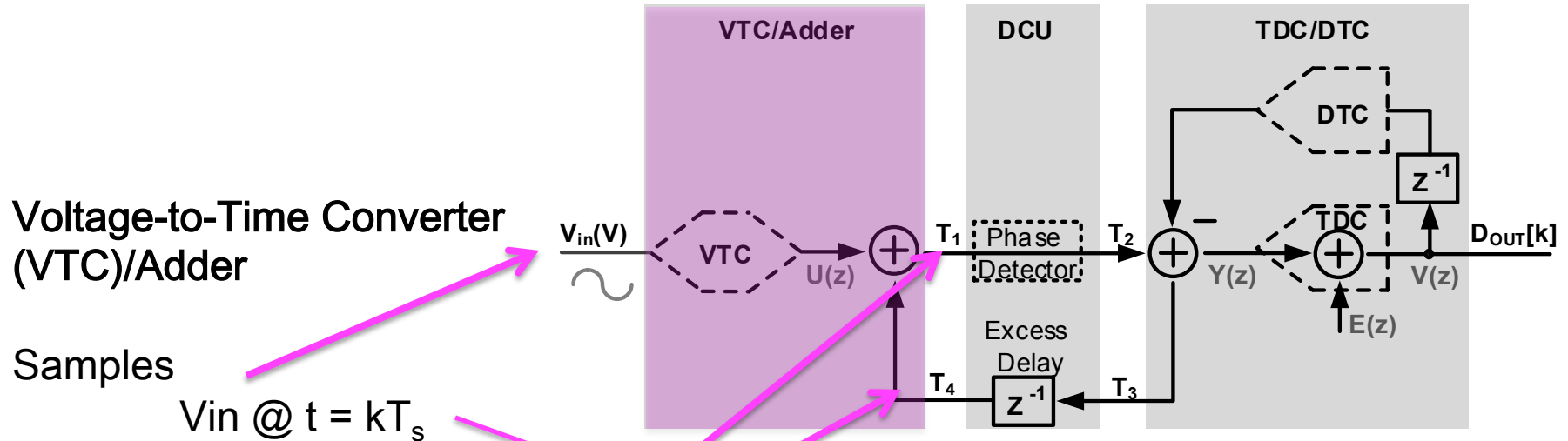
Pulse Width Addition



Pulse Width Subtraction



# System Model



Voltage-to-Time Converter (VTC)/Adder

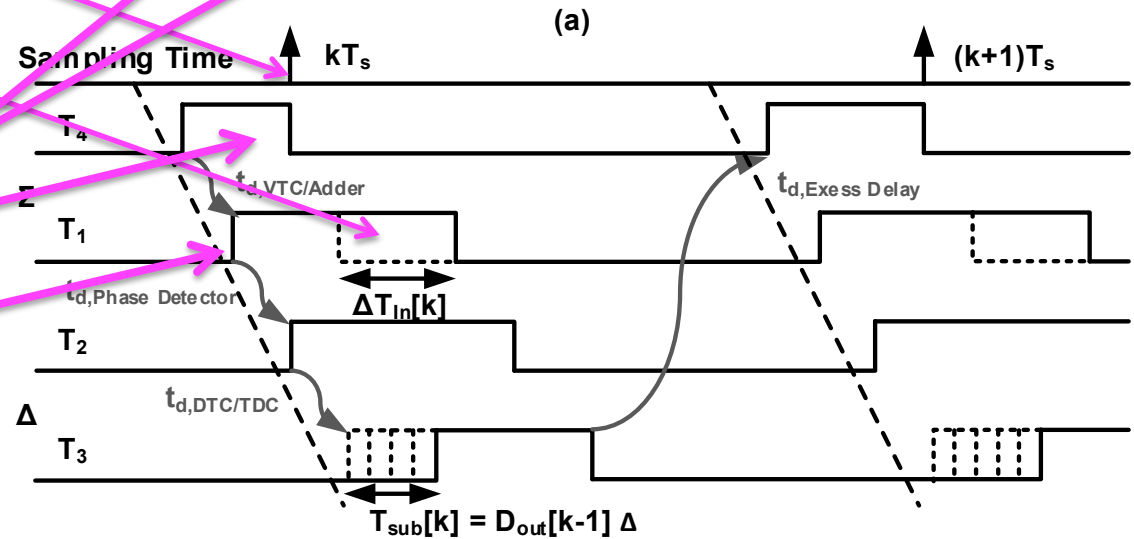
Samples

$$V_{in} @ t = kT_s$$

Converts it to  $\Delta T_{in}[k]$

Adds it to the feedback pulse  $T_4$

Result =  $T_1$





# System Model

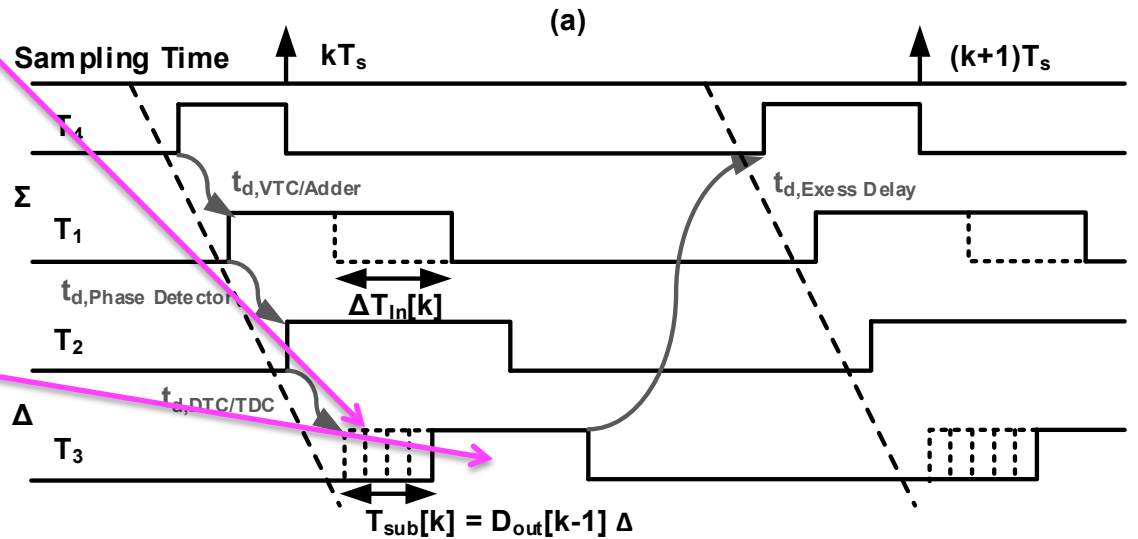
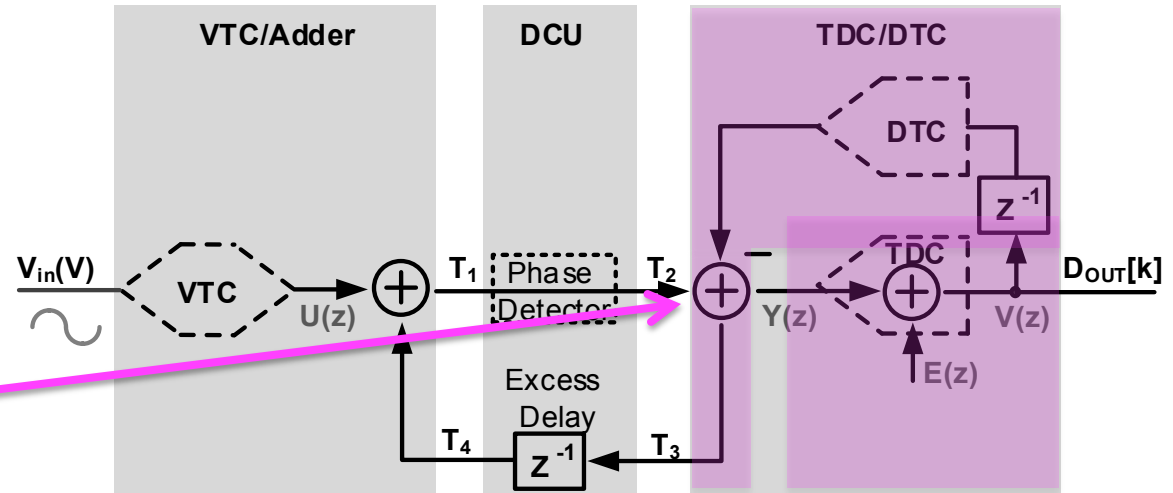
Digital-to-Time Converter (DTC)

Subtracts from  $T_2$   
 $D_{out}[k-1]$  units

Time-to-Digital Converter (TDC)

quantizes the result to get

$D_{out}[k]$

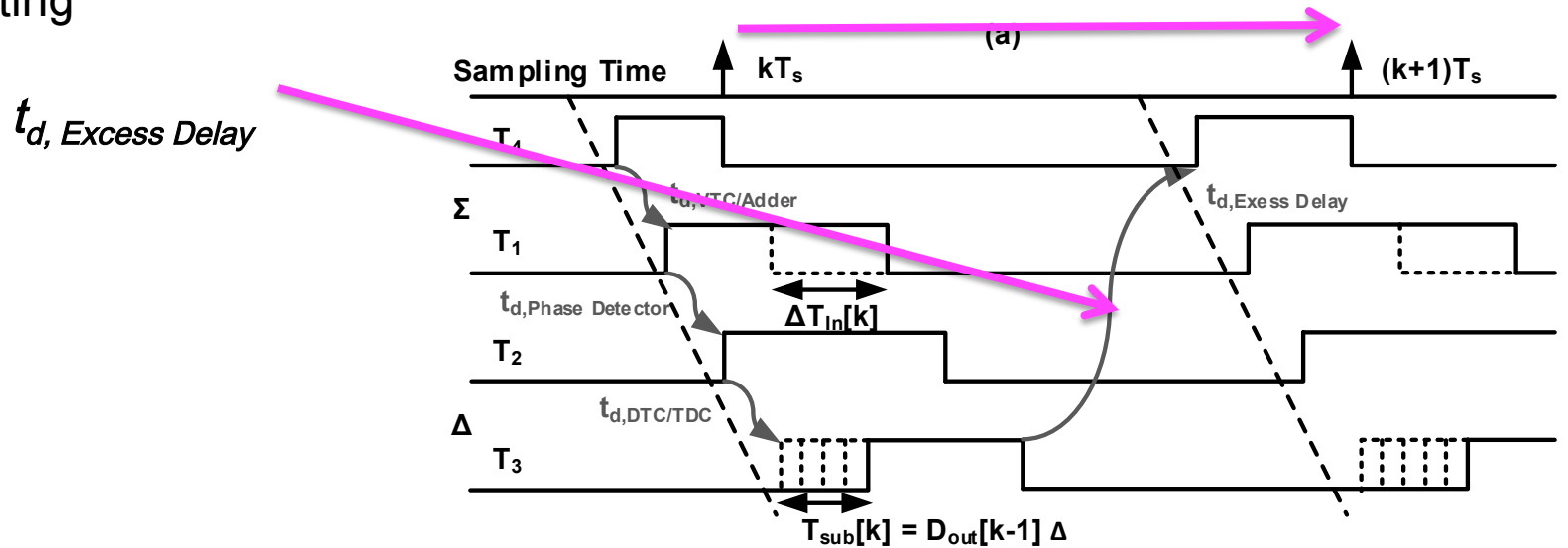
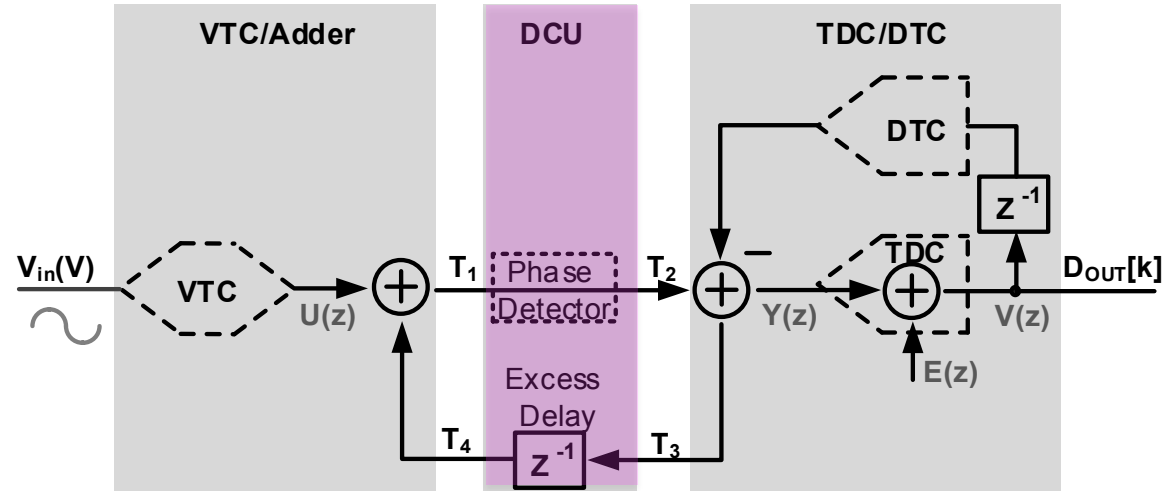


