

EE382M.20: System-on-Chip (SoC) Design

Lecture 7 – Task Scheduling

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Lecture 7: Outline

- **Uni-processor scheduling**
 - Aperiodic tasks
 - Periodic tasks
 - Dependent tasks
- **Special considerations**
 - Context-switch times
 - Interrupts
- **Multi-processor scheduling**
 - MPSoC synthesis

Multiplexing Software Modules

A **B**

Call B Return

SUBROUTINES
Hierarchical
Sequential, static

A **B**

Resume B Resume A

Resume B Resume A

COROUTINES
Symmetric
Sequential, static

A **B**

PROCESSES
Symmetric
Concurrent, dynamic

Modularity Complexity

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Scheduling

- Assume that we are given a task graph $G=(V,E)$
- A *schedule* τ of G is a mapping $V \rightarrow D_t$ of a set of tasks V to start times from domain D_t , such that none overlap

$G=(V,E)$ $V1 \rightarrow V2$ $V3 \rightarrow V4$

τ

D_t t

- Find such a mapping
 - Optimize throughput (rate of G), latency (makespan of G)
 - Resource, dependency, real-time (deadline) constraints

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Task Scheduling Problems

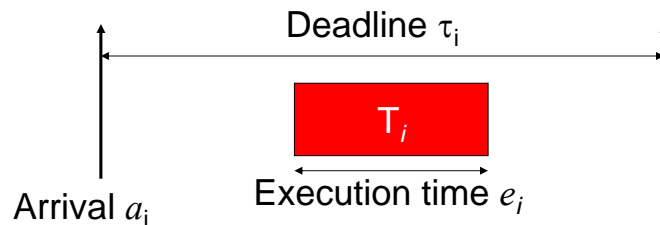
- **Task types**
 - **Periodic**
 - Set of tasks $\{ T_1, T_2, \dots \}$
 - Period t_i
 - (Worst-case) execution time e_i
 - **Aperiodic/sporadic**
 - Arrival/release time a_i
- **Task dependencies**
 - Tasks with precedence constraints
 - Dependencies, task graph
- **Preemptive vs. non-preemptive**
 - Task with higher priority can preempt lower priority one
- **Uni- vs. multi-processor scheduling**
 - Pre-defined vs. joint binding/partitioning
 - Symmetric vs. asymmetric multi-processing (SMP/AMP)
 - Homogeneous vs. heterogeneous

Uni-Processor Scheduling

- **Aperiodic, independent tasks (task set)**
 - Simultaneous (at system start) arrival times
 - Earliest Due Date (EDD) minimizes max. lateness (non-preemptive)
 - Arbitrary arrival times (statically known or dynamic)
 - Earliest Deadline First (EDF) minimizes max. lateness (preemptive)
 - Without preemption optimality only possible if arrival times known
- **Periodic, independent tasks**
 - Schedulability only (preemptive, static or dynamic)
 - Rate Monotonic Scheduling (RMS) is optimal fixed priority scheme
 - » Does not achieve 100% CPU utilization for guaranteed schedulability
 - Earliest Deadline First (EDF) is optimal dynamic priority scheme
 - » 100% utilization, but runtime support/overhead for dynamic priorities
- **Dependent tasks (task graph)**
 - Simultaneous (at system start) arrival times
 - Latest Deadline First (LDF) minimizes max. lateness (non-preempt.)
 - Arbitrary arrival times (statically known or dynamic)
 - Modified EDF* w/ successor-adjusted deadlines

Aperiodic, Independent Task Model

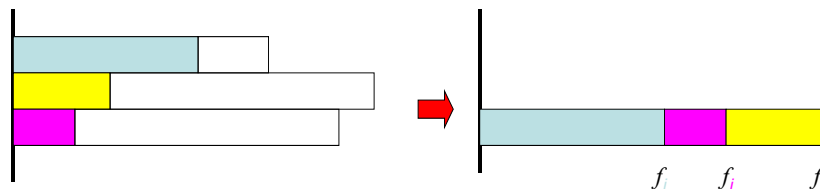
- e_i is execution time of task i
- Arrival time a_i of task i
- Deadline τ_i of task i (\rightarrow real-time!)



