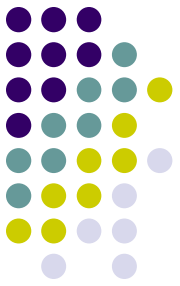
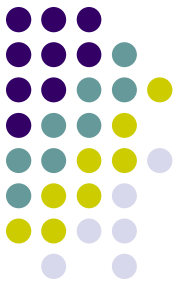


Design of Experiments - Terminology



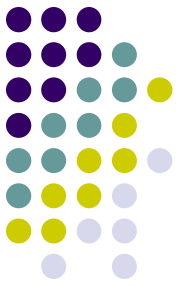
- Response variable
 - Measured output value
 - E.g. total execution time
- Factors
 - Input variables that can be changed
 - E.g. cache size, clock rate, bytes transmitted
- Levels
 - Specific values of factors (inputs)
 - Continuous (~bytes) or discrete (type of system)



A Problem

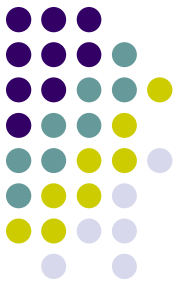
- *Full factorial design with replication*
 - Measure system response with all possible input combinations
 - Replicate each measurement n times to determine effect of measurement error
- m factors, v levels, n replications
 - $n v^m$ experiments
- $m = 5$ input factors, $v = 4$ levels, $n = 3$
 - → $3(4^5) = 3,072$ experiments!

Fractional Factorial Designs: $n2^m$ Experiments

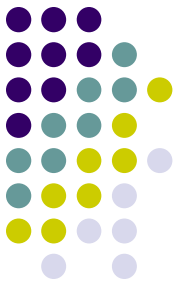


- Special case of generalized m -factor experiments
- Restrict each factor to two possible values
 - High, low
 - On, off
- Find factors that have largest impact
- Full factorial design with only those factors

Still Too Many Experiments with $n2^m$!

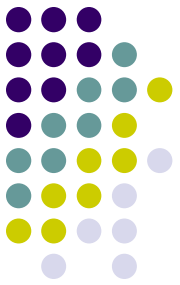


- Plackett and Burman designs (1946)
 - Multifactorial designs
- Effects of main factors only
 - Logically minimal number of experiments to estimate effects of m input parameters (factors)
 - Ignores interactions
- Requires $O(m)$ experiments
 - Instead of $O(2^m)$ or $O(v^m)$



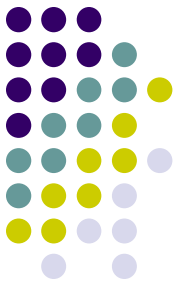
Plackett and Burman Designs

- PB designs exist only in sizes that are multiples of 4
- Requires X experiments for m parameters
 - $X = \text{next multiple of } 4 \geq m$
- PB design matrix
 - Rows = configurations
 - Columns = parameters' values in each config
 - High/low = +1/ -1
 - First row = from P&B paper
 - Subsequent rows = circular right shift of preceding row
 - Last row = all (-1)



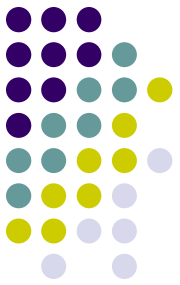
PB Design Matrix

Config	Input Parameters (factors)							Response
	A	B	C	D	E	F	G	
1	+1	+1	+1	-1	+1	-1	-1	9
2	-1	+1	+1	+1	-1	+1	-1	
3	-1	-1	+1	+1	+1	-1	+1	
4	+1	-1	-1	+1	+1	+1	-1	
5	-1	+1	-1	-1	+1	+1	+1	
6	+1	-1	+1	-1	-1	+1	+1	
7	+1	+1	-1	+1	-1	-1	+1	
8	-1	-1	-1	-1	-1	-1	-1	
Effect								



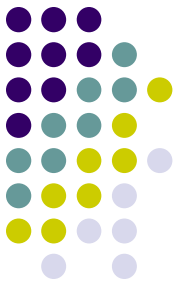
PB Design Matrix

Config	Input Parameters (factors)							Response
	A	B	C	D	E	F	G	
1	+1	+1	+1	-1	+1	-1	-1	9
2	-1	+1	+1	+1	-1	+1	-1	11
3	-1	-1	+1	+1	+1	-1	+1	
4	+1	-1	-1	+1	+1	+1	-1	
5	-1	+1	-1	-1	+1	+1	+1	
6	+1	-1	+1	-1	-1	+1	+1	
7	+1	+1	-1	+1	-1	-1	+1	
8	-1	-1	-1	-1	-1	-1	-1	
Effect								