# System Model

## Delay Control Unit (DCU) and Excess Delay

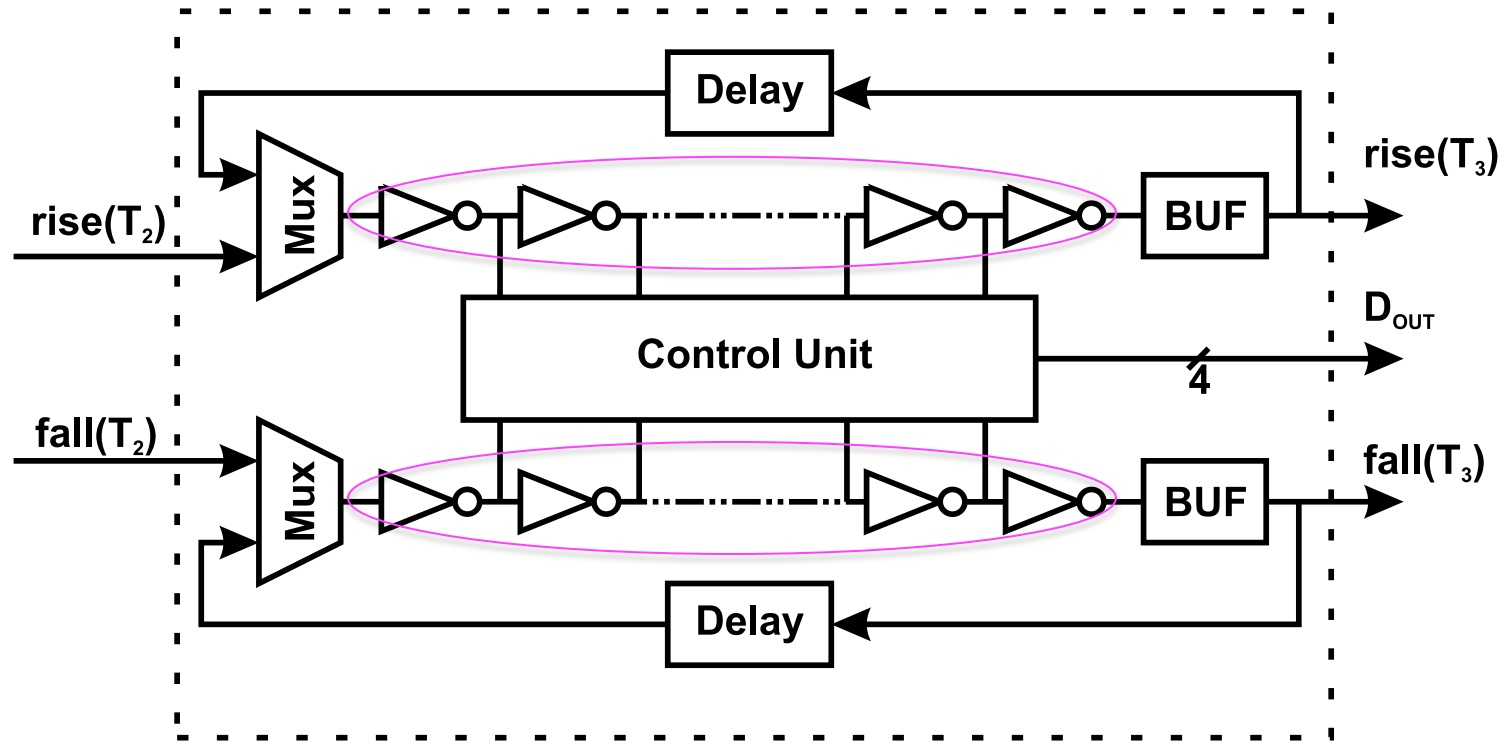
ensure uniform sampling

by adjusting

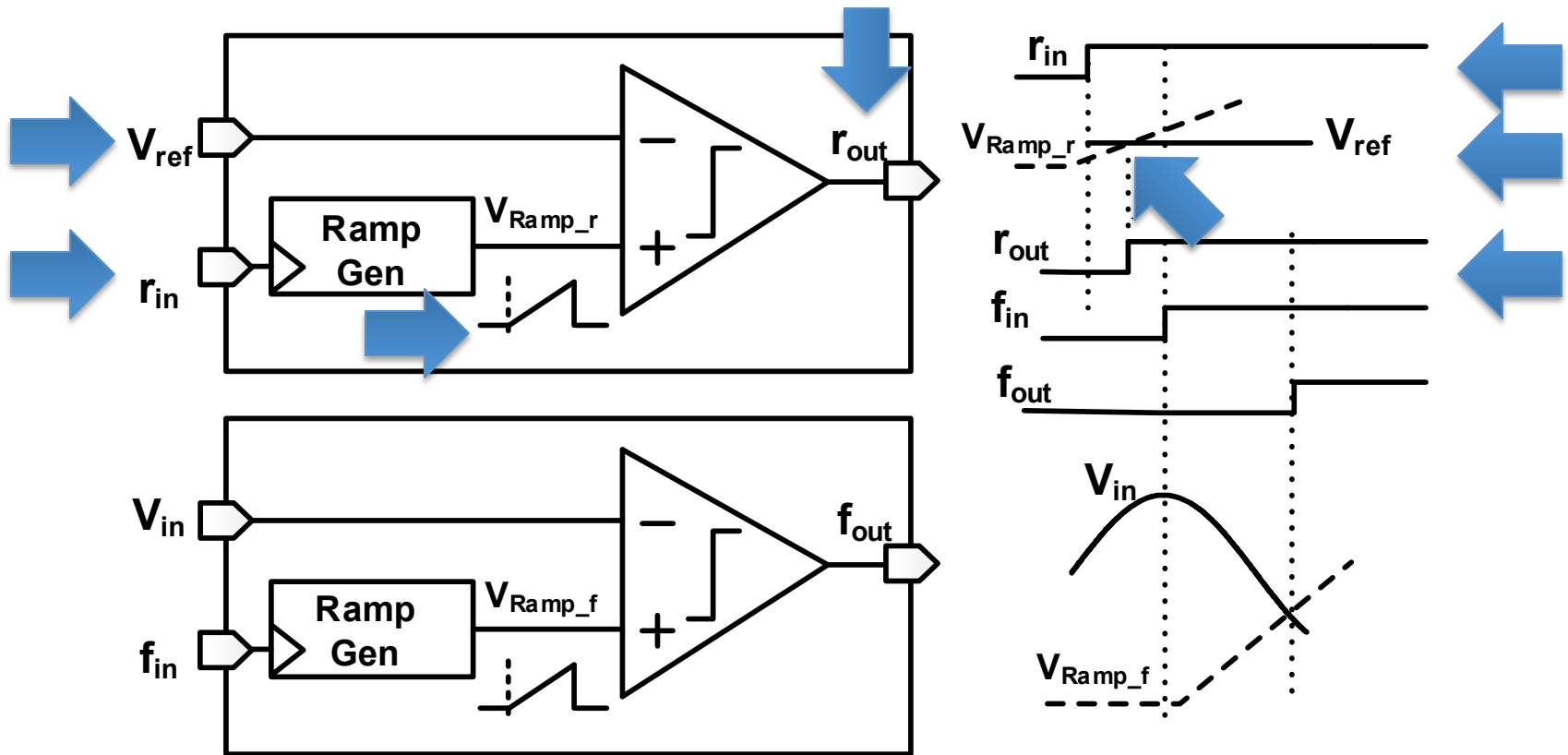


# TDC/DTC

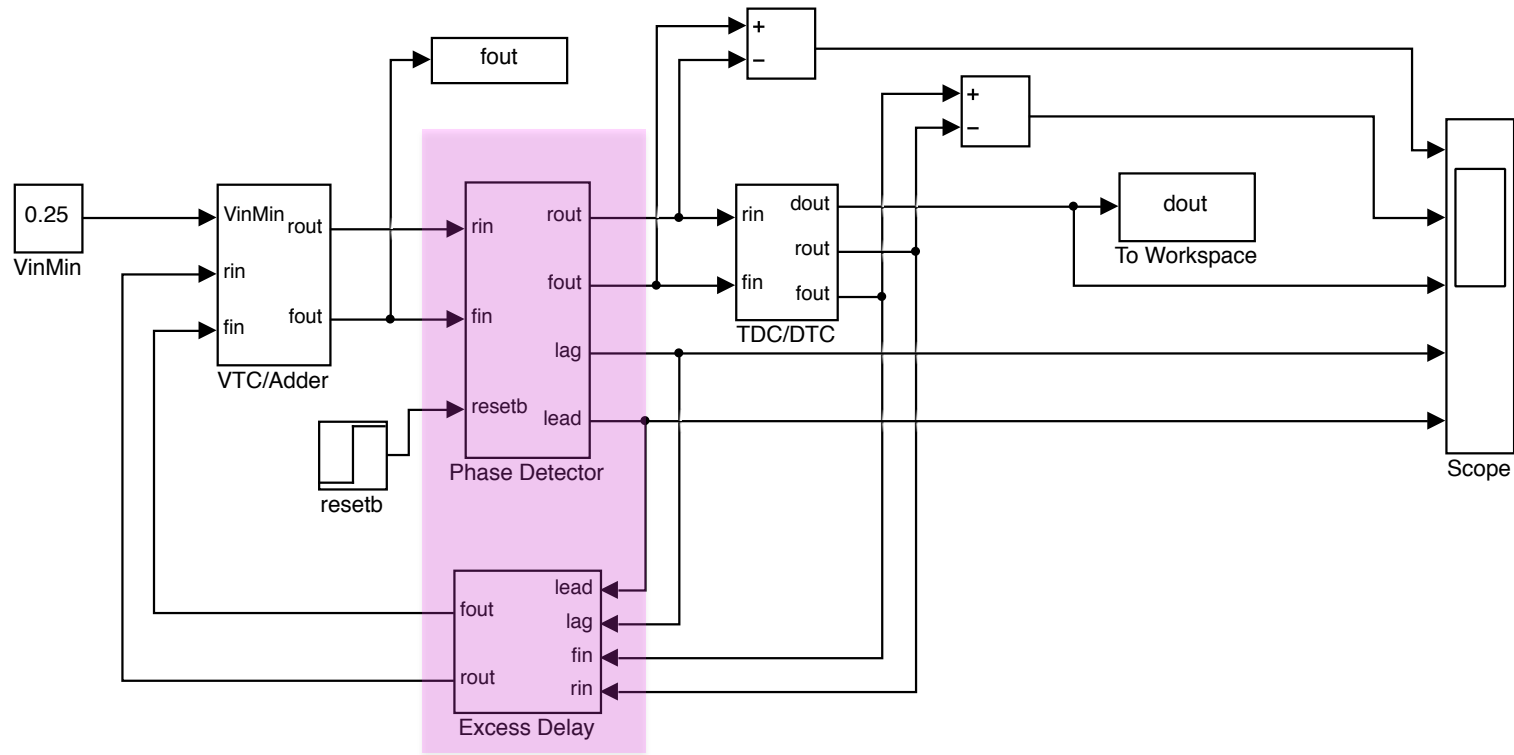
- TDC = Time-to-Digital Converter
- DTC = Digital-to-Time Converter



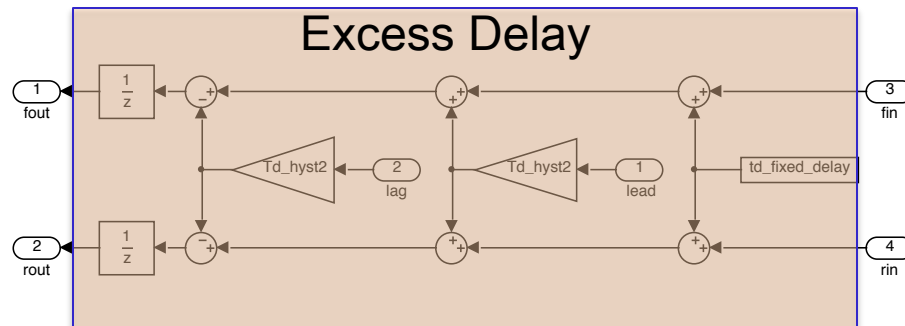
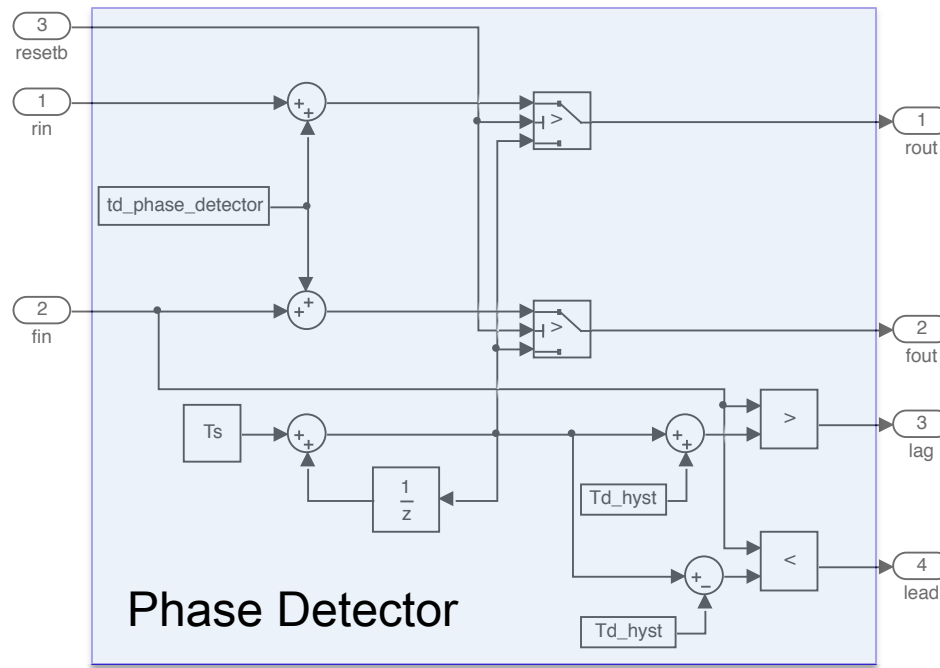
# Voltage-to-Time Converter/Adder