- **Waiting time**
 - Difference between start time s_i and arrival time a_i
- **Response time**
 - Difference between finish time f_i and arrival time a_i
- **Lateness/slack**
 - Difference between response time r_i and deadline τ_i

Simultaneous Arrival Times

- **Preemption is useless**
 - All tasks arrive at the same time
- **Total schedule makespan/length is fixed to $\sum e_i$**
 - Optimize average waiting time: Shortest Job First (SJF)
 - Optimize lateness under deadlines: real-time scheduling
- **Earliest Due Date (EDD)**
 - Execute task with earliest due date (deadline) first
 - Sort tasks by their (absolute) deadlines



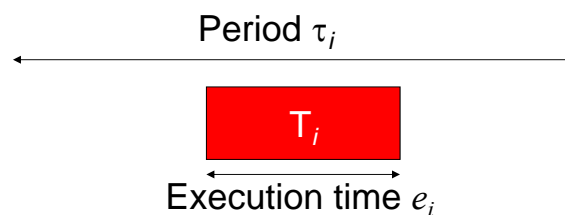
- EDD is optimal to minimize the maximum lateness

Different Arrival Times

- **Requires preemption for optimality**
 - Avg. waiting time: Shortest Remaining Time First (SRTF)
 - Real-time: Earliest Deadline First (EDF)
 - Alternative: Least Laxity (LL) / Least Slack Time First (LSF)
- **EDF and LL/LSF are optimal**
 - Minimizing maximum lateness
 - Differences in response times
- **If preemption is not allowed**
 - All arrival times need to be known to achieve optimality
 - Problem becomes NP-hard
 - EDF remains best online (unknown arrival times) algorithm

Periodic Task Model

- e_i is execution time of task i
- Tasks arrive at regular, periodic times $a_i = \{\tau_p, 2\tau_p, 3\tau_p, \dots\}$
- Deadline τ_i is period of task i (always real-time)



- **Waiting time w_i**
- **Response time r_i**
- **Lateness/slack l_i**

Scheduling Metrics

- **How do we evaluate a periodic scheduling policy**
 - Ability to satisfy all deadlines (\rightarrow real-time)
 - CPU utilization
 - Percentage of time devoted to useful work
 - Scheduling overhead
 - Time required to make scheduling decision
 - **Schedulability**
 - Find a schedule iff one exists that satisfies all deadlines
 - Worst-case CPU utilization that guarantees schedulability for any task set
- **Constraints**
 - Set of tasks T with period τ_i each
 - Response time $r_i = \text{finish time } f_i - \text{arrival time } a_i$
 - Deadline d_i ; $r_i < d_i$, in periodic case often $d_i = \tau_i$
 - Minimize latency
 - Lateness $l_i = r_i - d_i$

Periodic Task Scheduling

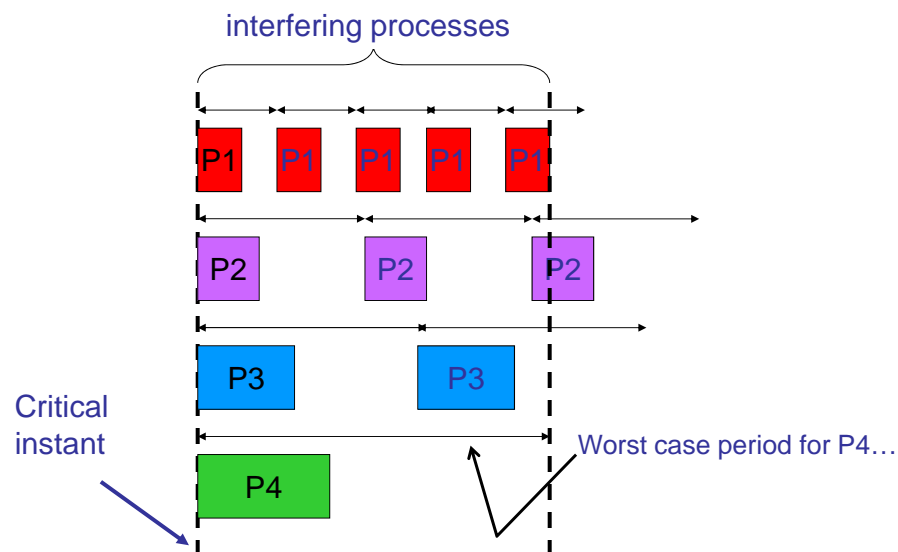
- **Scheduling Policies**
 - RMS – Rate Monotonic Scheduling
 - Task Priority = Rate = $1/\text{Period}$
 - RMS is the optimal preemptive *fixed-priority* scheduling policy
 - EDF – Earliest Deadline First
 - Task Priority = Current Absolute Deadline
 - EDF is the optimal preemptive *dynamic-priority* scheduling policy
- **Scheduling assumptions**
 - Single processor
 - All tasks are periodic
 - Zero context-switch time
 - Worst-case task execution times are known
 - No data dependencies among tasks
- **RMS and EDF have both been extended to relax these**

