ECE 306 Fall 2023
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Final Exam
Dec. 8th, 2023

Name and EID: $\qquad$

## Part A:

Problem 1 (10 points): $\qquad$
Problem 2 (10 points): $\qquad$
Problem 3 (10 points): $\qquad$
Problem 4 (10 points): $\qquad$
Problem 5 (10 points): $\qquad$
Part A Total: $\qquad$

Total (130 points): $\qquad$
Note: Please be sure that your answers to all questions (and all supporting work that is required) are contained in the space provided.

Note: Please be sure your name is recorded on each sheet of the exam.

Please read the following sentence, and if you agree, sign where requested:
I have not given nor received any unauthorized help on this exam.

Signature: $\qquad$

Name: $\qquad$
Question 1 (10 Points): Shown below is a transistor circuit with three inputs (A, B, C) and one output (Z). Also shown is the truth table for this circuit. The outputs of the truth table are not shown.

Your job: Complete the truth table. Every input combination produces an output of either 0 or 1.


| $A$ | $B$ | $C$ | $Z$ |
| :--- | :--- | :--- | :--- |
| 0 | 0 | 0 |  |
| 0 | 0 | 1 |  |
| 0 | 1 | 0 |  |
| 0 | 1 | 1 |  |
| 1 | 0 | 0 |  |
| 1 | 0 | 1 |  |
| 1 | 1 | 0 |  |
| 1 | 1 | 1 |  |

$\qquad$
Question 2 (10 Points): We wish to implement a new instruction that swaps 2 values, one in a register and one in memory. The instruction's format is shown below. SR1 contains a value to be swapped and SR2 contains an address to a location in memory that has the other value to be swapped.


The changes to the datapath are bolded in the diagram below.

$\qquad$
Part A: Complete the state machine for the swap instruction below.
State 32


Part B: Fill out the control signals for the states listed in the table below:

| State | J | GATE.MDR | GATE.TEMP | LD.TEMP | LD.MDR | LD.MAR |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 41 |  |  |  |  |  |  |
| 43 |  |  |  |  |  |  |

Name: $\qquad$
Question 3 (10 Points): We want to design the state machine for an automatic bird feeder. It has two types of feed: millets and sunflower seeds. The system takes 1 bit of input, and outputs 2 bits. The input and output are described below.

| Sensor Readings (inputs) |  |
| :---: | :--- |
| Input | Description |
| 0 | Empty |
| 1 | Not Empty |

Bird Feeder Actions (outputs)

| Out[1] | Out[0] | Description |
| :---: | :---: | :--- |
| 0 | 0 | Do nothing |
| 0 | 1 | Fill with millets |
| 1 | 0 | Fill with sunflower seeds |

Birds need a varied diet so our bird feeder alternates between sunflower seeds and millet. Every hour the feeder will read the sensor. If it is empty, it will fill with the opposite food choice. If it is not empty, it will do nothing. The feeder starts empty, and should be filled with millet.

Part A: Complete the finite state machine below that allows the bird feeder to operate as described. The 2-bit number on the top-right corner of each state is the state number for that state.


Name: $\qquad$
Part B: Complete the truth table corresponding to the state machine from part A.

| State[1] | State[0] | Input | Out[1] | Out[0] | Next State[1] | Next State[0] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 |  |  |  |  |
| 0 | 0 | 1 |  |  |  |  |
| 0 | 1 | 0 |  |  |  |  |
| 0 | 1 | 1 |  |  |  |  |
| 1 | 0 | 0 |  |  |  |  |
| 1 | 0 | 1 |  |  |  |  |
| 1 | 1 | 0 |  |  |  |  |
| 1 | 1 | 1 |  |  |  |  |

Part C: Draw the logic gate implementation for Out[1]. Use only AND, OR, and NOT gates.
$\square$

Name: $\qquad$
Question 4 (10 Points): What value is stored in the location labeled RESULT when the following program terminates?