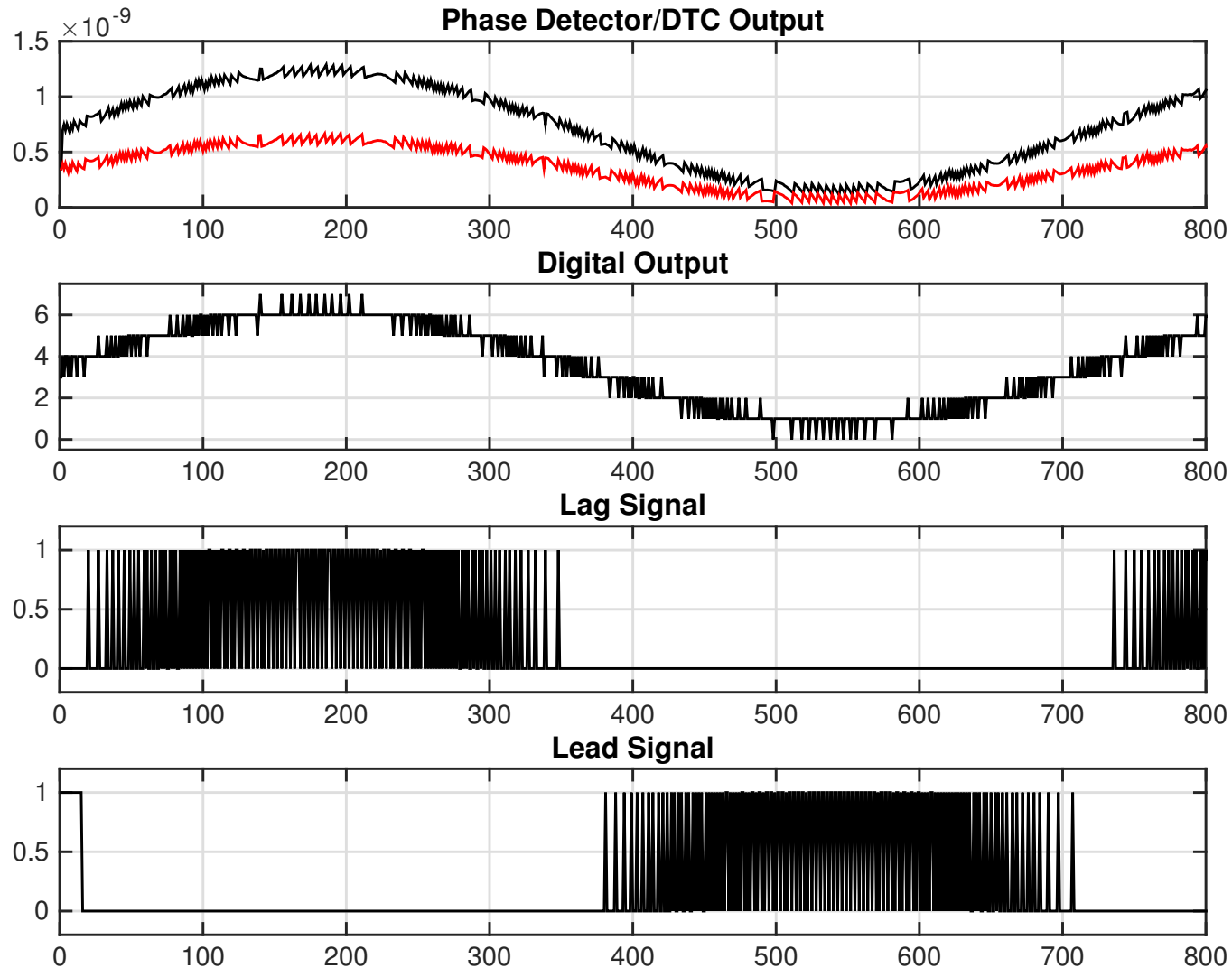
# Simulink Modeling



# Simulink Modeling - DCU



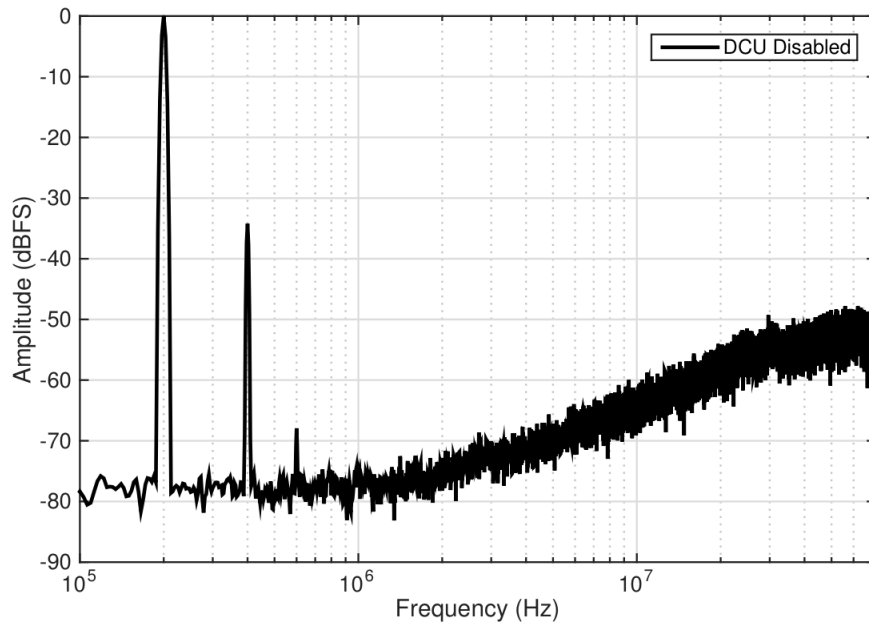
# Simulink Modeling



# Role of DCU in Reducing Distortion

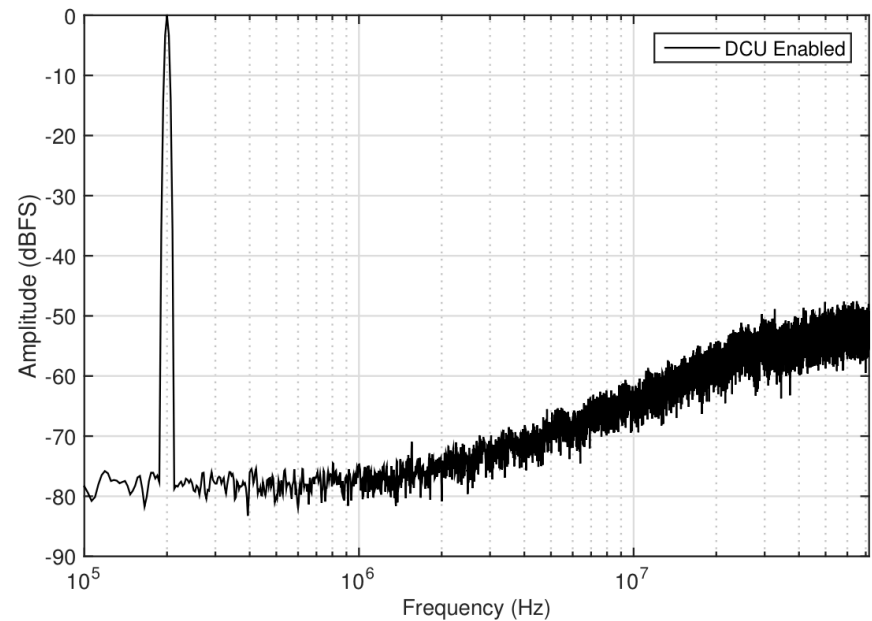
## DCU Disabled

Spectrum exhibits major harmonic distortion due to non-uniform sampling



## DCU Enabled

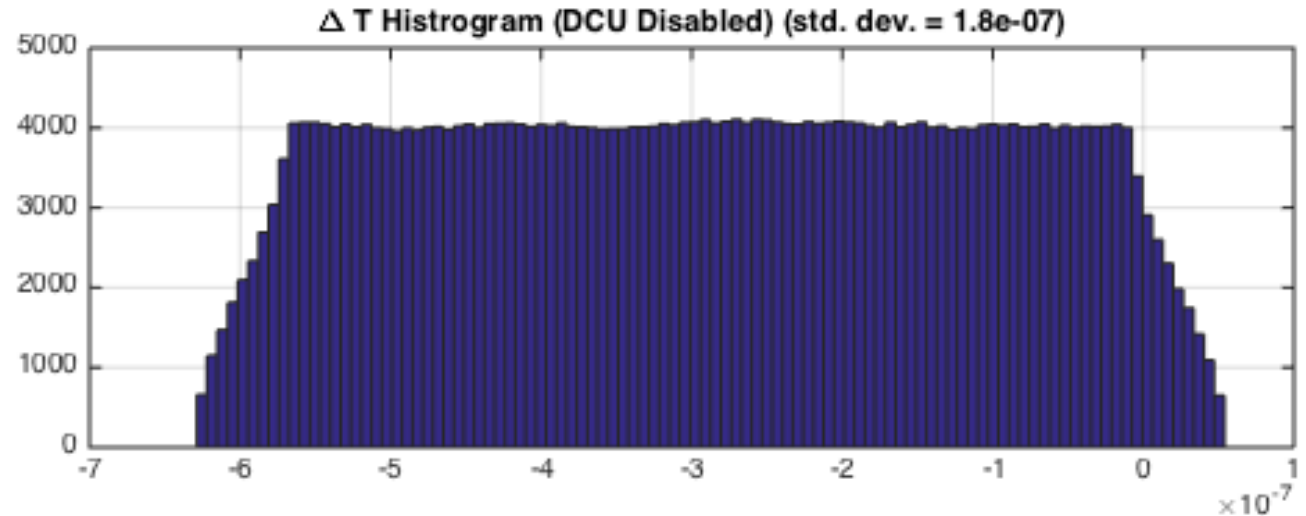
Spectrum is virtually distortion free



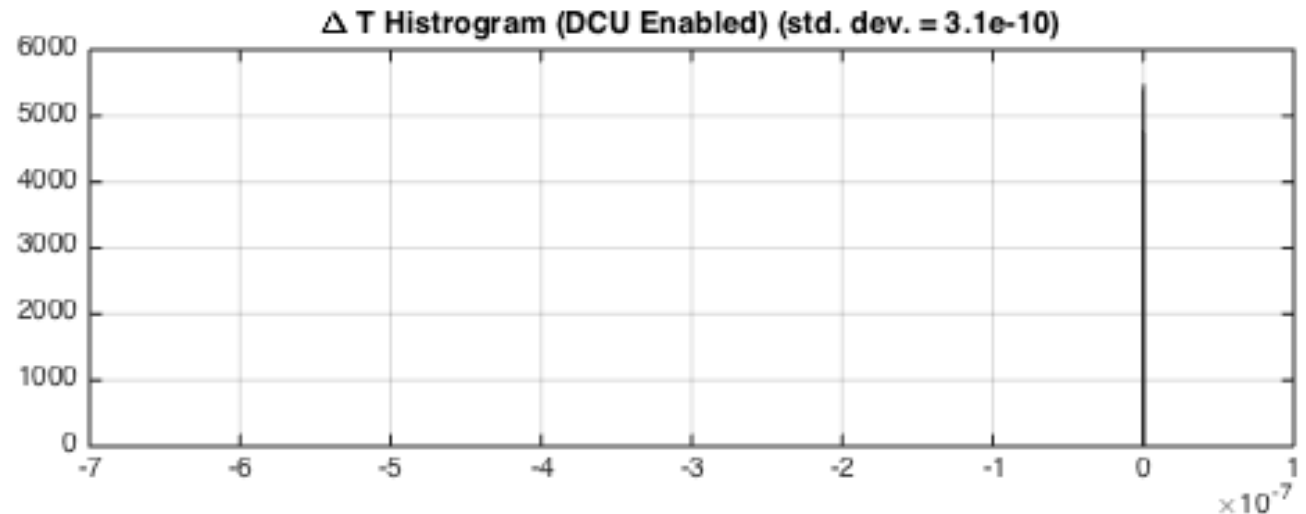


# Role of DCU in Reducing Distortion

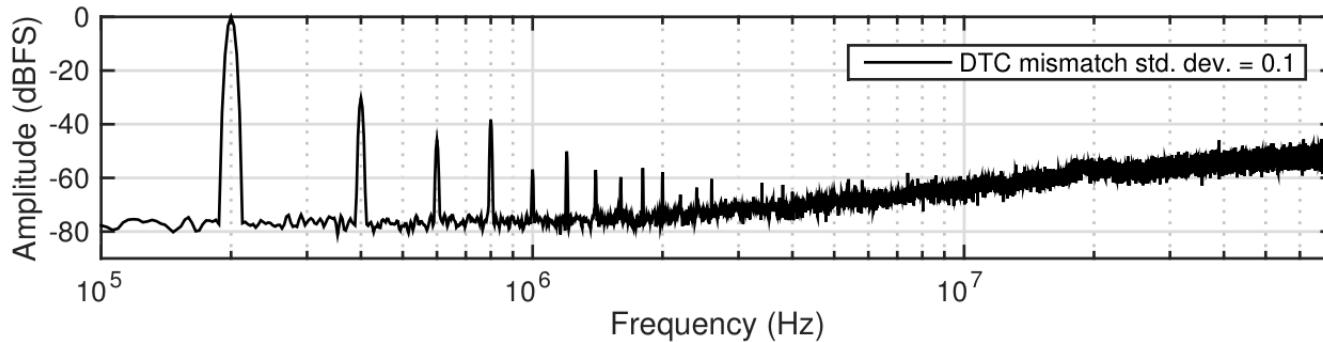
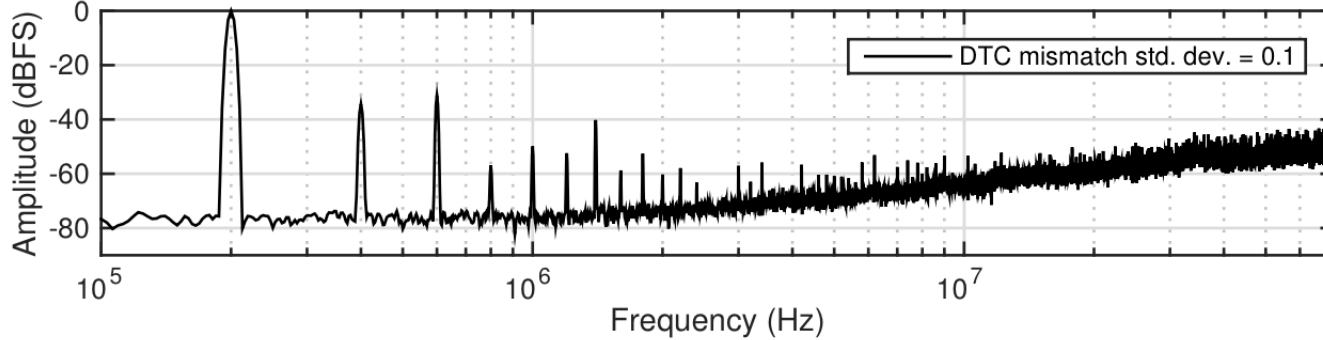
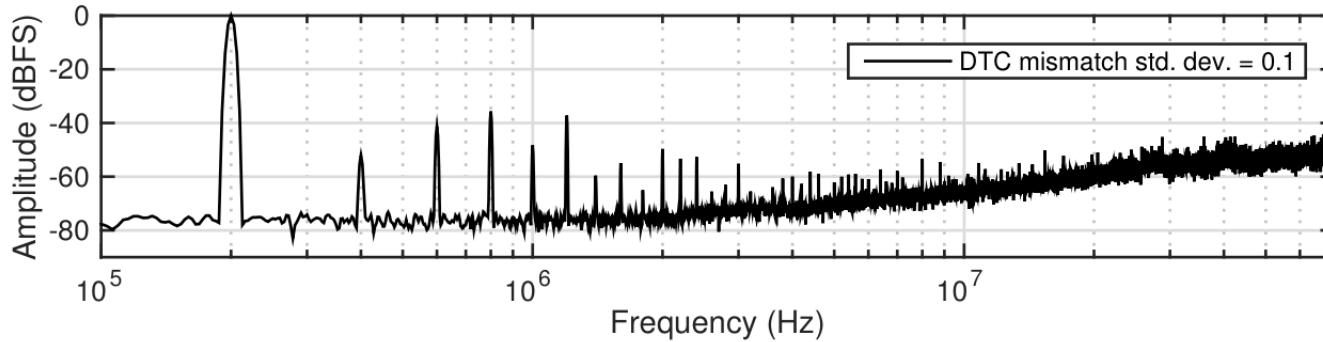
DCU Disabled