Rate Monotonic Scheduling (RMS)

- **Model**
 - All process run on single CPU.
 - Zero context switch time.
 - No data dependencies between processes.
 - Process execution time is constant.
 - Deadline is at end of period.
 - Highest-priority ready process runs.
- **RMS [Liu and Layland, 73]**
 - Widely-used, analyzable scheduling policy.
- **Rate Monotonic Analysis (RMA)**
 - Theoretical analysis

Critical Instant

- **Scheduling state that gives worst response time**
 - All processes become ready at the same time



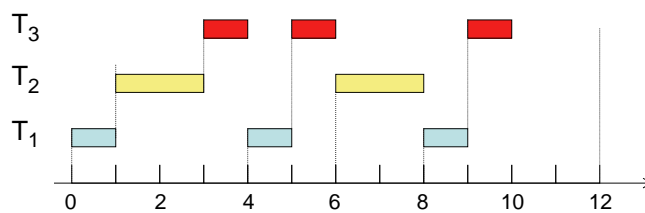
RMS Priorities

- **Optimal (fixed) priority assignment**
 - Shortest-period process gets highest priority
 - priority based preemption can be used...
 - Priority inversely proportional to period
 - Break ties arbitrarily
- **No fixed-priority scheme does better.**
 - *RMS provides the highest worst case CPU utilization while ensuring that all processes meet their deadlines*

RMS Example 1

Task T_i	Execution Time e_i	Period t_i
T_1	1	4
T_2	2	6
T_3	3	12

Static priority: $T_1 \gg T_2 \gg T_3$



Unrolled schedule

(least common multiple of process periods)

RMS CPU Utilization

- Utilization for n processes is

$$\sum_i e_i / t_i$$

- Schedulability analysis

$$\sum_i e_i / t_i \leq n(2^{1/n} - 1)$$

- As number of tasks approaches infinity, the **worst case maximum utilization approaches 69%**
 - Yet, is not uncommon to find total utilizations around .90 or more (.69 is worst case behavior of algorithm)
 - Achievable utilization is strongly dependent upon the relative values of the periods of the tasks comprising the task set...

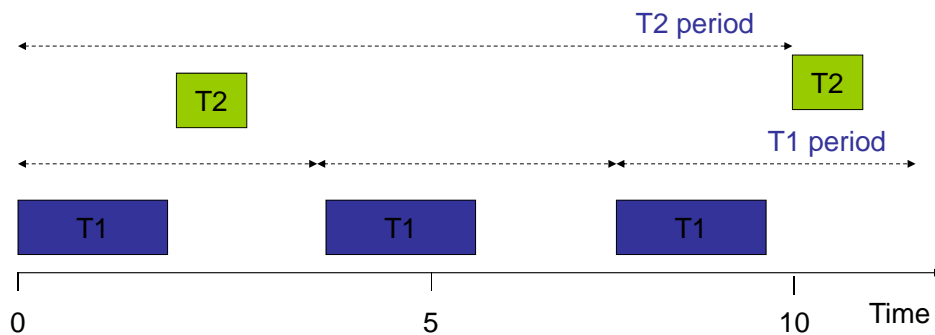
RMS Example 2

Task	Execution Time	Period
T_i	e_i	t_i
T_1	1	4
T_2	6	8

Is this task set schedulable?? If yes, give the CPU utilization.