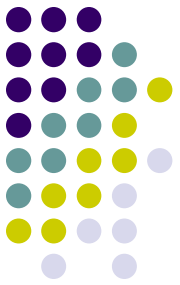
PB Design Matrix

Config	Input Parameters (factors)							Response
	A	B	C	D	E	F	G	
1	+1	+1	+1	-1	+1	-1	-1	9
2	-1	+1	+1	+1	-1	+1	-1	11
3	-1	-1	+1	+1	+1	-1	+1	2
4	+1	-1	-1	+1	+1	+1	-1	1
5	-1	+1	-1	-1	+1	+1	+1	9
6	+1	-1	+1	-1	-1	+1	+1	74
7	+1	+1	-1	+1	-1	-1	+1	7
8	-1	-1	-1	-1	-1	-1	-1	4
Effect								



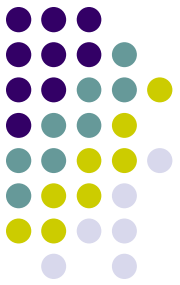
PB Design Matrix

Config	Input Parameters (factors)							Response
	A	B	C	D	E	F	G	
1	+1	+1	+1	-1	+1	-1	-1	9
2	-1	+1	+1	+1	-1	+1	-1	11
3	-1	-1	+1	+1	+1	-1	+1	2
4	+1	-1	-1	+1	+1	+1	-1	1
5	-1	+1	-1	-1	+1	+1	+1	9
6	+1	-1	+1	-1	-1	+1	+1	74
7	+1	+1	-1	+1	-1	-1	+1	7
8	-1	-1	-1	-1	-1	-1	-1	4
Effect	65							



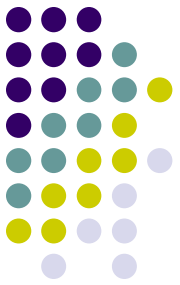
PB Design Matrix

Config	Input Parameters (factors)							Response
	A	B	C	D	E	F	G	
1	+1	+1	+1	-1	+1	-1	-1	9
2	-1	+1	+1	+1	-1	+1	-1	11
3	-1	-1	+1	+1	+1	-1	+1	2
4	+1	-1	-1	+1	+1	+1	-1	1
5	-1	+1	-1	-1	+1	+1	+1	9
6	+1	-1	+1	-1	-1	+1	+1	74
7	+1	+1	-1	+1	-1	-1	+1	7
8	-1	-1	-1	-1	-1	-1	-1	4
Effect	65	-45						



PB Design Matrix

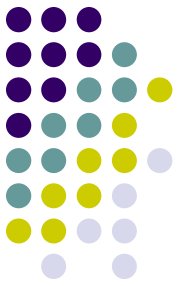
Config	Input Parameters (factors)							Response
	A	B	C	D	E	F	G	
1	+1	+1	+1	-1	+1	-1	-1	9
2	-1	+1	+1	+1	-1	+1	-1	11
3	-1	-1	+1	+1	+1	-1	+1	2
4	+1	-1	-1	+1	+1	+1	-1	1
5	-1	+1	-1	-1	+1	+1	+1	9
6	+1	-1	+1	-1	-1	+1	+1	74
7	+1	+1	-1	+1	-1	-1	+1	7
8	-1	-1	-1	-1	-1	-1	-1	4
Effect	65	-45	75	-75	-75	73	67	



PB Design

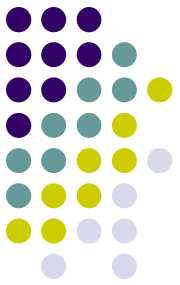
- Only magnitude of effect is important
 - Sign is meaningless
- In example, **most** → **least** important effects:
 - $[C, D, E] \rightarrow F \rightarrow G \rightarrow A \rightarrow B$

PB Design Matrix with Foldover



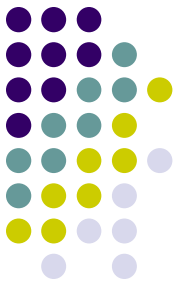
- Add X additional rows to matrix
 - Signs of additional rows are opposite original rows
- Provides some additional information about selected interactions