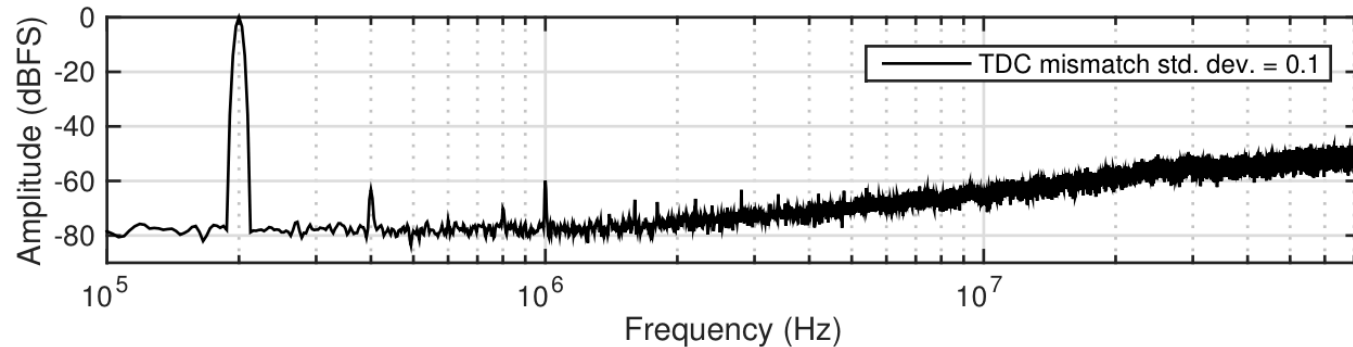
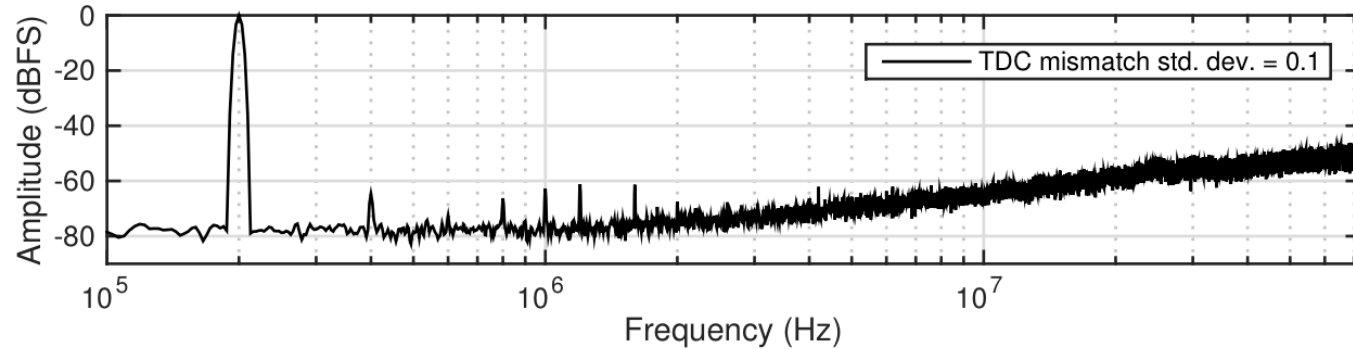
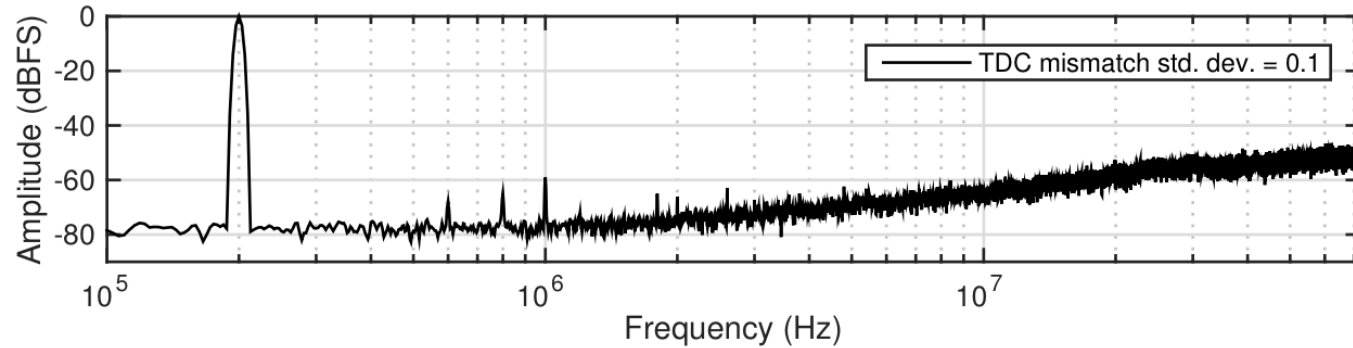
DCU Enabled