RMS CPU Utilization (cont'd)

- RMS cannot asymptotically *guarantee* use of 100% of CPU, even with zero context switch overhead.
 - Must keep idle cycles available to handle worst-case scenario.
- However, RMS guarantees all processes will always meet their deadlines.



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RMS Implementation

- **Statically fixed priority assignment**
 - Inversely proportional to period
- **Efficient implementation**
 - Scan processes
 - Choose highest-priority active process

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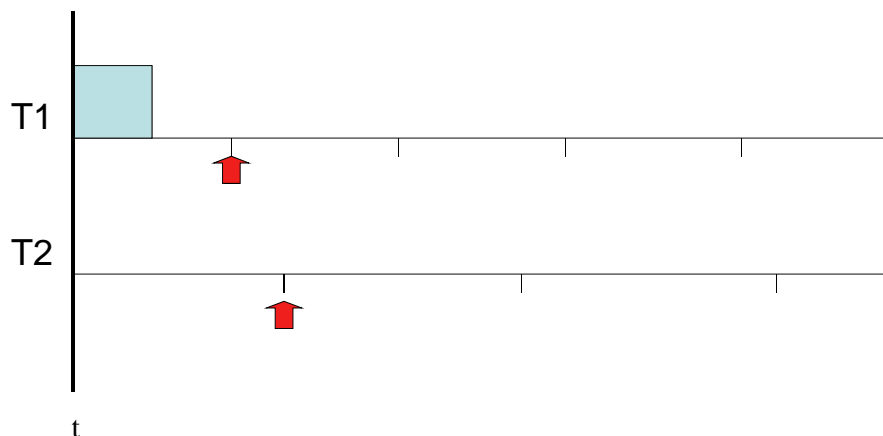
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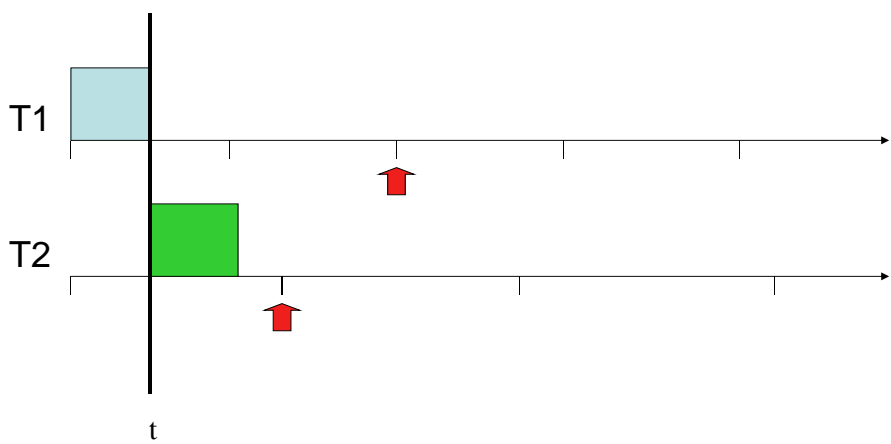
Earliest-Deadline-First (EDF) Scheduling

- **Dynamic priority scheduling scheme.**
 - Process closest to its deadline has highest priority
 - Requires recalculating processes at every timer interrupt
- **EDF analysis**
 - EDF can use 100% of CPU for worst case
 - Optimal for periodic scheduling
- **EDF implementation**
 - On each timer interrupt:
 - Compute time to deadline
 - Choose process closest to deadline
 - Generally considered too expensive to use in practice, unless the task count is small
 - Implementation on an OS with only fixed priorities [Margull'08]