|  | .ORIG $\times 3000$ |  |  |
| :---: | :---: | :---: | :---: |
|  | AND | R1, | R1, \#0 |
|  | LEA | R0, | LABEL1 |
| LOOP | LDR | R0, | R0, \#0 |
|  | BRz | DONE |  |
|  | LDR | R2, | R0, \#1 |
|  | ADD | R1, | R1, R2 |
|  | BRnzp L00P |  |  |
| DONE | ST | R1, | RESULT |
|  | HALT |  |  |
| RESULT | . BLKW | \#1 |  |
| LABEL1 | . FILL $\times 6000$ |  |  |
|  | . END |  |  |
|  | . ORIG |  | $\times 6000$ |
|  | .FILL |  | $\times 5010$ |
|  | .FILL |  | X0300 |
|  | . END |  |  |
|  | . ORIG |  | $\times 5010$ |
|  | .FILL |  | x4020 |
|  | .FILL |  | xFFFF |
|  | . END |  |  |
|  | . ORIG |  | x4020 |
|  | .FILL |  | x0000 |
|  | .FILL |  | x0007 |
|  | .END |  |  |

What kind of data structure does this program operate on?
$\square$

Name: $\qquad$
Question 5 (10 Points): A student wrote a program to multiply two positive numbers X and Y , and store the product in memory location x4002. M[x4000] contains the value $\mathrm{X} . \mathrm{M}[\mathrm{x} 4001]$ contains the value Y . Unfortunately she spends too much time watching football, so there is a bug in her code.

|  | .ORIG x3000 |  |  |
| :---: | :---: | :---: | :---: |
|  | LDI | R1, | X |
|  | LDI | R2, | Y |
|  | AND | R0, | R0, \#0 |
| LOOP | ADD | R0, | R0, R2 |
|  | ADD | R1, | R1, \#-1 |
|  | BRz | LOOP |  |
|  | STI | R0, | RESULT |
|  | HALT |  |  |
| X | . FILL $\times 4000$ |  |  |
| Y | .FILL $\times 4001$ |  |  |
| RESULT | .FILL $\times 4002$ |  |  |
|  | . END |  |  |

Your job: Circle the instruction causing the bug, and replace it in the box below with the correct instruction.

Name: $\qquad$
Question 6 ( 20 Points): You are given a program that takes 2 inputs from memory and stores the result of execution in an unknown memory location. During the execution of the program, we took 7 snapshots of the LC-3 microarchitecture. The first snapshot was taken during the first clock cycle of the program execution. Subsequent snapshots are shown in the table below in the order in which they are taken. Each snapshot contains the state number, the value on the bus during the clock cycle, and the control signals necessary to execute the state.

Part A: Fill in the blanks in the code and table. Use X if a control signal value doesn't matter.
.ORIG x3000

|  | LD | R0, | OUTPUT |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | LDR | R1, | R0 | \#16 | ;INPUT 1 |
|  | BRz | DONE |  |  |  |
|  | LDR | R2, | R0, | \#18 | ;INPUT 2 |
| LOOP | JSR | SUBTR | ACT |  |  |
|  | ADD | R1, | R0, | \#0 |  |
|  | BRzp | LOOP |  |  |  |
|  | ADD | R1, | R0, | R2 |  |
| DONE | STI | R1, | OUTPUT |  |  |
|  | HALT |  |  |  |  |
| OUTPUT | .FILL |  |  |  |  |
| SUBTRACT | NOT R0, R2 |  |  |  |  |
|  | ADD R0, R0, \#1 |  |  |  |  |
|  | ADD R0, R1, R0 |  |  |  |  |
|  | RET |  |  |  |  |
|  | . END |  |  |  |  |

(The first row of the table has been given to you as an example.)