PB Design Matrix with Foldover



A	B	C	D	E	F	G	Exec. Time
+1	+1	+1	-1	+1	-1	-1	9
-1	+1	+1	+1	-1	+1	-1	11
-1	-1	+1	+1	+1	-1	+1	2
+1	-1	-1	+1	+1	+1	-1	1
-1	+1	-1	-1	+1	+1	+1	9
+1	-1	+1	-1	-1	+1	+1	74
+1	+1	-1	+1	-1	-1	+1	7
-1	-1	-1	-1	-1	-1	-1	4
-1	-1	-1	+1	-1	+1	+1	17
+1	-1	-1	-1	+1	-1	+1	76
+1	+1	-1	-1	-1	+1	-1	6
-1	+1	+1	-1	-1	-1	+1	31
+1	-1	+1	+1	-1	-1	-1	19
-1	+1	-1	+1	+1	-1	-1	33
-1	-1	+1	-1	+1	+1	-1	6
+1	+1	+1	+1	+1	+1	+1	112
191	19	111	-13	79	55	239	

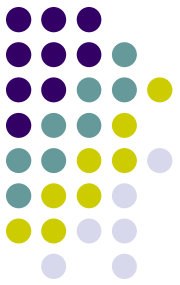
Case Study #1



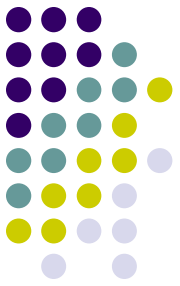
- Determine the most significant parameters in a processor simulator.
- [Yi, Lilja, & Hawkins, HPCA, 2003.]



Determine the Most Significant Processor Parameters

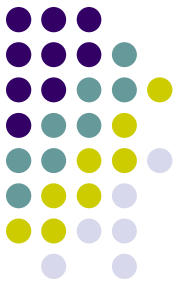


- Problem
 - So many parameters in a simulator
 - How to choose parameter values?
 - How to decide which parameters are most important?
- Approach
 - Choose reasonable upper/lower bounds.
 - Rank parameters by impact on total execution time.



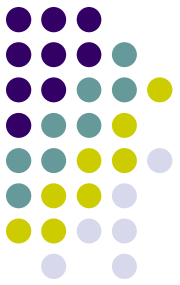
Simulation Environment

- SimpleScalar simulator
 - sim-outorder 3.0
- Selected SPEC 2000 Benchmarks
 - *gzip, vpr, gcc, mesa, art, mcf, equake, parser, vortex, bzip2, twolf*
- MinneSPEC Reduced Input Sets
- Compiled with gcc (PISA) at O3



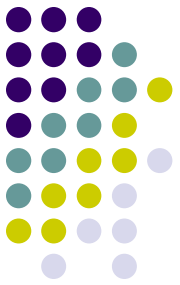
Functional Unit Values

Parameter	Low Value	High Value
Int ALUs	1	4
Int ALU Latency	2 Cycles	1 Cycle
Int ALU Throughput	1	
FP ALUs	1	4
FP ALU Latency	5 Cycles	1 Cycle
FP ALU Throughputs	1	
Int Mult/Div Units	1	4
Int Mult Latency	15 Cycles	2 Cycles
Int Div Latency	80 Cycles	10 Cycles
Int Mult Throughput	1	
Int Div Throughput	Equal to Int Div Latency	
FP Mult/Div Units	1	4
FP Mult Latency	5 Cycles	2 Cycles
FP Div Latency	35 Cycles	10 Cycles
FP Sqrt Latency	35 Cycles	15 Cycles
FP Mult Throughput	Equal to FP Mult Latency	
FP Div Throughput	Equal to FP Div Latency	
FP Sqrt Throughput	Equal to FP Sqrt Latency	



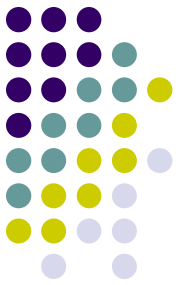
Memory System Values, Part I

Parameter	Low Value	High Value
L1 I-Cache Size	4 KB	128 KB
L1 I-Cache Assoc	1-Way	8-Way
L1 I-Cache Block Size	16 Bytes	64 Bytes
L1 I-Cache Repl Policy	Least Recently Used	
L1 I-Cache Latency	4 Cycles	1 Cycle
L1 D-Cache Size	4 KB	128 KB
L1 D-Cache Assoc	1-Way	8-Way
L1 D-Cache Block Size	16 Bytes	64 Bytes
L1 D-Cache Repl Policy	Least Recently Used	
L1 D-Cache Latency	4 Cycles	1 Cycle
L2 Cache Size	256 KB	8192 KB
L2 Cache Assoc	1-Way	8-Way
L2 Cache Block Size	64 Bytes	256 Bytes