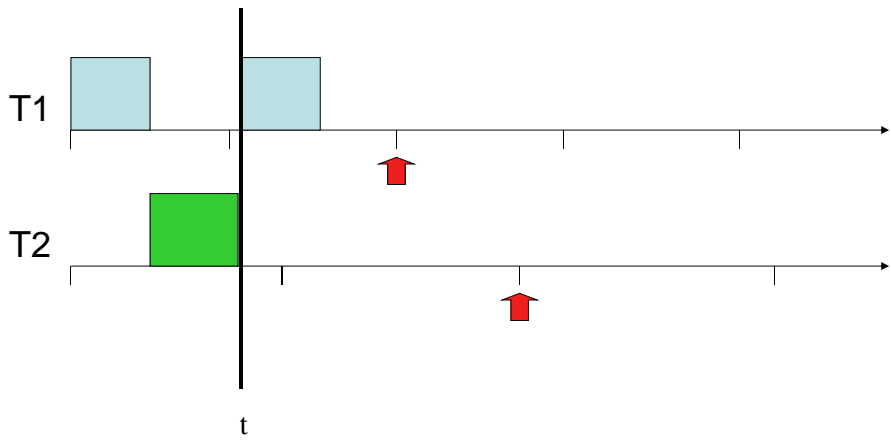
EDF Example



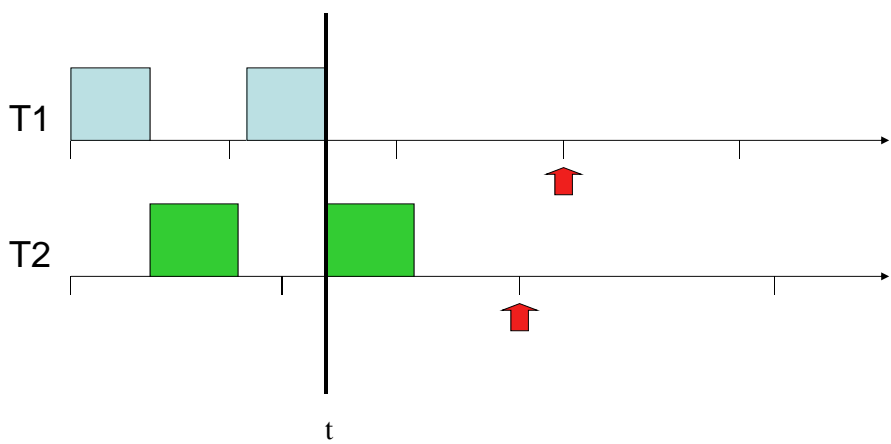
EDF Example