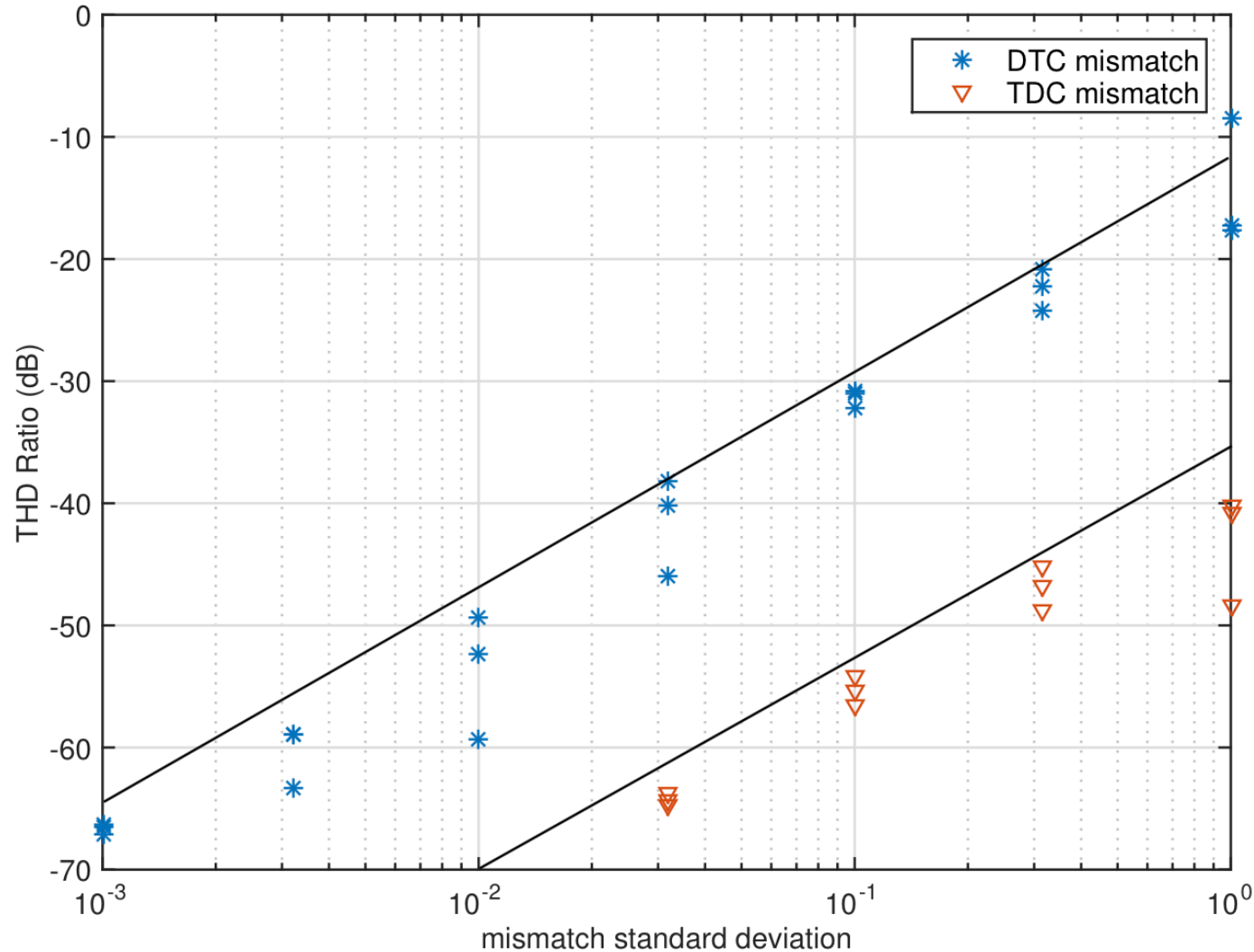
# Effect of DTC Element Mismatch

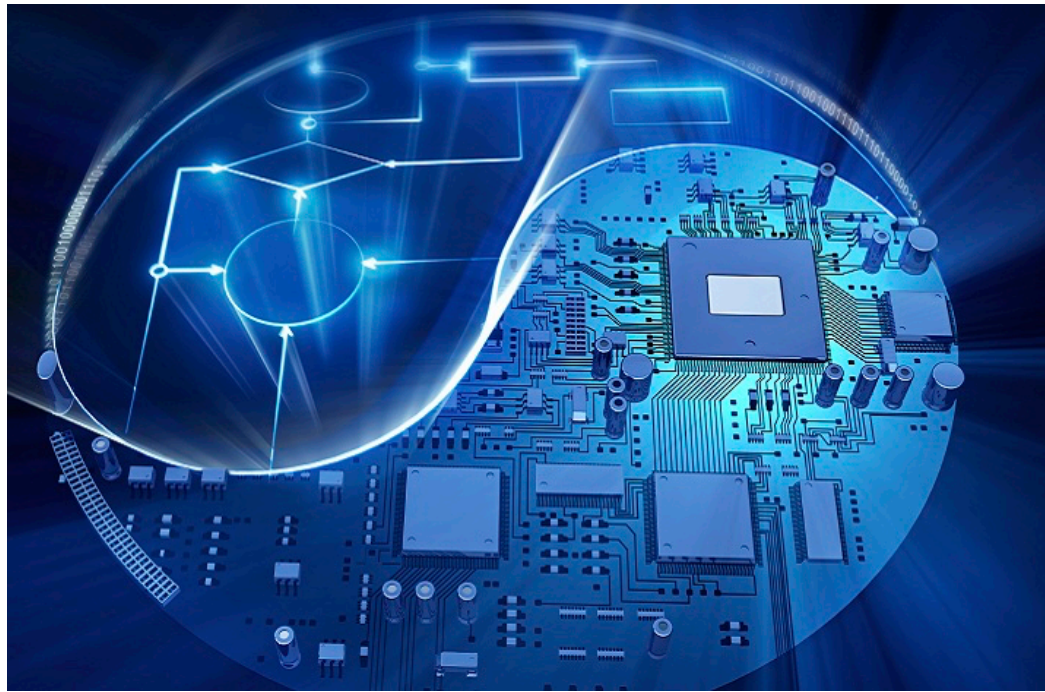


# Effect of TDC Element Mismatch



# Comparison of DTC/TDC Element Mismatch

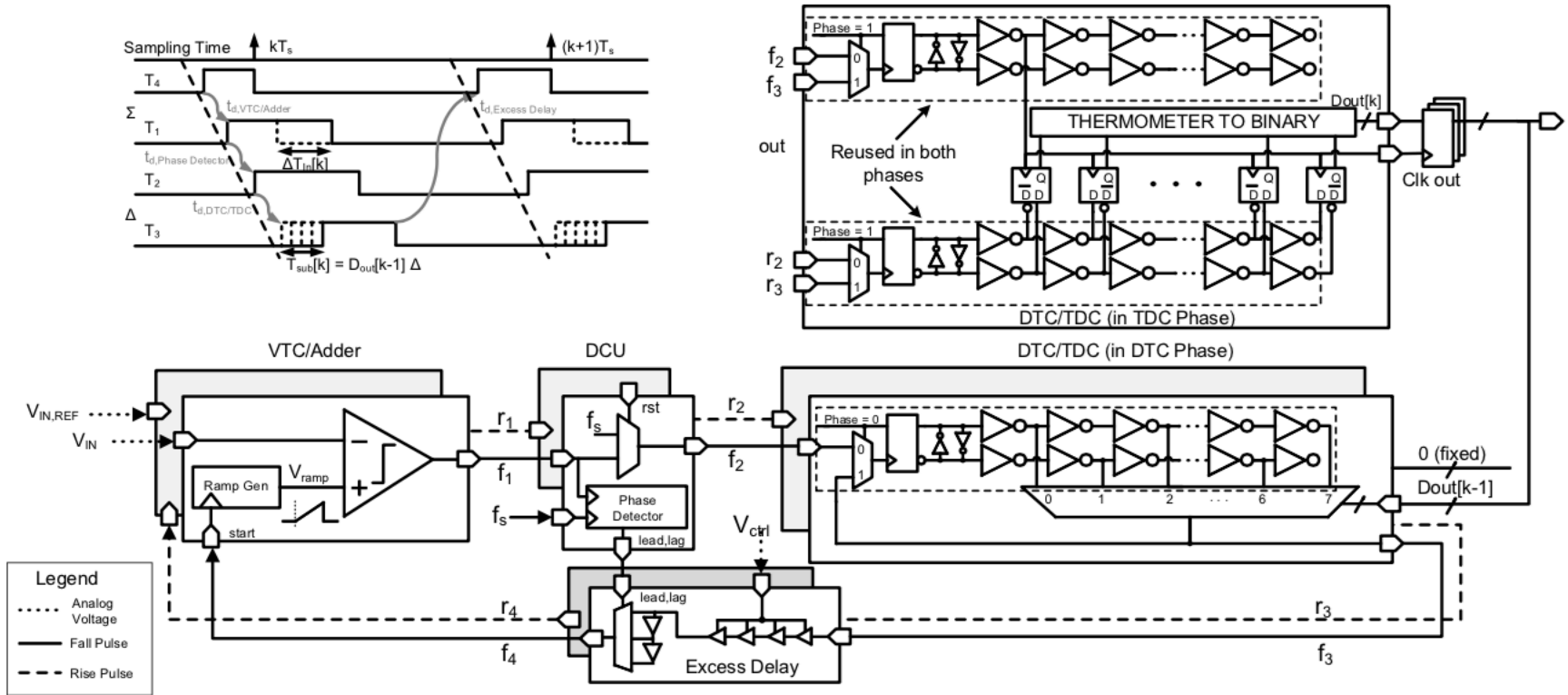




Second Contribution

# Prototype ADC Chips

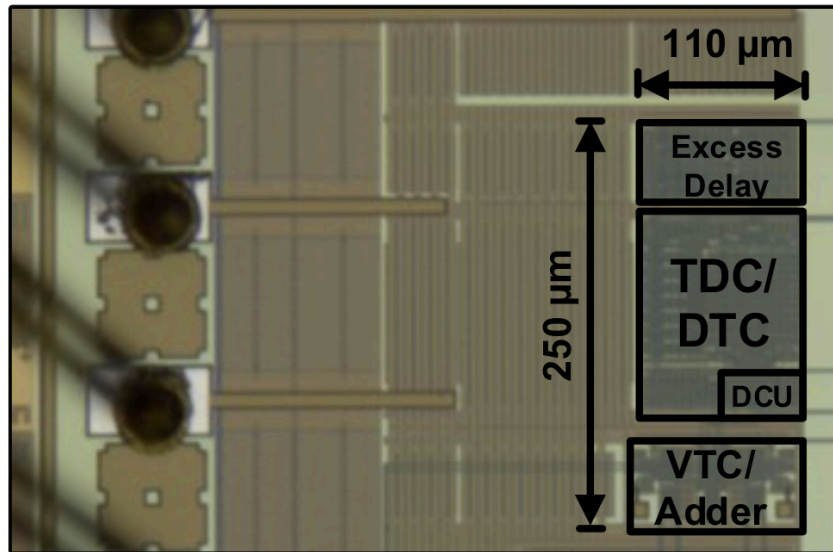
# First Generation Chip in TSMC 180nm



TSMC = Taiwan Semiconductor Manufacturing Company

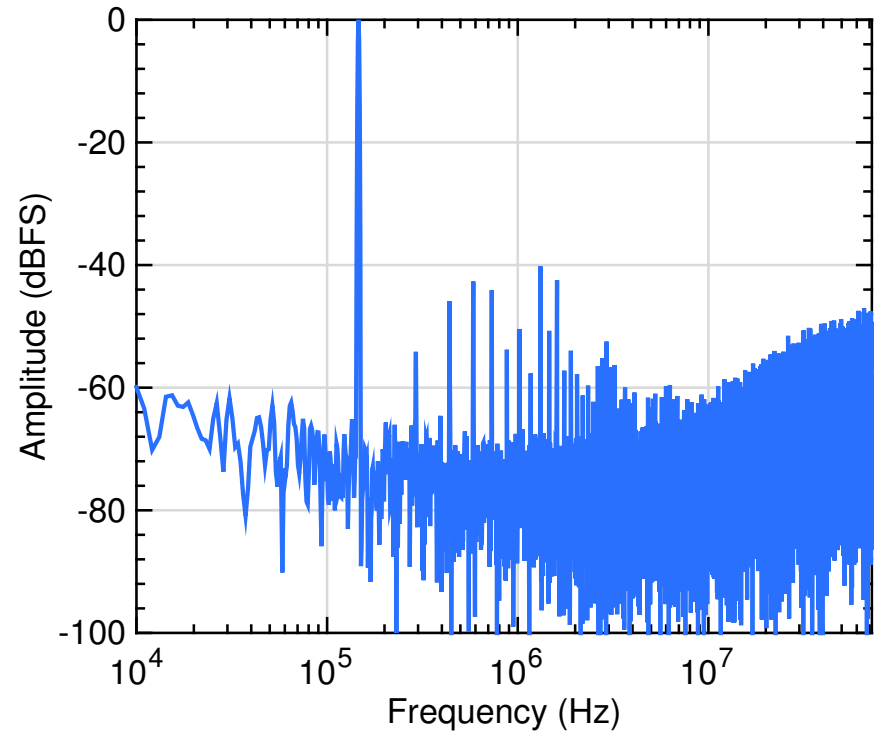
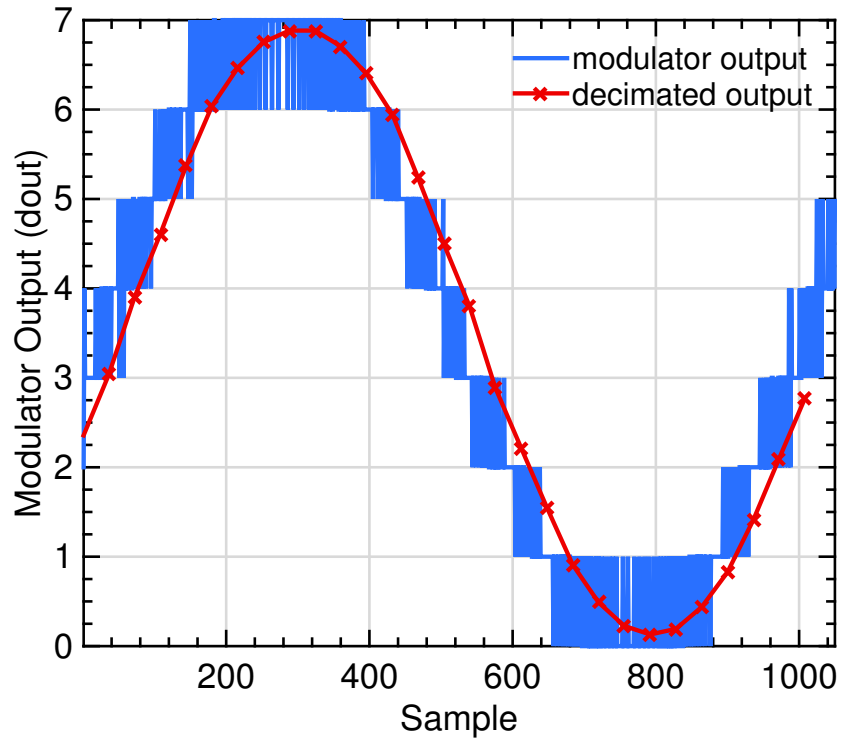
# First Generation Chip Details

Parameter	Value	Units
Process	TSMC 180nm 6M 1P	-
Supply Voltage ( $V_{DD}$ )	1.8	V
Oversample Frequency ( $f_s$ )	144	MHz
Quantizer (TDC) Number of Bits	3	bits
DAC (DTC) Number of Bits	3	bits
TDC LSB ( $\Delta$ )	80	ps
$t_{d,VTC/Adder}$	2.1	ns
$t_{d,PhaseDetector}$	0.57	ns
$t_{d,DTC}$	1.24	ns
$t_{d,ExcessDelay}$ (Average)	2.8	ps
Area	0.0275	mm <sup>2</sup>



Quantity	Value	Units
$f_s$	144	MHz
OSR	36	-
BW	2.0	MHz
$f_{in}$	146.1	kHz
$V_{in,pk-pk}$	400	mV
SNR	44.6	dB
SNDR	34.6	dB
THD	-35.0	dB
ENoB	5.5	bits
Power	2.7	mW

# First Generation Chip Waveforms

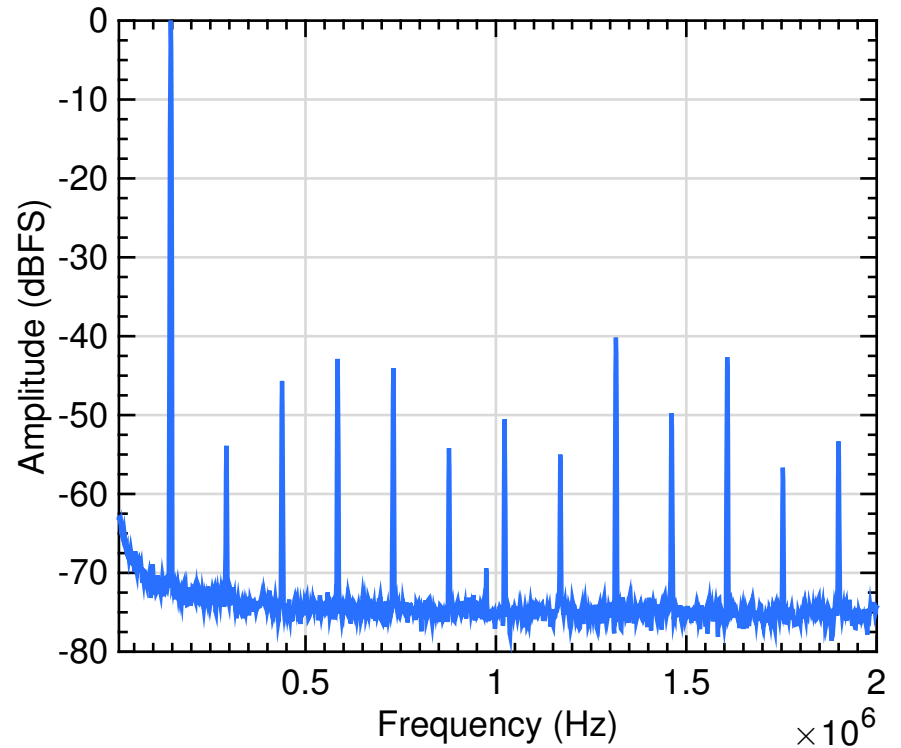
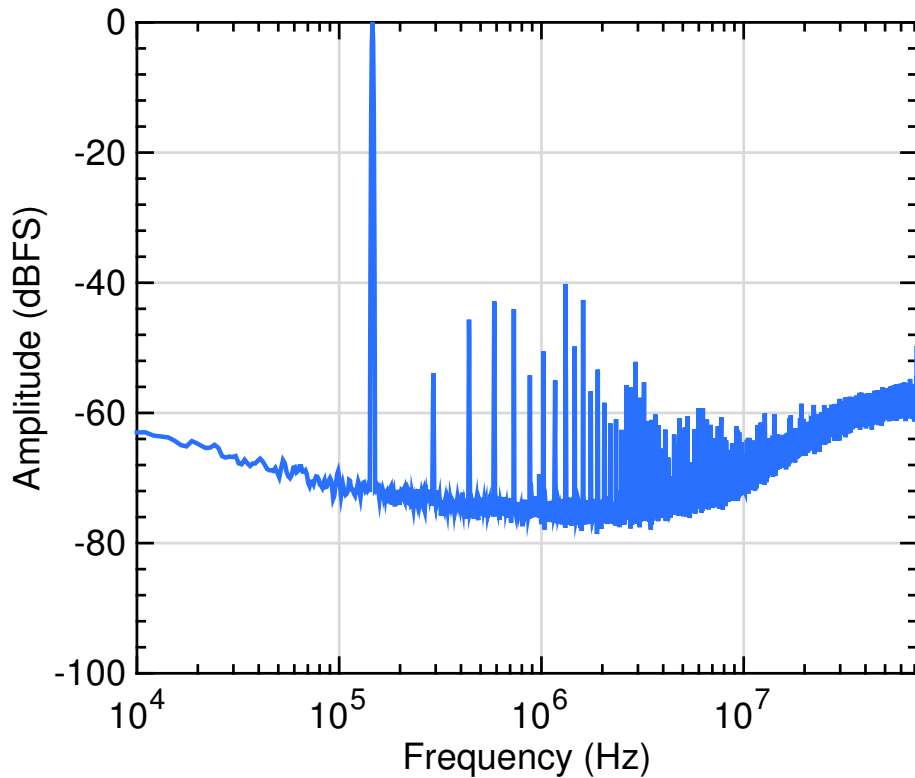