Memory System Values, Part II

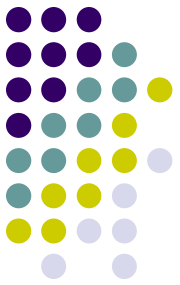
Parameter	Low Value	High Value
L2 Cache Repl Policy	Least Recently Used	
L2 Cache Latency	20 Cycles	5 Cycles
Mem Latency, First	200 Cycles	50 Cycles
Mem Latency, Next	0.02 * Mem Latency, First	
Mem Bandwidth	4 Bytes	32 Bytes
I-TLB Size	32 Entries	256 Entries
I-TLB Page Size	4 KB	4096 KB
I-TLB Assoc	2-Way	Fully Assoc
I-TLB Latency	80 Cycles	30 Cycles
D-TLB Size	32 Entries	256 Entries
D-TLB Page Size	Same as I-TLB Page Size	
D-TLB Assoc	2-Way	Fully-Assoc
D-TLB Latency	Same as I-TLB Latency	



Processor Core Values

Parameter	Low Value	High Value
Fetch Queue Entries	4	32
Branch Predictor	2-Level	Perfect
Branch MPred Penalty	10 Cycles	2 Cycles
RAS Entries	4	64
BTB Entries	16	512
BTB Assoc	2-Way	Fully-Assoc
Spec Branch Update	In Commit	In Decode
Decode/Issue Width	4-Way	
ROB Entries	8	64
LSQ Entries	$0.25 * \text{ROB}$	$1.0 * \text{ROB}$
Memory Ports	1	4

Determining the Most Significant Parameters

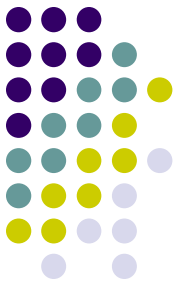


1. Run simulations to find **response**

- With input parameters at high/low, on/off values

Config	Input Parameters (factors)							Response
	A	B	C	D	E	F	G	
1	+1	+1	+1	-1	+1	-1	-1	9
2	-1	+1	+1	+1	-1	+1	-1	
3	-1	-1	+1	+1	+1	-1	+1	
...	...	...	...	...	...	...	...	
Effect								

Determining the Most Significant Parameters

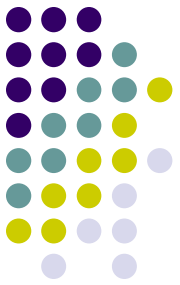


2. Calculate the **effect** of each parameter

- Across configurations

Config	Input Parameters (factors)							Response
	A	B	C	D	E	F	G	
1	+1	+1	+1	-1	+1	-1	-1	9
2	-1	+1	+1	+1	-1	+1	-1	
3	-1	-1	+1	+1	+1	-1	+1	
...	...	...	...	...	...	...	...	
Effect	65							

Determining the Most Significant Parameters

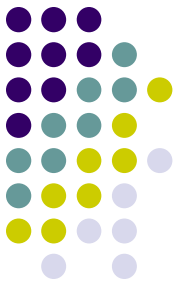


3. For each benchmark

Rank the parameters in descending order of effect
(1=most important, ...)

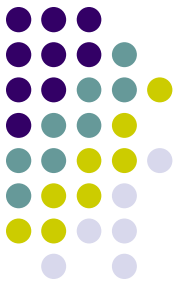
Parameter	Benchmark 1	Benchmark 2	Benchmark 3
A	3	12	8
B	29	4	22
C	2	6	7
...	...	...	...

Determining the Most Significant Parameters



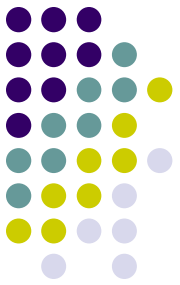
4. For each parameter
Average the ranks

Parameter	Benchmark 1	Benchmark 2	Benchmark 3	Average
A	3	12	8	7.67
B	29	4	22	18.3
C	2	6	7	5
...	...	...	...	...