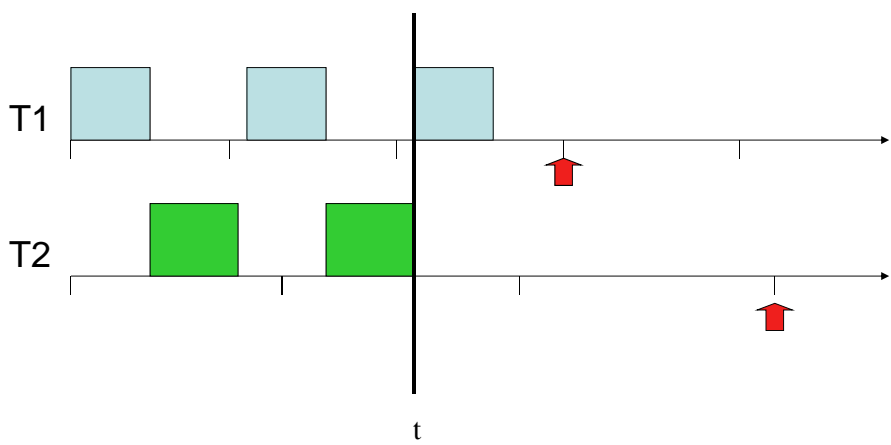
EDF Example

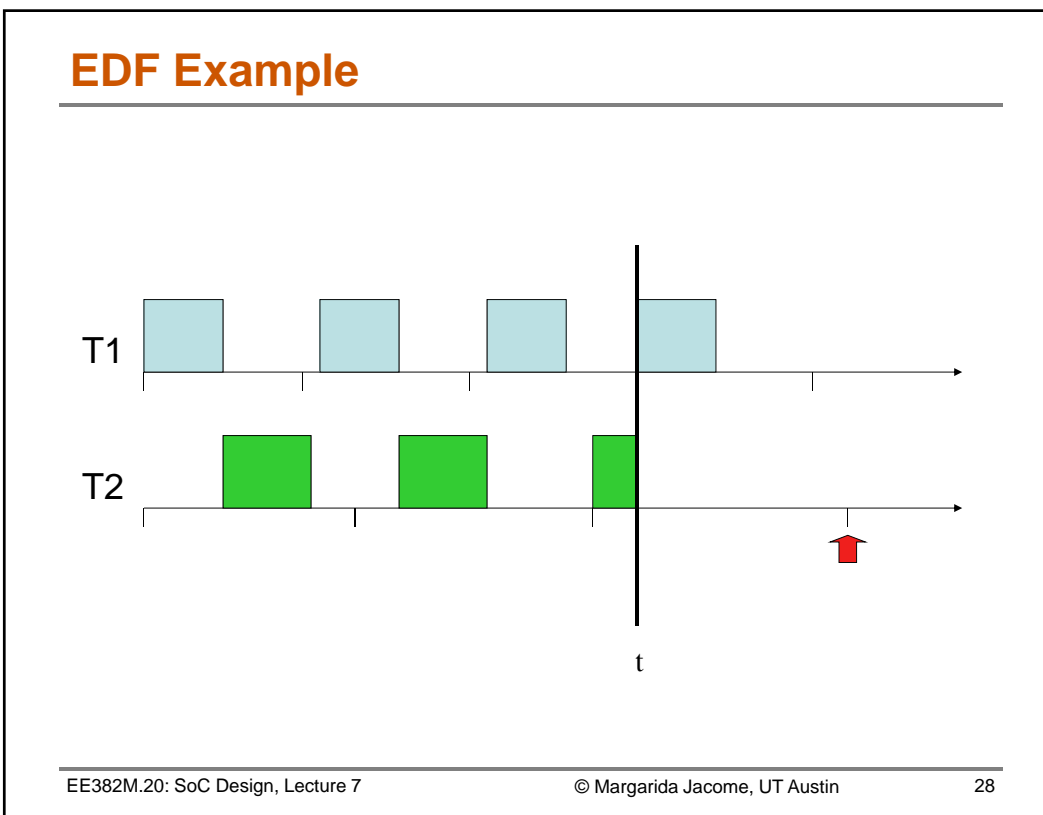
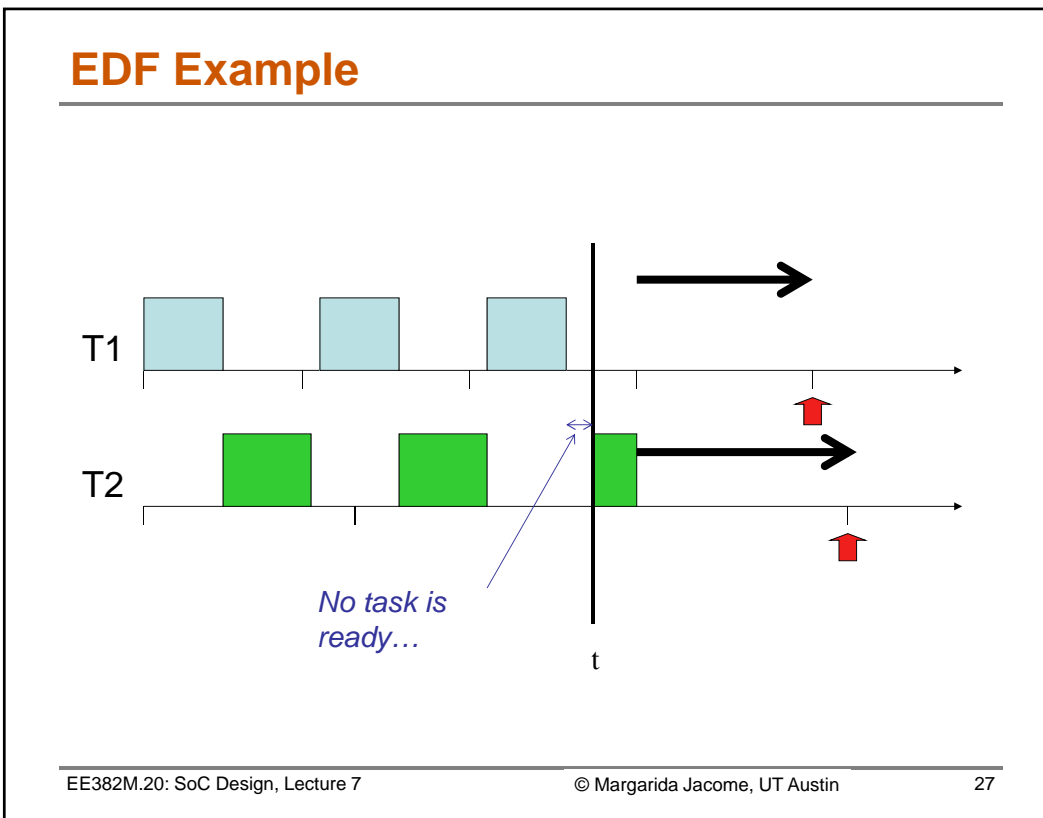