Input is a 146.1 kHz sinusoid



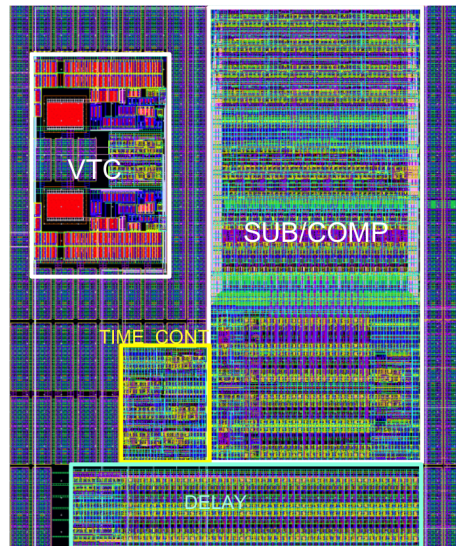
# First Generation Chip Waveforms

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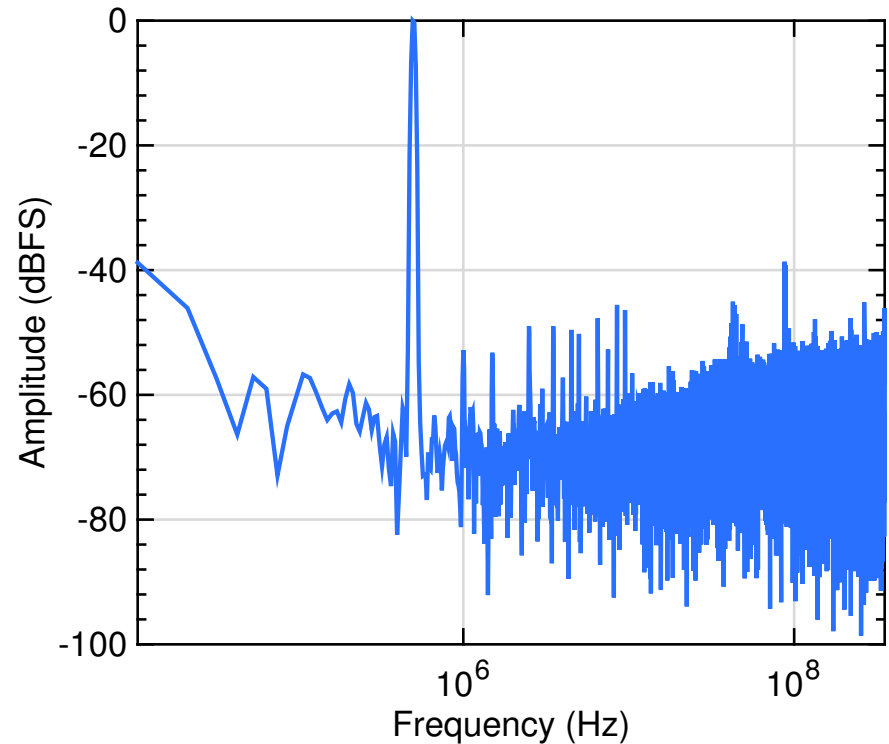
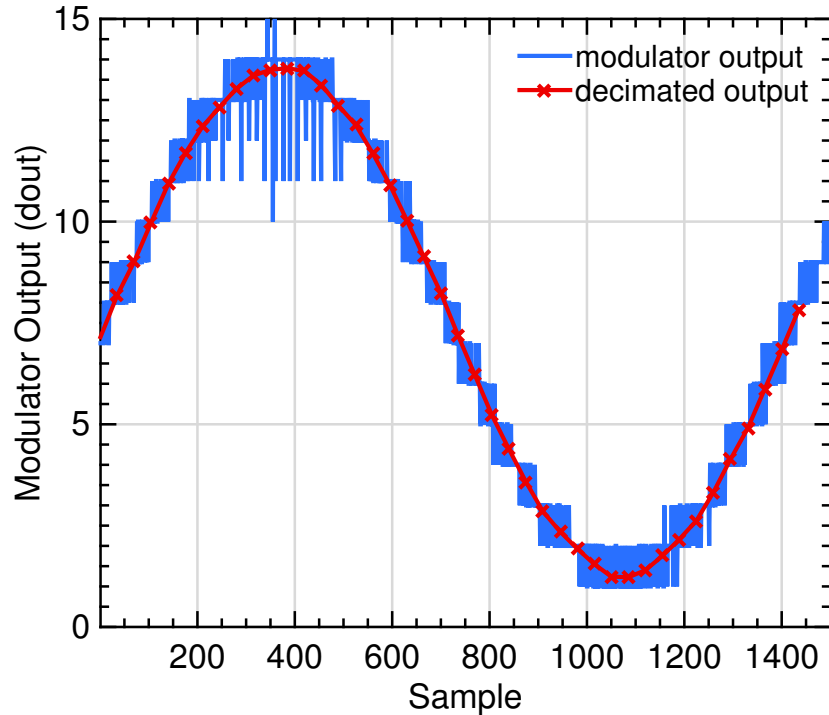
# Second Generation Chip in IBM 45nm SOI

Parameter	Value	Units
Process	IBM 45nm SOI 10M 1P	-
Supply Voltage ( $V_{DD}$ )	1.8/1.0	V
Oversample Frequency ( $f_s$ )	640	MHz
Quantizer (TDC) Number of Bits	4	bits
DAC (DTC) Number of Bits	4	bits
TDC LSB ( $\Delta$ )	15.8	ps
$t_{d,VTC/Addeer}$	714	ps
$t_{d,PhaseDetector}$	116	ps
$t_{d,DTC}$	302	ps
$t_{d,ExcessDelay}$ (Average)	400	ps
Area	0.0192	mm <sup>2</sup>



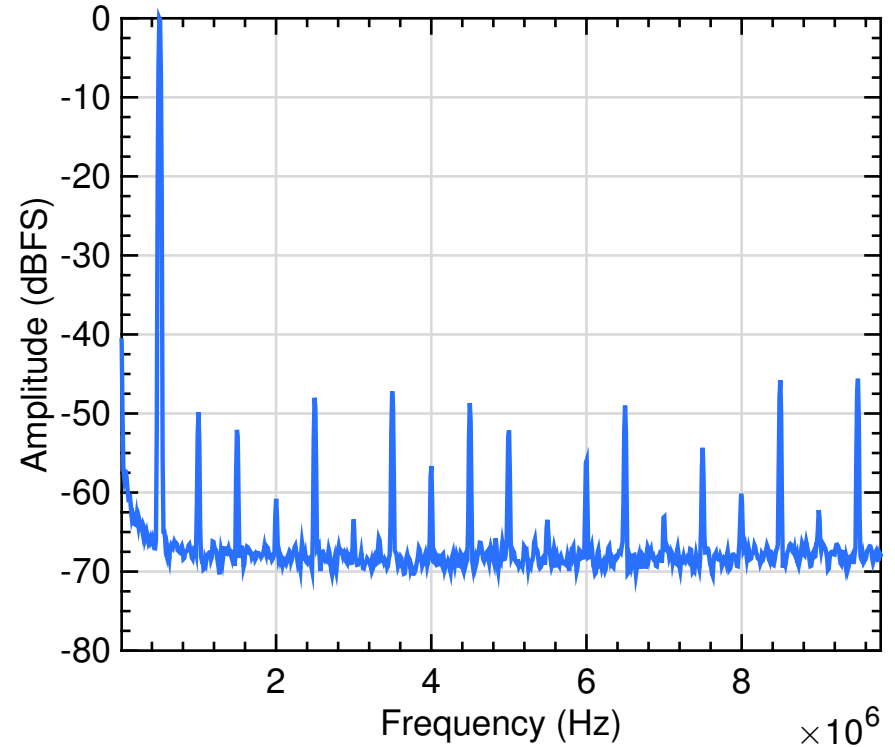
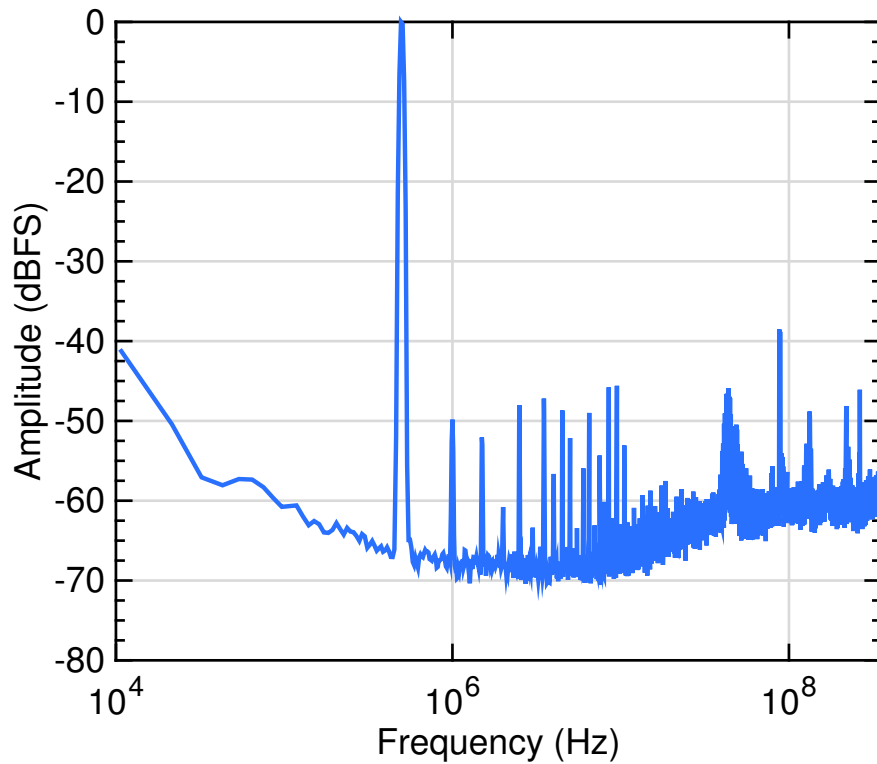
Quantity	Value	Units
$f_s$	705	MHz
OSR	36	-
BW	9.8	MHz
$f_{in}$	500	kHz
$V_{in,pk-pk}$	600	mV
SNR	41.2	dB
SNDR	37.5	dB
EN <sub>oB</sub>	6	bits
THD	-39.6	dB
Power	8.0	mW