Most Significant Parameters

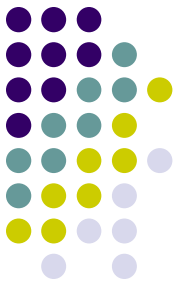
Number	Parameter	gcc	gzip	art	Average
1	ROB Entries	4	1	2	2.77
2	L2 Cache Latency	2	4	4	4.00
3	Branch Predictor Accuracy	5	2	27	7.69
4	Number of Integer ALUs	8	3	29	9.08
5	L1 D-Cache Latency	7	7	8	10.00
6	L1 I-Cache Size	1	6	12	10.23
7	L2 Cache Size	6	9	1	10.62
8	L1 I-Cache Block Size	3	16	10	11.77
9	Memory Latency, First	9	36	3	12.31
10	LSQ Entries	10	12	39	12.62
11	Speculative Branch Update	28	8	16	18.23



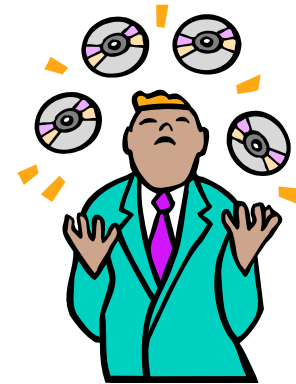
General Procedure

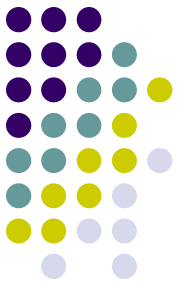
- Determine upper/lower *bounds* for parameters
- Simulate configurations to find *response*
- Compute *effects* of each parameter for each configuration
- *Rank* the parameters for each benchmark based on effects
- *Average* the ranks across benchmarks
- Focus on *top-ranked* parameters for subsequent analysis

Case Study #2



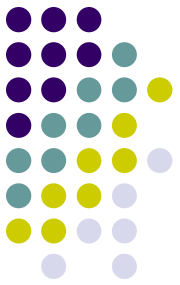
- Benchmark program classification.





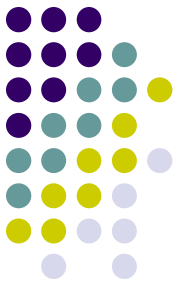
Benchmark Classification

- By application type
 - Scientific and engineering applications
 - Transaction processing applications
 - Multimedia applications
- By use of processor function units
 - Floating-point code
 - Integer code
 - Memory intensive code
- Etc., etc.



Another Point-of-View

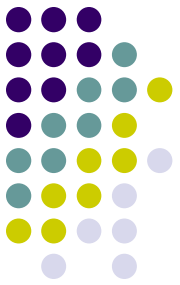
- Classify by overall *impact* on processor
- Define:
 - Two benchmark programs are **similar** if –
 - They stress the same components of a system to similar degrees
- How to measure this similarity?
 - Use Plackett and Burman design to find ranks
 - Then compare ranks