EDF Example

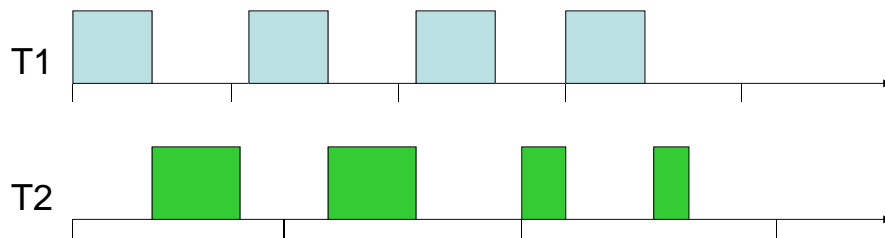


EDF Example





EDF Example



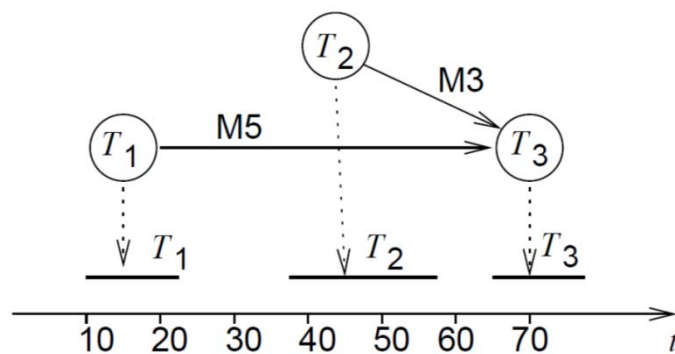
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Dependent Tasks

- Task graph



- On uni-processor, periodic derived from aperiodic

- All tasks must have same period
- Period(throughput) = $1 / \text{makespan}(\text{latency})$

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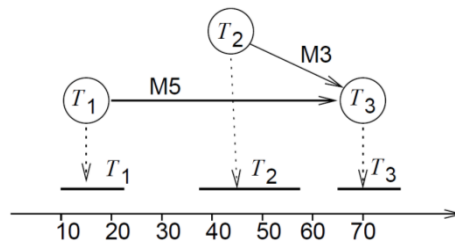
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Simultaneous Arrival Times

- **Latest Deadline First (LDF)**
 - Process task graph from sinks to sources
 - Among tasks without successors, insert the ones with the latest deadline into the schedule
 - At runtime, process in generated static reverse order

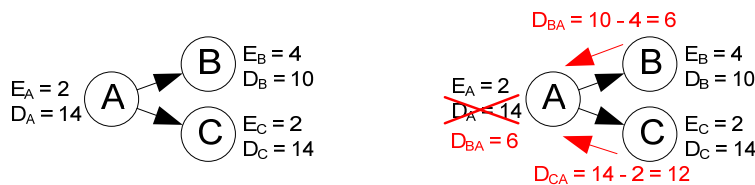
➤ **Optimal for uni-processor**

- Non-preemptive
- If no local deadlines, just topological sort



Different Arrival Times

- **Modified EDF***
 - Process graph from sinks to sources
 - Propagate deadlines adjusted for execution times
 - Under global time basis (adjusted for arrival times)
 - At each node, deadline = min(original, propagated)
 - Run regular EDF schedule for independent tasks