| State | BUS | Control Signals |
| :---: | :---: | :---: |
| 18 | x3000 | LD.MAR = 1, GatePC = 1, LD.PC = 1, PCMUX = PC +1 |
| 6 | x4257 | LD.MAR = 1, ALUK = , SR1MUX = |
| 6 | x4259 | LD.MAR = 1, ALUK = , SR1MUX = |
| 9 | xFFF5 | LD.REG $=1, \mathrm{DR}=\mathrm{IR}[11: 9], \mathrm{ALUK}=\mathrm{NOT}, \mathrm{SR} 1 \mathrm{MUX}=\mathrm{IR}[8: 6]$ |
| 21 |  | LD.REG = 1, DRMUX = , , ADDR2MUX = |
| 16 | - | LD. MDR = __ , MIO.EN = __, R.W = ___, LD. MAR = |
|  | - | LD.BEN = _ , $\mathrm{J}=\ldots, \mathrm{l}$, |

Part B: Given the above table, and the fact that the RET instruction was executed 7 times, what were the inputs if R1 has value $\times 0000$ when the program terminates?

Input 1: $\qquad$ Input 2: $\qquad$

Name: $\qquad$
Question 7 (20 Points): An programmer did a poor job implementing some important features in the operating system. Thankfully, he did manage to implement TRAPs. The table below shows how the memory in the system region is configured at the start of the program. Recall the exception vector for privilege mode exception is $x 00$, for illegal opcode is x 01 , and for access control violation is x 02 .

| Memory Address | Data | Comments |
| :--- | :--- | :--- |
| $\ldots$ |  |  |
| $x 0100$ | $x 1500$ |  |
| $x 0101$ | $x 1510$ |  |
| $x 0102$ | $x 1520$ |  |
| $\ldots$ |  |  |
| $x 1500$ | $x 8000$ |  |
| $\ldots$ | $x 8000$ |  |
| $x 1510$ |  |  |
| $\ldots$ | $x D 025$ |  |
| $x 1520$ |  |  |
| $\ldots$ |  |  |

Table below shows the user program to be executed. The user program starts executing at x3000 with priority 0 .

| Memory Address | Data | Assembly | Comments |  |
| :--- | :--- | :--- | :--- | :--- |
| x3000 | x5020 | AND R0, R1, \#0 | ; Start of User Program |  |
| x3001 | x103F | ADD $\quad$ R0, R0, \#-1 |  |  |
| x3002 | xA003 | C | LDI $\quad$ R0, A |  |
| x3003 | x07FE | BRzp C |  |  |
| x3004 | xA002 | LDI $\quad$ R0, B |  |  |
| x3005 | xF025 |  | TRAP $\quad$ x25 |  |
| x3006 | x0E00 | A | .FILL x0E00 |  |
| x3007 | x0E01 | B | .FILL x0E01 |  |

Name: $\qquad$
Part A: During the first 300 cycles of executing this program, what exception(s) occur if any? Assume that each memory access takes 5 cycles. Also, use the state diagram and the datapath that handles interrupts and exceptions.
$\square$
Part B: What is in memory locations x2FFC~x2FFF after 300 cycles of execution?

| Memory Address | Content |
| :--- | :--- |
| x2FFC |  |
| x2FFD |  |
| x2FFE |  |
| x2FFF |  |

Part C: Suppose the operating system engineering changes the access control violation service routine as follows.

|  | ST | R0, | SAVE_R0 |  |
| :--- | :--- | :--- | :--- | :--- |
|  | LDR | R0, | R6, | $\# 0$ |
|  | ADD | R0, | R0, | $\# 1$ |
|  | STR | R0, | R6, | $\# 0$ |
|  | LDR | R0, | R0, | $\#-1$ |
|  | ST | R0, | LABEL |  |
| LABEL | LD | R0, | SAVE_R0 |  |
|  | BLKW \#1 |  |  |  |
| SAVE R0 | RTI |  |  |  |
|  | .BLKW | $\# 1$ |  |  |

He hopes to fix the exception by executing the faulting instruction in privileged mode. Unfortunately, the code above does not do what he wishes for the user program on the previous page. Why?