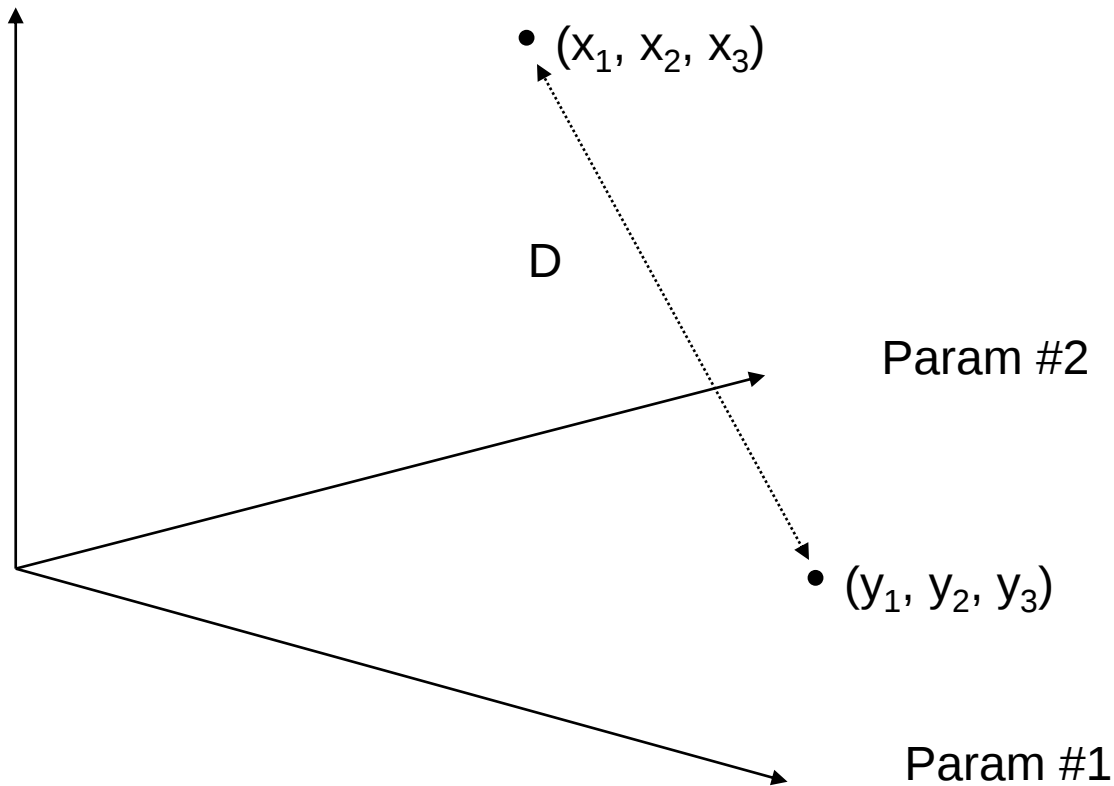
Similarity metric

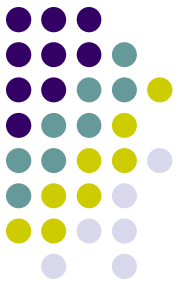
- Use **rank** of each parameter as elements of a vector
- For benchmark program X , let
 - $\mathbf{X} = (x_1, x_2, \dots, x_{n-1}, x_n)$
 - x_1 = rank of parameter 1
 - x_2 = rank of parameter 2
 - ...

Vector Defines a Point in n -space



Param #3

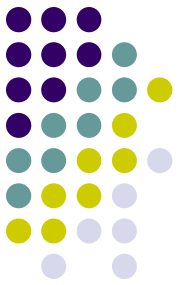




Similarity Metric

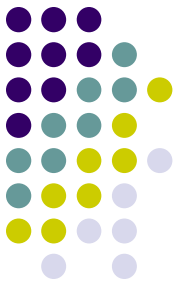
- Euclidean Distance Between Points

$$D = [(x_1 - y_1)^2 + (x_2 - y_2)^2 + \dots + (x_{n-1} - y_{n-1})^2 + (x_n - y_n)^2]^{1/2}$$



Most Significant Parameters

Number	Parameter	gcc	gzip	art
1	ROB Entries	4	1	2
2	L2 Cache Latency	2	4	4
3	Branch Predictor Accuracy	5	2	27
4	Number of Integer ALUs	8	3	29
5	L1 D-Cache Latency	7	7	8
6	L1 I-Cache Size	1	6	12
7	L2 Cache Size	6	9	1
8	L1 I-Cache Block Size	3	16	10
9	Memory Latency, First	9	36	3
10	LSQ Entries	10	12	39
11	Speculative Branch Update	28	8	16



Distance Computation

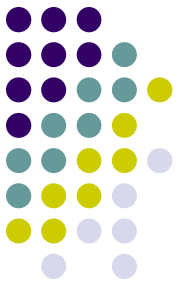
- Rank vectors

- $G_{cc} = (4, 2, 5, 8, \dots)$
- $G_{zip} = (1, 4, 2, 3, \dots)$
- $A_{rt} = (2, 4, 27, 29, \dots)$