➤ **Optimal for uni-processor**

- Preemptive

Lecture 7: Outline

- ✓ **Uni-processor scheduling**

- ✓ Aperiodic tasks
- ✓ Periodic tasks
- ✓ Dependent tasks

- **Special considerations**

- Context-switch times
- Interrupts

- **Multi-processor scheduling**

- MPSoC synthesis

Performance Evaluation

- **Context switch time**

- Non-zero context switch time can push limits of a tight schedule
- Hard to calculate effects
 - Depends on order of context switches
- In practice, OS context switch overhead is small

- **May want to test**

- Context switch time assumptions on real platform
- Scheduling policy

What about interrupts?

- **Interrupt overhead**

- Interrupts take time away from processes
- Other event processing may be masked during interrupt service routine (ISR)
- Perform minimum work possible in the interrupt handler

- **Device processing structure**

- ISR performs minimal I/O.
 - Get register values, put register values
- Interrupt service process/thread performs most of device function
- **Sporadic tasks**
 - Frequent aperiodic tasks
 - Turn into periodic tasks via sporadic task server process



Caches

- **Processes can cause additional caching problems.**

- Even if individual processes are well-behaved, processes may interfere with each other
- Worst-case execution time with *bad cache behavior* is usually much worse than execution time with good cache behavior

- **Perform schedulability analysis without caches**

- Take any online performance gains as “free lunch”

Uni-Processor Summary

- **Scheduling**
 - Dynamic, preemptive & priority-based scheduling
 - Real-time operating system (RTOS)
 - Independent periodic tasks
 - Earliest-deadline-first (EDF)
 - Aperiodic or dependent tasks
 - EDF or modified EDF*
 - Mix of periodic/aperiodic/sporadic
 - Split into hierarchy of periodic/independent dynamic schedule with aperiodic/dependent statically scheduled subgraphs

- **What if your set of processes is unschedulable?**
 - Change deadlines in requirements.
 - Reduce execution times of processes.
 - Get a faster CPU
 - Change the partitioning!

Lecture 7: Outline

- ✓ **Uni-processor scheduling**
 - ✓ Aperiodic tasks
 - ✓ Periodic tasks
 - ✓ Dependent tasks

- ✓ **Special considerations**
 - ✓ Context-switch times
 - ✓ Interrupts

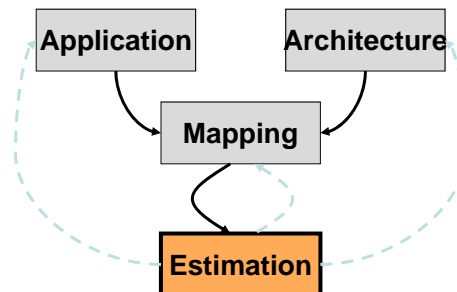
- **Muti-processor scheduling**
 - MPSoC synthesis

Multi-Processor Scheduling

- **NP-complete in general**
 - Inter-dependency with partitioning/binding
 - Use of heuristics
- **Independent tasks**
 - Partition and apply uni-processor scheduling
 - Aperiodic tasks: bin packing, longest-processing time first (LPT)
 - Uni-processor extensions to homogeneous SMP (multi-core)
 - Global EDF (non-optimal), P-Fair (optimal)
- **Dependent tasks or heterogeneous processors**
 - For simple cases, partition first and schedule separately
 - In general, solve partitioning & scheduling jointly
 - Heuristics from compilers & high-level synthesis (Lecture 12)
 - MPSoC Synthesis

MPSoC Synthesis

- **Design space exploration (DSE)**
 - General application MoCs & architectures
 - Multi-objective, Pareto optimality
 - Traditional HW/SW co-design approaches not sufficient
- **Iterative process**
 - Determine mapping
 - Partitioning & scheduling
 - Evaluate solutions



- **EE382V: Embedded System Design & Modeling**