# Second Generation Chip in IBM 45nm SOI

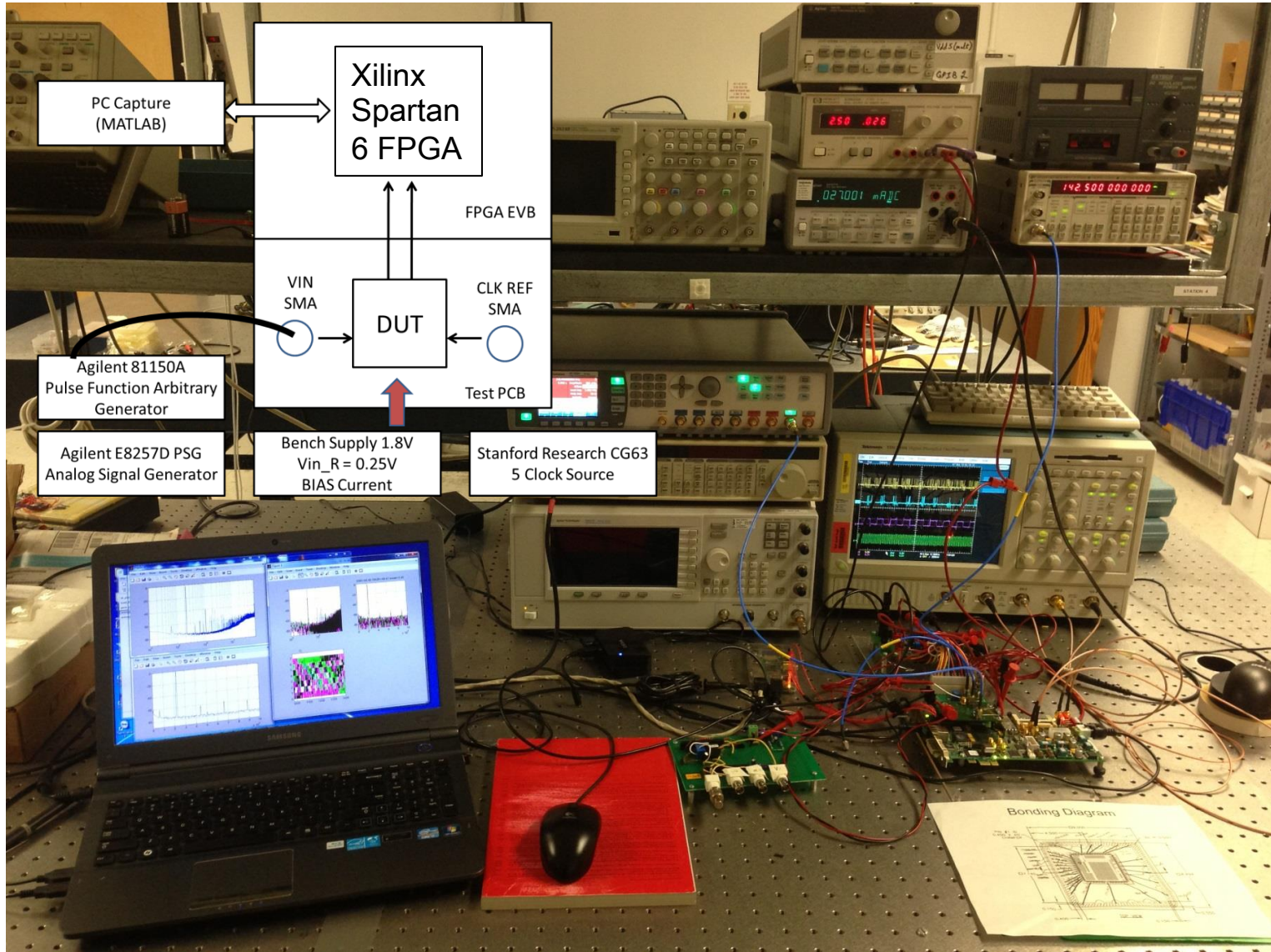


Input is a 500 kHz sinusoid

# Second Generation Chip in IBM 45nm SOI



# Test Setup



# Comparison Table

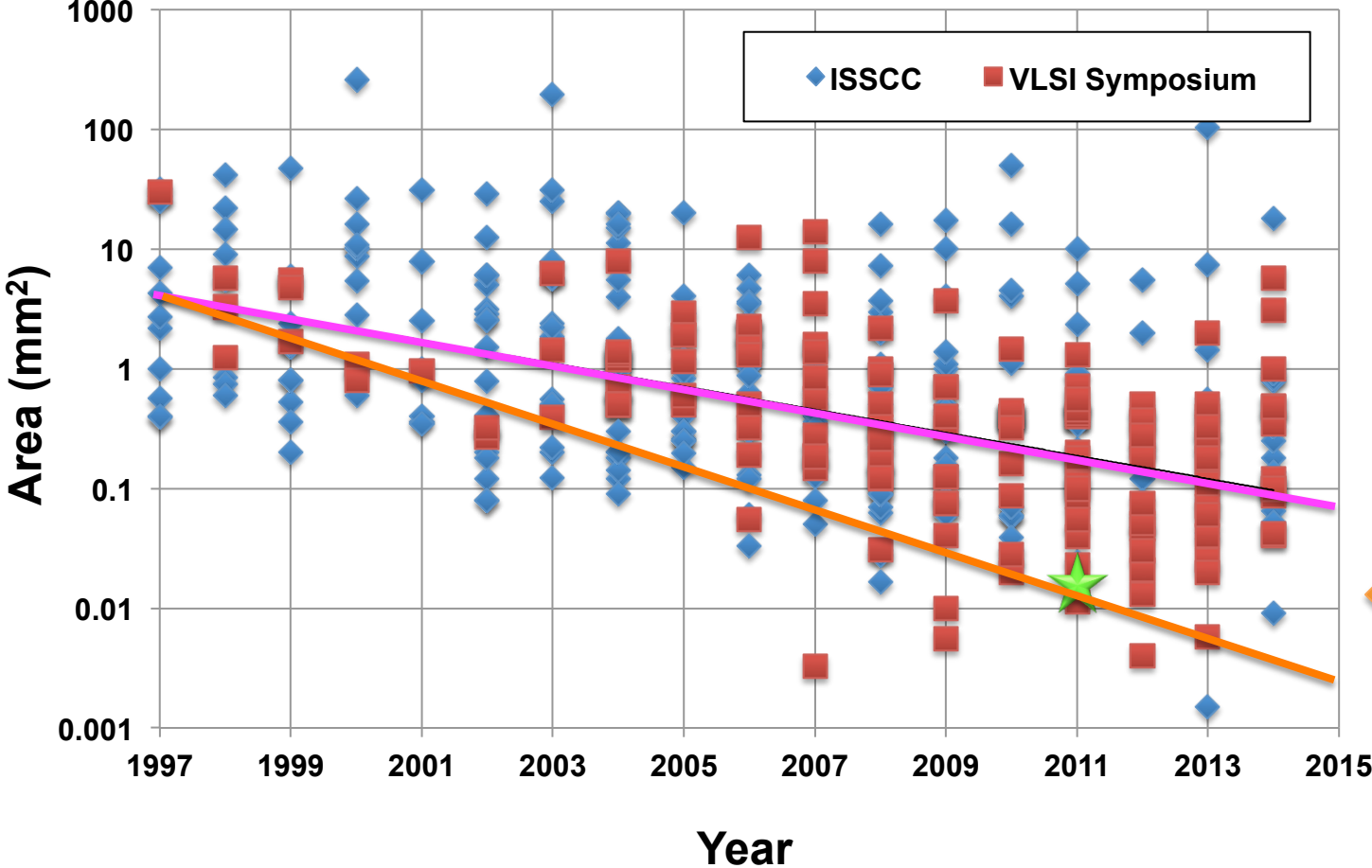
Parameter	Gen1	Gen2	Units
	Value	Value	
Process	TSMC 180nm 6M 1P	IBM 45nm SOI 10M 1P	-
Supply Voltage ( $V_{DD}$ )	1.8	1.8/1.0	V
Oversample Frequency ( $f_s$ )	144	640	MHz
Quantizer (TDC) Number of Bits	3	4	bits
DAC (DTC) Number of Bits	3	4	bits
TDC LSB ( $\Delta$ )	80	15.8	ps
$t_{d,VTC/Adde}$	2.1	714	ps
$t_{d,PhaseDetector}$	0.57	116	ps
$t_{d,DTC}$	1.24	302	ps
$t_{d,ExcessDelay}$ (Average)	2.8	400	ps
Area	0.0275	0.0192	mm <sup>2</sup>

Design  
Parameters

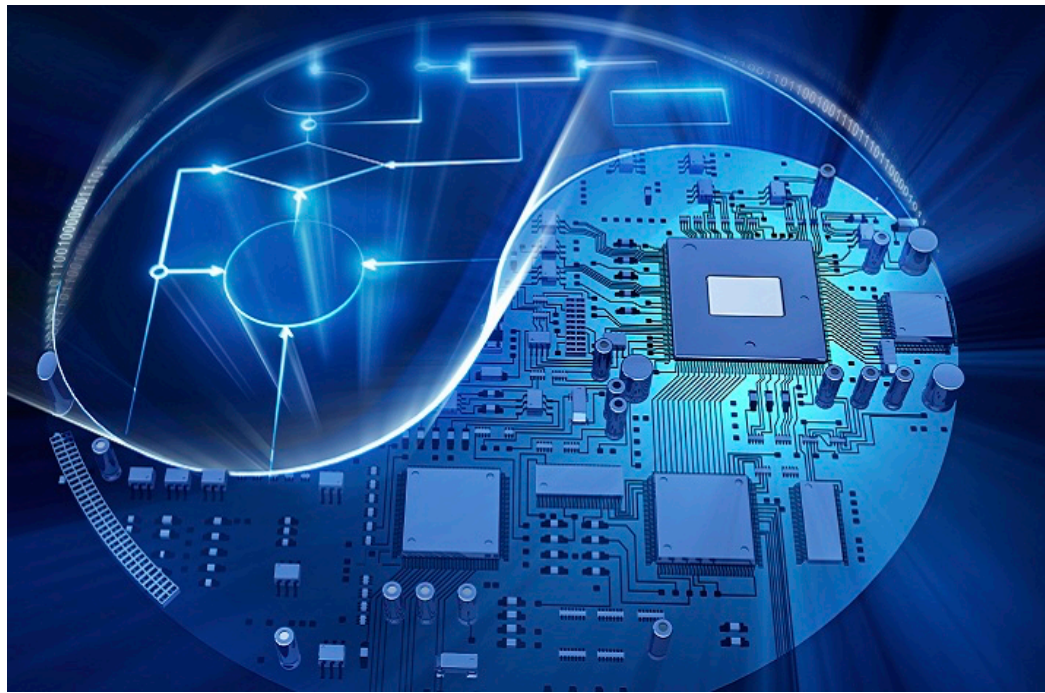
Measured  
Results

$f_s$	144	705	MHz
OSR	36	36	-
BW	2.0	9.8	MHz
$f_{in}$	146.1	500	kHz
$V_{in,pk-pk}$	400	600	mV
SNR	44.6	41.2	dB
SNDR	34.6	37.5	dB
THD	-35.0	6	bits
ENoB	5.5	-39.6	dB
Power	2.7	8.0	mW

# Analog-to-Digital Converter Area Comparison



B. Murmann, "ADC Performance Survey 1997-2015," [Online]. Available: <http://web.stanford.edu/~murmann/adcsurvey.html>.



Third Contribution

# Nonlinearity Calibration



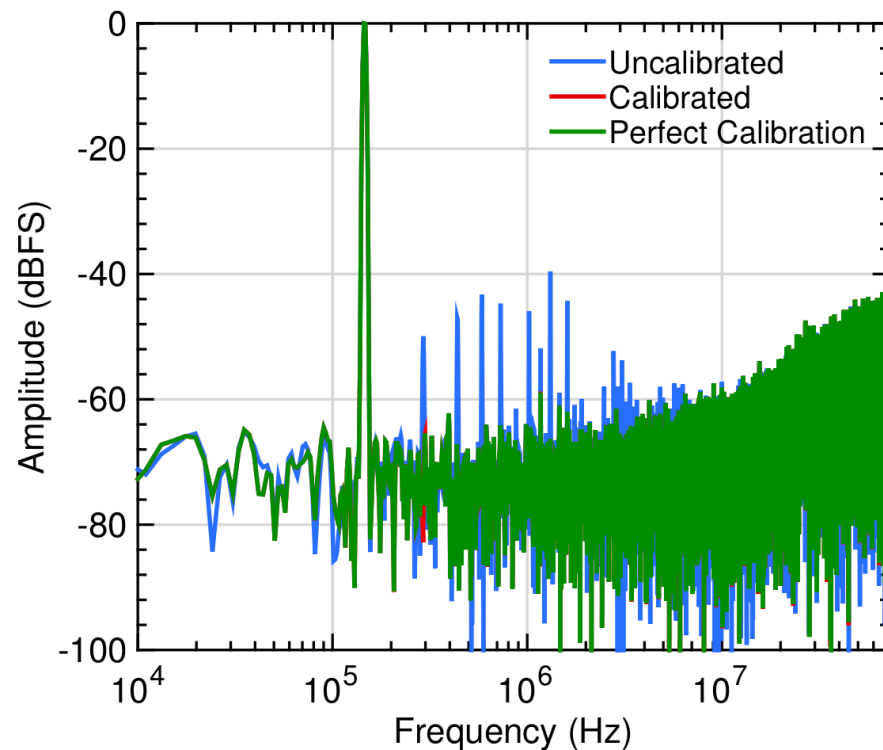
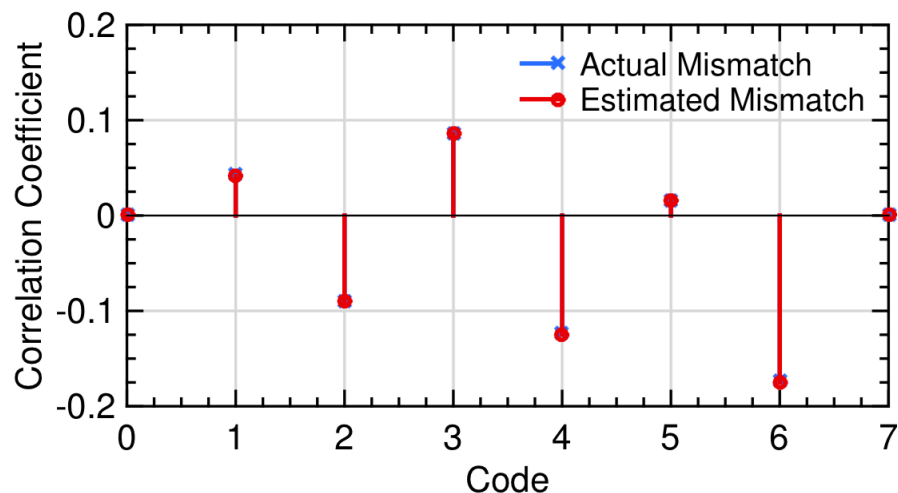
# Nonlinearity Due to Element Mismatch

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- In the presence of DTC (DAC) element mismatch Multibit DSMs exhibit harmonic distortion.
- To lower the distortion, need
  - extremely good matching, and/or
  - dynamic element matching (DEM) schemes.
- Alternatively:
  - Lookup table (LUT) that maps each code out of the modulator to the true value of the DTC can perfectly cancel nonlinearity.
- Problem:
  - How do we estimate the DTC element mismatch?

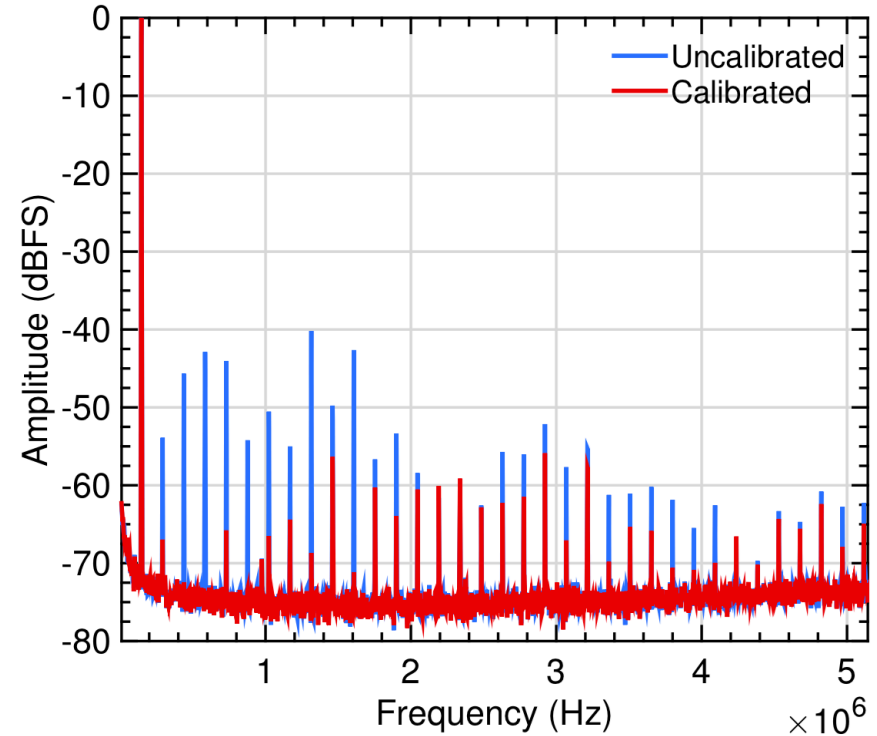
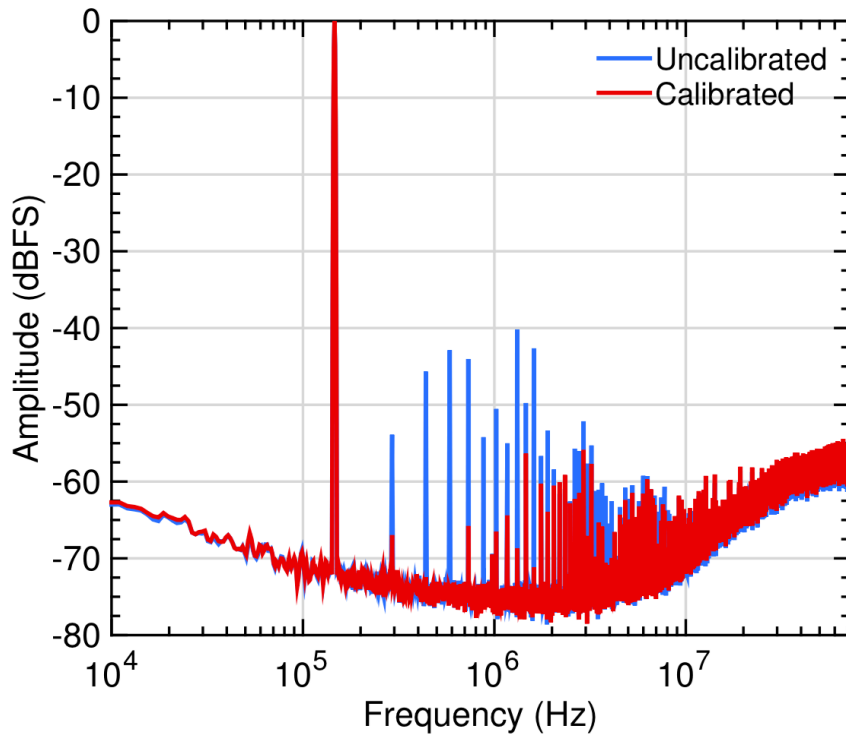