- Euclidean distances

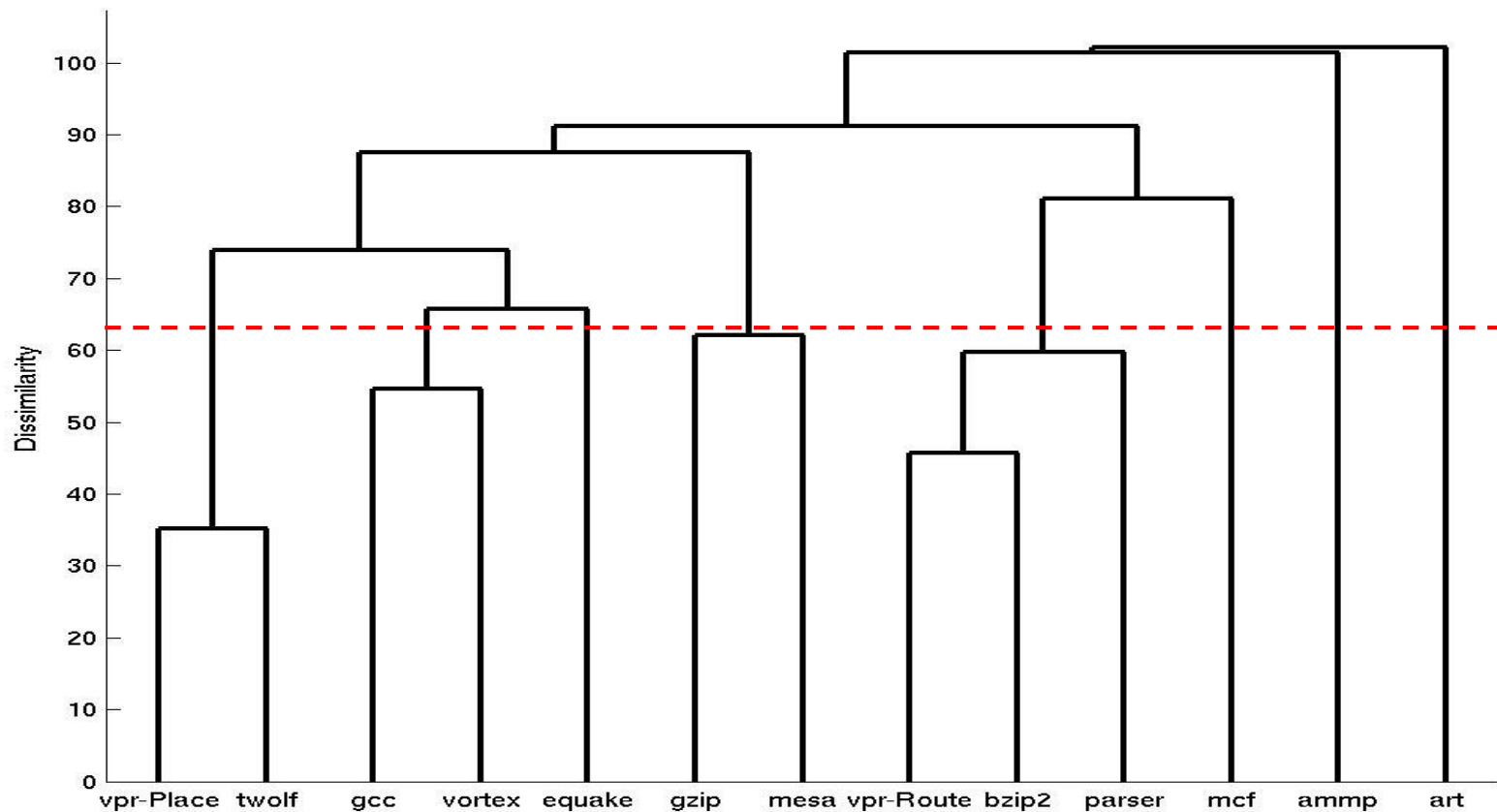
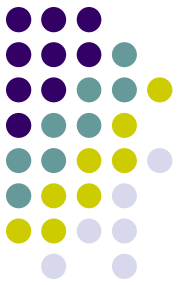
- $D(g_{cc} - g_{zip}) = [(4-1)^2 + (2-4)^2 + (5-2)^2 + \dots]^{1/2}$
- $D(g_{cc} - a_{rt}) = [(4-2)^2 + (2-4)^2 + (5-27)^2 + \dots]^{1/2}$
- $D(g_{zip} - a_{rt}) = [(1-2)^2 + (4-4)^2 + (2-27)^2 + \dots]^{1/2}$

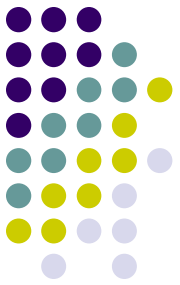
Euclidean Distances for Selected Benchmarks



	gcc	gzip	art	mcf
gcc	0	81.9	92.6	94.5
gzip		0	113.5	109.6
art			0	98.6
mcf				0

Dendrogram of Distances Showing (Dis-)Similarity

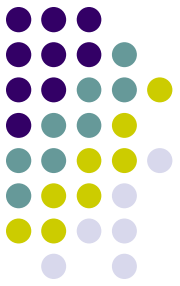




Final Benchmark Groupings

Group	Benchmarks
I	Gzip, mesa
II	Vpr-Place, twolf
III	Vpr-Route, parser, bzip2
IV	Gcc, vortex
V	Art
VI	Mcf
VII	Equake
VIII	ammp

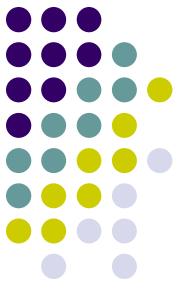
Case Study #3



- Determine the “big picture” impact of a system enhancement.