Name: $\qquad$
Question 8 (20 Points): A binary tree is a common data structure, used to represent (among other things) family trees and organization charts. A binary tree consists of nodes, connected by links as shown in the example below.


If this tree were an organization chart, C would be the CEO and o and e employees who report directly to him. If the tree were a family tree, C would be the patriarch.

Each link connects a "parent" node to one of its possible "child" nodes. For example, node o has two children nodes, $m$ and $p$. Node $r$ has no children. Every node except one has a single parent. The node that does not have a parent is called the "root." Each node can have up to two children. The children are the roots of subtrees. For example, the entire tree has a root (node C), a left subtree (consisting of nodes $\mathrm{o}, \mathrm{m}, \mathrm{p}, \mathrm{u}, \mathrm{t}$ ) and a right subtree (consisting of node e and r ). Node o is the root of a subtree having a left subtree (consisting of node m ) and a right subtree (consisting of nodes $\mathrm{p}, \mathrm{u}$, and t ).

Unlike a linked list which has only one order in which all the nodes of the link list can be visited, the nodes of a tree can be visited in several different orders. One of the orders is called "pre-order traversal," in which the root is visited first, then all the nodes of its left subtree, then all the nodes of its right subtree. In the tree above the pre-order traversal visits $C$ then $o, m, p$, $u, t, e$, and $r$ in that order.

If we identify the data of each node as the ASCII code of a typed character, each node in the tree above occupies three words of LC-3 memory as shown below: a link to the left child, a link to the right child, and the data (ascii code). If the node does not have a left (or right) subtree, the corresponding link is x 0000 .

## Left Child Pointer

## Right Child Pointer

## ASCII Character

Name: $\qquad$
Below is a program which prints all the characters in the tree in the order described above. For each node it visits, it keeps track of the right child (if there is one), and then follows the left child. When it visits a node with no left child, the program goes through the right children in reverse order. Assume the tree is already in memory with the root at address $\times 4000$.

Your Job: Fill in the missing instructions.

> .ORIG x3000
> LD R6, STACK
> LD R1,
$\qquad$
LOOP
TRAP x21 ; OUT

LDR R0, R1, \#1
BRz SKIP

SKIP
LDR R1, R1, \#0
BR_LOOP
LD R2,
ADD R0, R2, R6
BRz DONE
BR__ LOOP

DONE HALT

TREE_ROOT .FILL x4000
DONE_VAL .FILL x0200 ; xFE00+x0200=x0000
STACK .FILL xFE00
.END

Name: $\qquad$
Question 9 (20 Points): In this question, we modify how JSRIJSRR and RET works in LC3. JSR/JSRR will use the stack as the linkage instead of R7 by pushing the return PC onto the stack. Similarly, RET will load the PC with the value popped from the top of the stack.

In memory, there are 10 subroutines to print the 10 digits. For example, the subroutine to print the number " 5 " consists of the following instructions:

| Print5 | LD R0 Label5 |
| :--- | :--- |
|  | OUT |
|  | RET |
| Label5 | .FILL $x 35$ |

Since each subroutine requires 4 memory locations, the starting address of each subroutine is always 4 greater than the starting address of the previous subroutine. The starting address of the subroutine Print0 is $\times 5000$. Therefore, the starting address of the subroutine Print1 is $\times 5004$, the starting address of the subroutine Print2 is $\times 5008$, and so on.

A student wishes to surprise Dr. Patt by printing our course number " 306 " with a program that does not use any JSR/JSRR instructions nor I/O trap service routines in the main program.
Your Job: Fill in the blanks in the main program, so that executing this program will result in printing the digits " 306 " on the console, and then halt the machine.

Hint: What happens when a RET is executed without a JSR being executed beforehand?
. ORIG $\times 3000$

$\qquad$
-

HALT
SP_INIT .FILL xFE00

## . END