# Simulated Estimation/Calibration



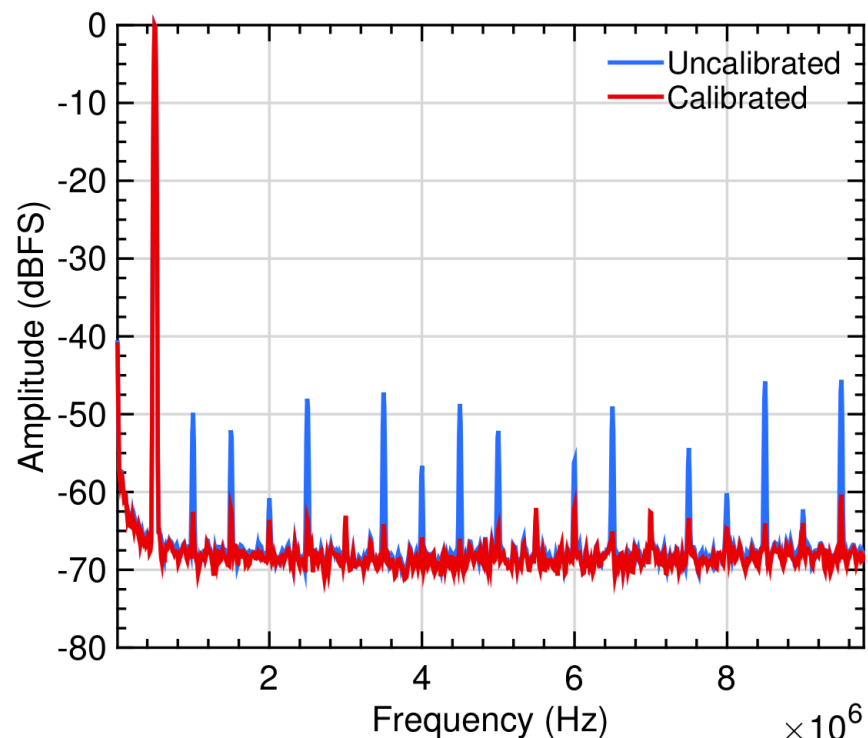
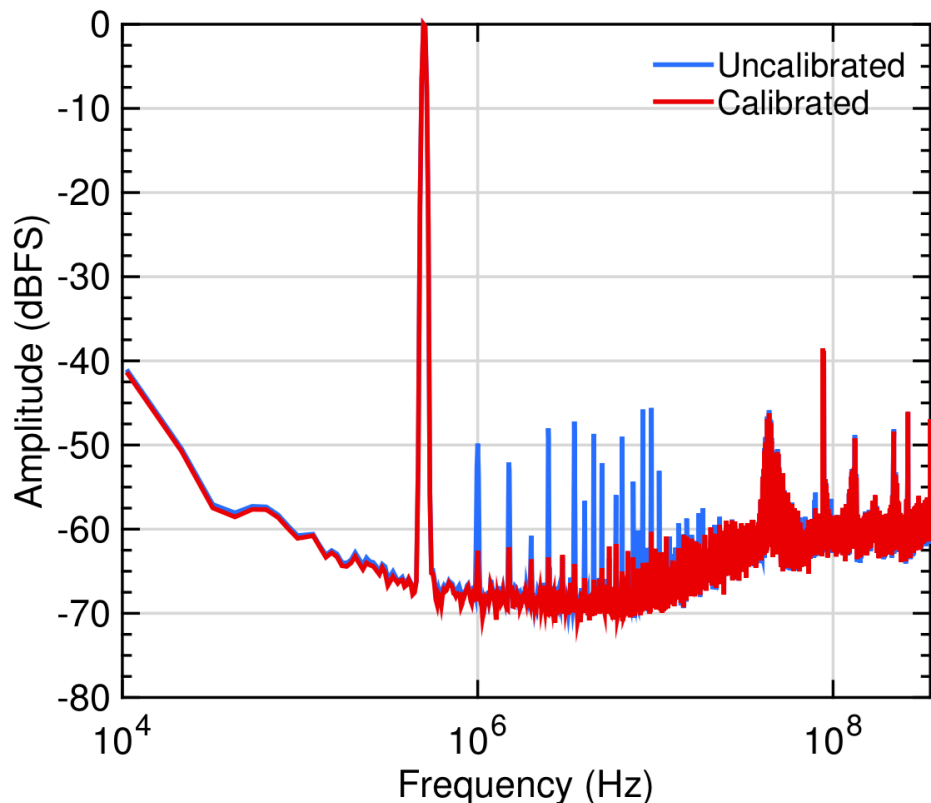
	Uncalibrated	Calibrated	Improvement	Perfect Cal.	Units
SNR	45.5	46.0	0.5	46.0	dB
SNDR	35.1	44.8	9.9	44.8	dB
THD	-35.5	-50.7	15.0	-50.7	dB
ENoB	5.5	7.2	1.7	7.2	bit

# First Generation Chip Calibration



	Uncalibrated	Calibrated	Improvement	Units
SNR	44.6	44.8	0.2	dB
SNDR	34.6	44.0	9.4	dB
THD	-35.0	-51.0	16.0	dB
ENoB	5.5	7.0	1.5	bit

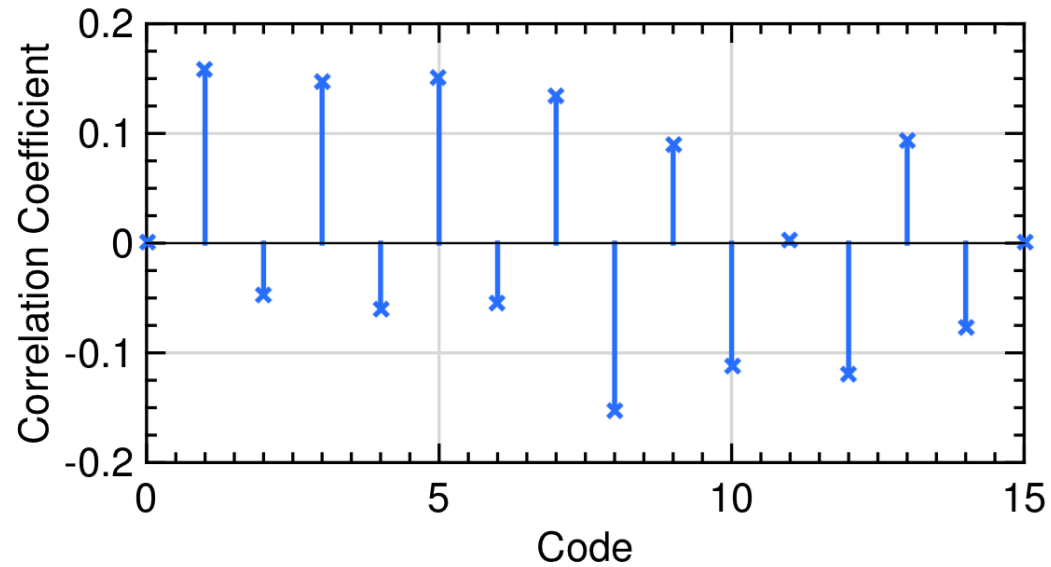
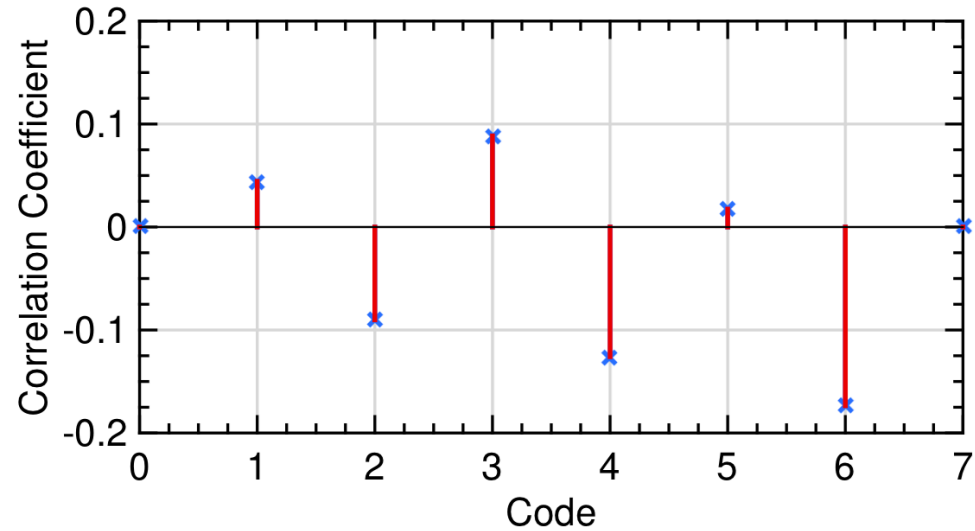
# Second Generation Chip Calibration



	Uncalibrated	Calibrated	Improvement	Units
SNR	44.6	44.8	0.2	dB
SNDR	34.6	44.0	9.4	dB
THD	-35.0	-51.0	16.0	dB
EnoB	5.5	7.0	1.5	bit

# Mismatch Coefficients

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# Summary of Contributions

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- **Contribution 1:**

Architect and model novel time-based delta sigma ADC

- Replace voltage-domain with time-domain processing to enable scaling
- Calibrate loop delay to reduce non-uniform sampling effects
- Reuse elements of TDC/DTC to save area

- **Contribution 2:**

Fabricate and test two prototype two ADC chips

- TSMC 180nm CMOS
- IBM 45nm SOI

- **Contribution 3:**

Analyze and mitigate major nonlinearity

- Estimate element mismatch coefficients
- Perform digital post-correction

# Future Work

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- Reduction in DTC unit delay element mismatch by
  - utilizing (non-inverting) buffers rather than inverters, or
  - using the same structure of DTC/TDC but with feedback that truncates the LSB, or
  - using extra inverter stages and implementing a dynamic element matching scheme.
- Circuit-level improvements
  - Improve thermal/flicker noise in front-end circuits, mainly comparator
  - Reduce power consumption of front-end by removing replica of ramp generator and comparator in the VTC/Adder and replacing it with a calibrated delay cell.

# Summary of Relevant Work by Presenter

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- Y. Mortazavi, S. M. Mortazavi Zanjani, A. Brennan, D. Allen, M. Ranjbar, A 12.6  $\mu$ W 70+ dB DR 2nd Order CT  $\Delta\Sigma$  Audio ADC in 55nm CMOS, *2015 IEEE Custom Integrated Circuits Conference*, Sep. 28-30, 2015, San Jose, CA USA, to be submitted.
- W. Jung, Y. Mortazavi, B. L. Evans, and A. Hassibi, "An all-digital PWM-based  $\Delta\Sigma$  ADC with an inherently matched multi-bit quantizer/DAC," *2014 IEEE Custom Integrated Circuits Conference*, Sep. 15-17, 2014, San Jose, CA USA.
- Y. Mortazavi, W. Jung, B. L. Evans, and A. Hassibi, "A mostly-digital PWM-based  $\Delta\Sigma$  ADC with an inherently matched multi-bit quantizer/DAC," *IEEE Transactions on Circuits and Systems II: Analog and Digital Signal Processing*, under review.
- M. Nassar, J. Lin, Y. Mortazavi, A. Dabak, I. H. Kim and B. L. Evans, "Local Utility Powerline Communications in the 3-500 kHz Band: Channel Impairments, Noise, and Standards", *IEEE Signal Processing Magazine, Special Issue on Signal Processing Techniques for the Smart Grid*, vol. 29, no. 5, pp. 116-127, Sep. 2012.
- M. Nassar, K. Gulati, Y. Mortazavi, and B. L. Evans, "Statistical Modeling of Asynchronous Impulsive Noise in Powerline Communication Networks", *Proc. IEEE Global Communications Conf.*, Dec. 5-9, 2011, Houston, TX USA.
- A. G. Olson, A. Chopra, Y. Mortazavi, I. C. Wong, and B. L. Evans, "Real-Time MIMO Discrete Multitone Transceiver Testbed", *Proc. Asilomar Conf. on Signals, Systems, and Computers*, Nov. 4-7, 2007, Pacific Grove, CA USA. [Won Best Student Paper Award for the Architecture and Implementation Track].



# References

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- [Rao2011] – S. Rao, B. Young, A. Elshazly, W. Yin, N. Sasidhar, and P. Hanumolu, “A 71dB SFDR open loop VCO-based ADC using 2-level PWM modulation,” *2011 Symp. VLSI Circuits*, pp. 270–271, June 2011.
- [Taylor2013] – G. Taylor and I. Galton, “A reconfigurable mostly-digital delta-sigma ADC with a worst-case FOM of 160dB,” *IEEE Journal of Solid-State Circuits*, vol. 48, no. 4, pp. 983 – 995, Feb. 2013.
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- [Taillefer2009] – C. S. Taillefer and G. W. Roberts, “Delta–sigma A/D conversion via time-mode signal processing,” *IEEE Transactions on Circuits and Systems I: Regular Papers*, vol. 56, no. 9, pp. 1908–1920, 2009.
- [Daniels2010] – J. Daniels, W. Dehaene, M. S. J. Steyaert, and A. Wiesbauer, “A/D conversion using asynchronous delta-sigma modulation and time-to-digital conversion,” *IEEE Transactions on Circuits and Systems I: Regular Papers*, vol. PP, no. 99, pp. 1 –1, 2010.

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Questions?

# Element Mismatch Estimation

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1. Calculate  $X[k]$ , the windowed-FFT of the modulator output ( $x[n]$ ).
2. Repeat the following for  $u \in \{1, 2, \dots, 2^{N_oB} - 2\}$ 
  - (a) Calculate  $I_u[k]$ , the windowed-FFT of the event that the modulator code equals  $u$ , i.e.,  $\mathbf{1}(x[n] = u)$ .
  - (b) Correlate a predetermined set of bins ( $k_1, \dots, k_j$ ) from  $X[k]$  with the same bins from  $I_u[k]$ . Call the result  $\epsilon[u]$ .
  - (c) Where  $x(n) = u$ , replace  $x(n)$  with  $T(u) = u + \epsilon[u]$ .

Mathematically,

$$\epsilon[u] = \frac{\sum_{k=k_1}^{k_j} \{\Re(X[k]I_u[k]) + \Im(X[k]I_u[k])\}}{\sum_{k=k_1}^{k_j} \{\Re(I_u[k]I_u[k]) + \Im(I_u[k]I_u[k])\}} \quad (7.1)$$

where  $\Re(\cdot)$  and  $\Im(\cdot)$  denote the real and imaginary parts of the argument, respectively.