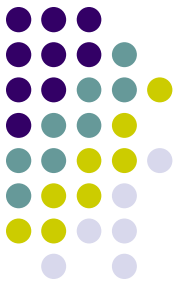


Determining the Overall Effect of an Enhancement



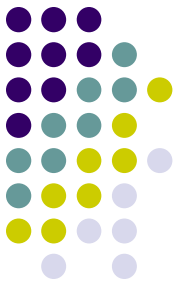
- Problem:
 - Performance analysis is typically limited to single metrics
 - Speedup, power consumption, miss rate, etc.
 - Simple analysis
 - Discards a lot of good information

Determining the Overall Effect of an Enhancement



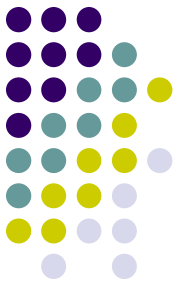
- Find most important parameters **without** enhancement
 - Using Plackett and Burman
- Find most important parameters **with** enhancement
 - Again using Plackett and Burman
- Compare parameter ranks

Example: Instruction Precomputation



- Profile to find the most common operations
 - $0+1$, $1+1$, etc.
- Insert the results of common operations in a table when the program is loaded into memory
- Query the table when an instruction is issued
- Don't execute the instruction if it is already in the table
- Reduces contention for function units

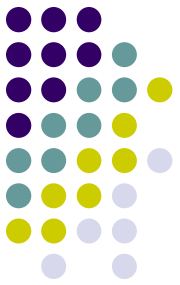
The Effect of Instruction Precomputation



Average Rank

Parameter	Before	After	Difference
ROB Entries	2.77		
L2 Cache Latency	4.00		
Branch Predictor Accuracy	7.69		
Number of Integer ALUs	9.08		
L1 D-Cache Latency	10.00		
L1 I-Cache Size	10.23		
L2 Cache Size	10.62		
L1 I-Cache Block Size	11.77		
Memory Latency, First	12.31		
LSQ Entries	12.62		

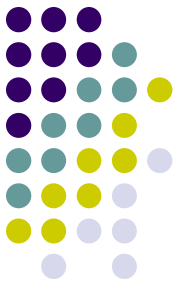
The Effect of Instruction Precomputation



Average Rank

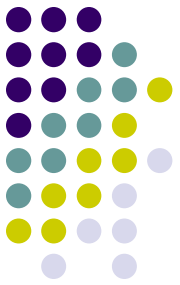
Parameter	Before	After	Difference
ROB Entries	2.77	2.77	
L2 Cache Latency	4.00	4.00	
Branch Predictor Accuracy	7.69	7.92	
Number of Integer ALUs	9.08	10.54	
L1 D-Cache Latency	10.00	9.62	
L1 I-Cache Size	10.23	10.15	
L2 Cache Size	10.62	10.54	
L1 I-Cache Block Size	11.77	11.38	
Memory Latency, First	12.31	11.62	
LSQ Entries	12.62	13.00	

The Effect of Instruction Precomputation



Average Rank

Parameter	Before	After	Difference
ROB Entries	2.77	2.77	0.00
L2 Cache Latency	4.00	4.00	0.00
Branch Predictor Accuracy	7.69	7.92	-0.23
Number of Integer ALUs	9.08	10.54	-1.46
L1 D-Cache Latency	10.00	9.62	0.38
L1 I-Cache Size	10.23	10.15	0.08
L2 Cache Size	10.62	10.54	0.08
L1 I-Cache Block Size	11.77	11.38	0.39
Memory Latency, First	12.31	11.62	0.69
LSQ Entries	12.62	13.00	-0.38



Summary

- Plackett and Burman (*multi-factorial design*)
- $O(m)$ experiments
- Main effects only
 - *No interactions*
- For only 2 input values (high/low, on/off)
- Examples – rank parameters, group benchmarks, overall impact of an enhancement